

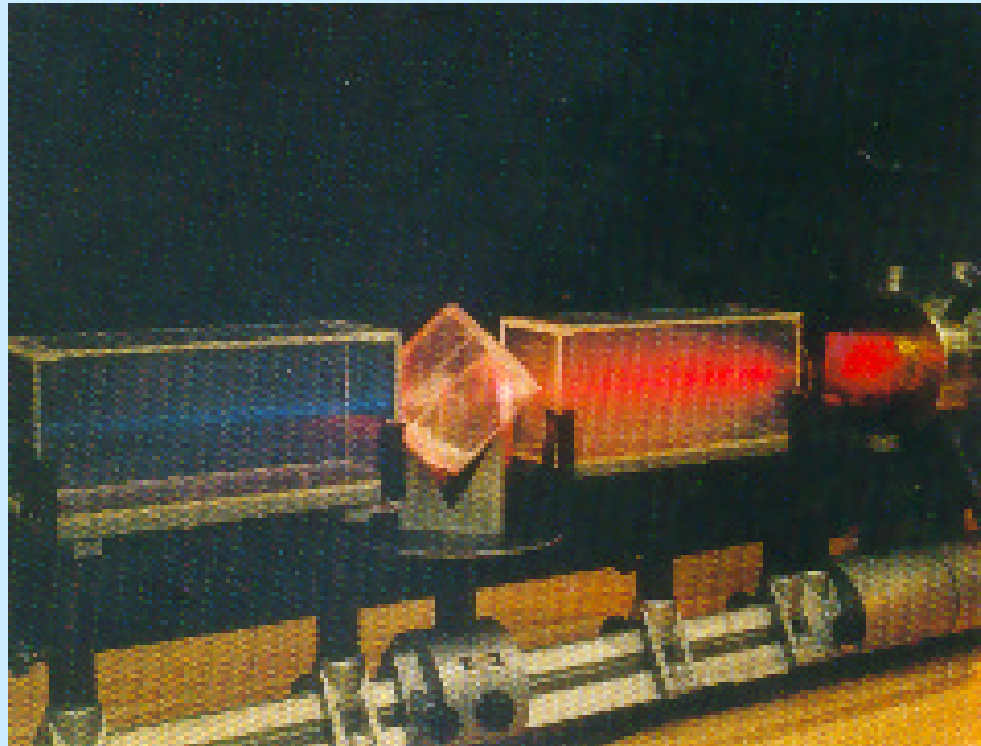
ONERA

The logo for ONERA (Office National d'Études et de Recherches Aéronautiques) features the word "ONERA" in a black, sans-serif font. Below the text is a thin horizontal line, and further down is a blue, curved line that arches over the text.

Les Oscillateurs Paramétriques Optiques: fondements et Applications

E. ROSENER
DSG/ONERA

Tout a commencé comme ça...

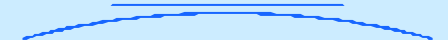


T.H. Maiman, Nature (1960)



P.A. Franken, A.E. Hill, C.W. Peters and G. Weireich, Phys. Rev. Lett. (1961)

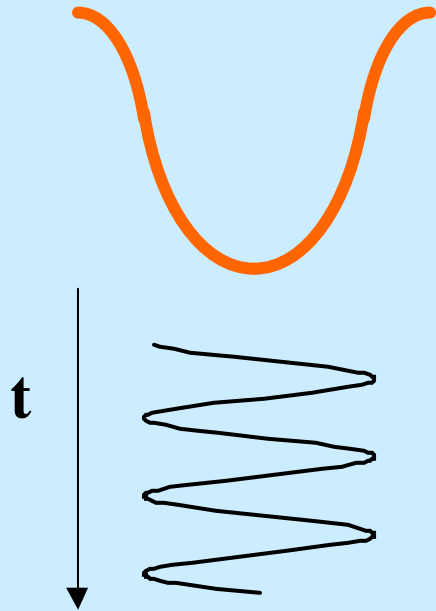
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- Modèle mécanique de l'optique non linéaire
- Equations de couplage paramétrique: aspect ondulatoire
- Equations de Manley-Rowe: aspect corpusculaire
- Amplification paramétrique
- Oscillation paramétrique optique
- Accord et quasi-accord de phase
- Comportement dynamique des OPO
- Quelques applications et développements actuels

Optique non linéaire quadratique

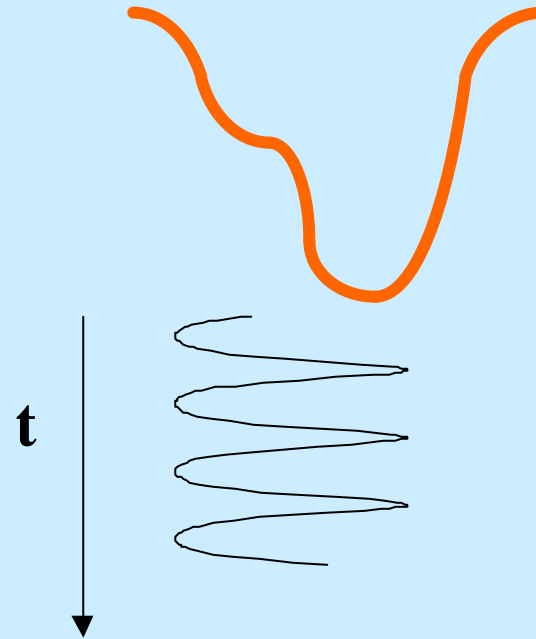
SYSTEME SYMETRIQUE



$$P(t) = \epsilon_0 c^{(1)} E(t)$$

\downarrow
 w

SYSTEME NON SYMETRIQUE



Susceptibilité optique non linéaire

$$+ \epsilon_0 c^{(2)} E(t)^2$$

\downarrow
 $2w$

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1. Modèle mécanique de l'optique non linéaire quadratique

Potentiel anharmonique $U(x) = \frac{1}{2} m \omega_0^2 x^2 + \frac{1}{3} m D x^3$

Force d'excitation périodique: $F(t) = q E \cos(\omega t) = \frac{q E}{2} (e^{i\omega t} + cc)$

Equation différentielle

$$\ddot{x} + g \dot{x} + \omega_0^2 x + D x^2 = \frac{q E}{2m} (e^{i\omega t} + cc)$$

Analyse harmonique de x(t)

$$x(t) = x_0 + x_1 e^{i\omega t} + x_2 e^{i2\omega t} + \dots + cc$$

Rectification optique

Réponse linéaire:
Indice
absorption

**Génération de
Seconde harmonique**

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1. Modèle mécanique de l'optique non linéaire quadratique

Réponse linéaire:

$$x_1 = \frac{qE}{m} \frac{1}{(\omega_0^2 - \omega^2) + i\omega g} \approx \frac{qE}{2\omega m} \frac{1}{(\omega_0 - \omega) + i g/2}$$

Polarisation du milieu:

$$P_1(t) = N q x_1(t) = \frac{N q x_1}{2} \left(e^{i\omega t} + cc \right)$$

$$P_1(t) = \frac{\epsilon_0}{2} \left(c_1^{(\omega)} E e^{i\omega t} + cc \right)$$

Par définition

Modèle de Lorentz:

$$c_1^{(\omega)} = \frac{N q^2}{2\omega m \epsilon_0} \frac{1}{(\omega_0 - \omega) + i g/2}$$

1. Modèle mécanique de l'optique non linéaire quadratique

Identification terme à terme des termes en 2ω

$$P_2(t) = N q x_2(t) = \frac{N q x_2}{2} \left(e^{i 2\omega t} + cc \right)$$

**Polarisation non linéaire
du milieu:**

$$P_2(t) = \frac{\epsilon_0}{2} \left(c_2^{(2\omega)} E^2 e^{i 2\omega t} + cc \right) \quad \text{Par définition}$$

Réponse non linéaire:

$$x_2 \approx \frac{q^2 D}{2 m^2} \frac{1}{[(\omega_0 - \omega) + i g/2]^2 [(\omega_0 - 2\omega) + i 2/3 g]}$$

Susceptibilité quadratique optique:

$$c_2^{(2\omega)} = \frac{N q^3 D}{24 \omega^3 m^2 \epsilon_0} \frac{1}{[(\omega_0 - \omega) + i g/2]^2 [(\omega_0 - 2\omega) + i 2/3 g]}$$

Double résonance à ω_0 et $\omega_0/2$

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1. Modèle mécanique de l'optique non linéaire quadratique

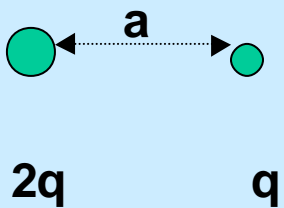
Règle de Miller:

Loin des résonnances

$$\frac{c_2^{(2w)}}{e_0^2 \left(c_I^{(w)} \right)^2 \left(c_I^{(2w)} \right)} = \frac{m D}{2 N^2 q^3} = d^{(2w)}$$

mat	n_1	n_2	$c^{\text{pm/V}}$	d
GaSb	3.8	3.82	628	$3.2 \cdot 10^9$
GaAs	3.27	3.30	368	$5.4 \cdot 10^9$
ZnSe	2.42	2.43	78	$8 \cdot 10^9$

Origine microscopique de la règle de Miller:



$$V(x) = \frac{-q^2}{4\pi\epsilon_0} \left(\frac{1}{x} + \frac{2}{a-x} \right) \approx \frac{-q^2}{4\pi\epsilon_0} \left(5.83 + 24 \left(\frac{x}{a} \right)^2 - 17 \left(\frac{x}{a} \right)^3 \right)$$

$$D = -51 \frac{q^2}{4\pi\epsilon_0 m a^4}$$

Pour $a = 0,5 \text{ nm}$ alors $D = 2 \cdot 10^{41} \text{ SI}$ soit $d = 6 \cdot 10^{19} \text{ SI}$ pour $N = 6 \cdot 10^{28} \text{ m}^{-3}$

1. Modèle mécanique de l'optique non linéaire quadratique

Aspect tensoriel

$$\begin{bmatrix} P_x \\ P_y \\ P_z \end{bmatrix} = \epsilon_0 \begin{bmatrix} d_{11} & d_{12} & d_{13} & d_{14} & d_{15} & d_{16} \\ d_{21} & d_{22} & d_{23} & d_{24} & d_{25} & d_{26} \\ d_{31} & d_{32} & d_{33} & d_{34} & d_{35} & d_{36} \end{bmatrix} \begin{bmatrix} E_x^2 \\ E_y^2 \\ E_z^2 \\ E_z E_y \\ E_z E_x \\ E_x E_y \end{bmatrix}$$

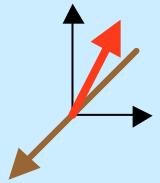
GaAs:

$$\begin{bmatrix} 0 & 0 & 0 & d_{14} & 0 & 0 \\ 0 & 0 & 0 & 0 & d_{14} & 0 \\ 0 & 0 & 0 & 0 & 0 & d_{14} \end{bmatrix}$$

$$P_x = d_{14} E_{zy}$$

Pas de non linéarité le long des axes cristallographiques

Non linéarité le long de (110)

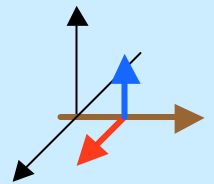


NbLiO₃:

$$\begin{bmatrix} d_{11} & -d_{11} & d_{13} & 0 & d_{15} & 0 \\ 0 & 0 & 0 & d_{15} & 0 & -d_{11} \\ d_{31} & d_{31} & 0 & 0 & 0 & 0 \end{bmatrix}$$

$$P_z = d_{31} E_x^2$$

Non linéarité le long de (010)



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2. Équation de propagation de l'interaction non linéaire

$$\nabla \cdot E = 0$$

$$\nabla \cdot B = 0$$

$$\nabla \times E = -\frac{\partial}{\partial t} B$$

$$\nabla \times B = \underbrace{\mathbf{m}_0 \frac{\partial}{\partial t} (\mathbf{e}_0 E + P)}_D = \frac{1}{c^2} \frac{\partial}{\partial t} E + \underbrace{\mathbf{m}_0 \frac{\partial}{\partial t} P}_{\text{Courant de déplacement}}$$

Maxwell

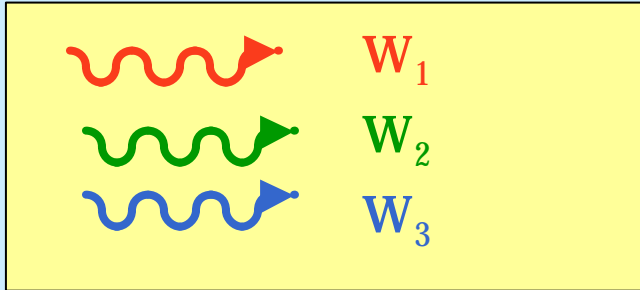
Polarisation linéaire et non linéaire: $P(t) = P_l(t) + P_{nl}(t) = \mathbf{e}_0 \mathbf{c}_1 E(t) + P_{nl}(t)$

Indice optique: $n_{op}^2 = 1 + \mathbf{c}_1$

$$\nabla^2 E - \left(\frac{n_{op}}{c}\right)^2 \frac{\partial^2}{\partial t^2} E = \mathbf{m}_0 \frac{\partial^2}{\partial t^2} P_{nl}(t)$$

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Équation de propagation de l'interaction non linéaire



Mélange à 3 ondes

$$\underbrace{\cos(\omega_1 t)\cos(\omega_2 t)}_{P_2(t)} \rightarrow \underbrace{\cos[(\omega_1 + \omega_2)t]}_{\text{Somme De Fréquences}} \text{ et } \underbrace{\cos[(\omega_1 - \omega_2)t]}_{\text{Différence De Fréquence}}$$

Terme de somme de fréquences:

$$P_{nl}(z,t) = \frac{\epsilon_0 c^2}{2} \left(\underbrace{E_2(z,t)^*}_{\omega_1} \underbrace{E_3(z,t)}_{-\omega_2 + \omega_3} + cc \right)$$

Transfert d'énergie entre les ondes

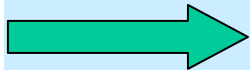
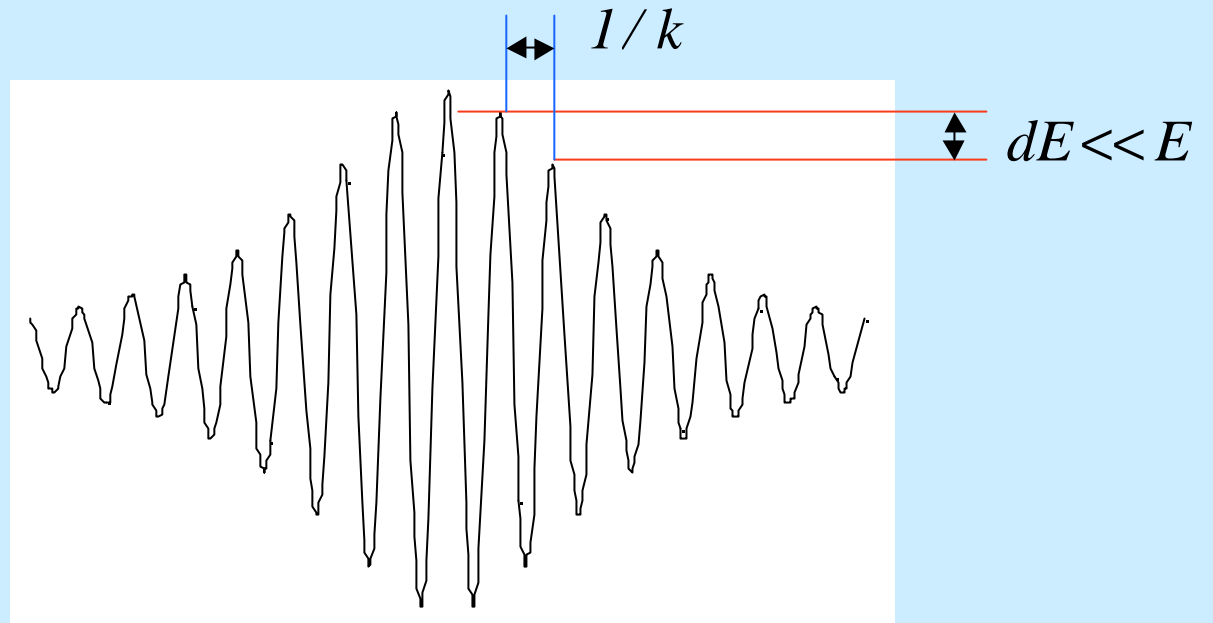
$$E_j(z,t) = \frac{1}{2} \left(\underbrace{E_j(z)}_{\text{Interaction}} \underbrace{e^{i(\omega_j t - k_j z)}}_{\text{Ondes planes (sans interaction)}} + cc \right)$$

Interaction Évolue lentement Ondes planes (sans interaction) ONERA

Équation de propagation de l'interaction non linéaire

Approximation
de la Fonctions- enveloppe

$$\left| \frac{d^2 E_j}{dz^2} \right| \ll \left| k_j \frac{d E_j}{dz} \right|$$



$w_3 - w_2 \rightarrow w_1$	$\frac{d}{dz} E_1 = -i \frac{w_1}{2n_1 c} c_2 E_3 E_2^* e^{-i Dk z}$
$w_3 - w_1 \rightarrow w_2$	$\frac{d}{dz} E_2 = -i \frac{w_2}{2n_2 c} c_2 E_3 E_1^* e^{-i Dk z}$
$w_1 + w_2 \rightarrow w_3$	$\frac{d}{dz} E_3 = -i \frac{w_3}{2n_3 c} c_2 E_1 E_2 e^{+i Dk z}$

Désaccord de phase $Dk = k_3 - k_1 - k_2$

Équation de propagation de l'interaction non linéaire: doublage de fréquence

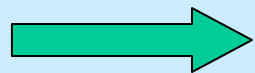
Doublage de fréquence $\omega_1 = \omega_2 = \omega$ et $\omega_3 = 2\omega$

$$2\omega - \omega \rightarrow \omega \quad \frac{d}{dz} E_{\omega} = -i \frac{\omega}{2n_{\omega} c} \mathbf{c}_2 E_{2\omega} E_{\omega}^* e^{-i \mathbf{Dk} z} \quad \text{reconversion}$$

$$\omega + \omega \rightarrow 2\omega \quad \frac{d}{dz} E_{2\omega} = -i \frac{\omega}{n_{2\omega} c} \mathbf{c}_2 E_{\omega}^2 e^{+i \mathbf{Dk} z}$$

Pompe non déplétée: $E_{\omega}(z) \approx E_0$

$$E_{2\omega}(z) = \frac{\omega}{n_{2\omega} c} \mathbf{c}_2 E_0^2 L \operatorname{sinc} \left(\frac{\mathbf{Dk} l}{2} \right)$$

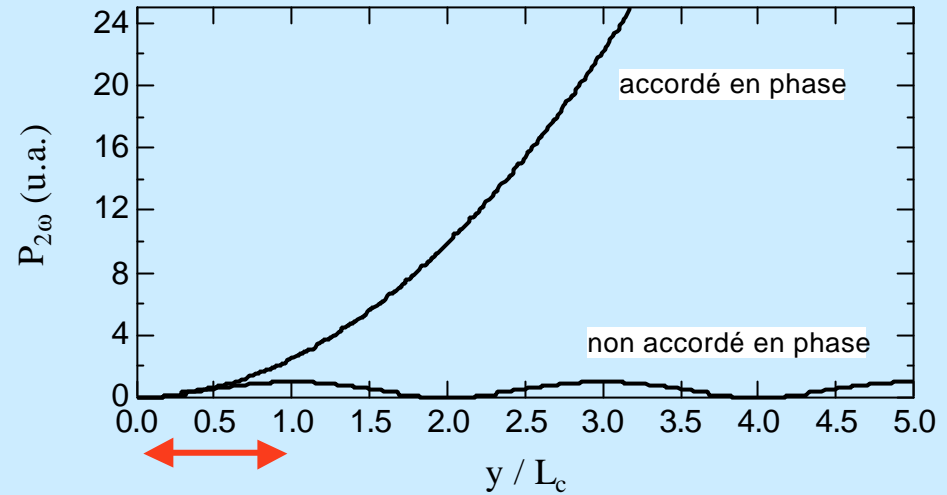


Rendement de conversion

$$P_{2\omega}(z) = 2 \frac{Z_0^3}{n_{2\omega} c} (\omega e_0 \mathbf{c}_2 L)^2 \operatorname{sinc}^2 \left(\frac{\mathbf{Dk} l}{2} \right) P_{\omega}^2$$

Équation de propagation de l'interaction non linéaire: désaccord de phase dans le doublage de fréquence

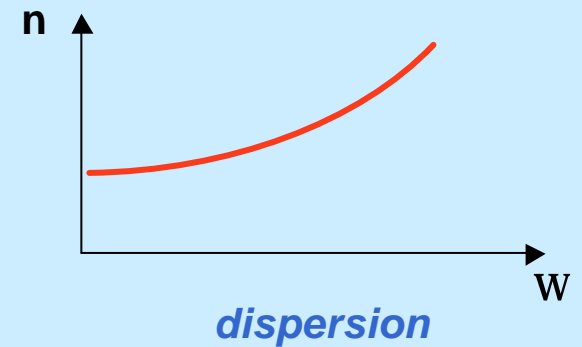
$$P_{2\omega}(z) \propto L^2 \operatorname{sinc}^2\left(\frac{Dkl}{2}\right) P_{\omega}^2$$



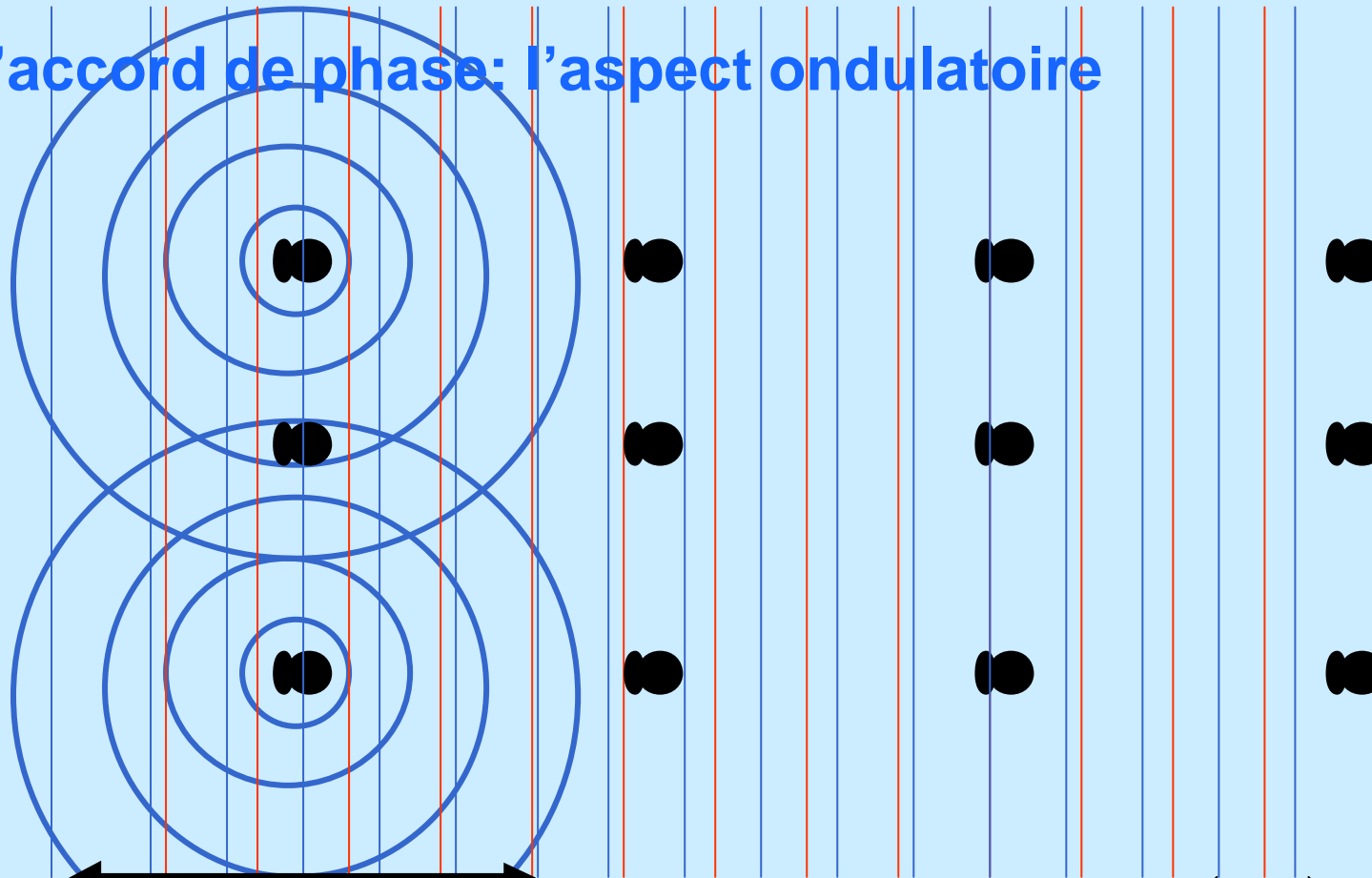
Longueur de cohérence:

$$L_c = \frac{I_0}{4(n_{2\omega} - n_{\omega})}$$

Exemple: dans GaAs
 Fondamental 10,6 μm \otimes GSH 5,3 μm
 $c = 100 \text{ pm/V}$
 $n_2 - n_1 = 2,5 \cdot 10^{-2}$
 $L_c = 106 \mu\text{m}$
 $P_2 = 10^{-11} P_1^2 \text{ (W/cm}^2\text{)}$



L'accord de phase: l'aspect ondulatoire



$$2L_c = \frac{l_0}{2 [n(2w) - n(w)]}$$

$$c(w) = \frac{c}{n(w)} \rightarrow l(w) = \frac{l_0}{n(w)}$$

$$c(2w) = \frac{c}{n(2w)} \rightarrow l(2w) = \frac{l_0}{n(2w)}$$

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3. Equations de Manley-Rowe: aspect corpusculaire

abracadabra....: $A_j = \sqrt{\frac{n_j}{w_j}} E_j \longrightarrow$

Amplitude de flux de photons:

$$F_j = \frac{P_j}{\hbar w_j} = \frac{1}{2\hbar Z_0} |A_j|^2$$

$$\begin{array}{ll} w_3 - w_2 \rightarrow w_1 & \frac{d}{dz} A_1 = -i\mathbf{k} A_3 A_2^* e^{-i\mathbf{Dk}z} \\ w_3 - w_1 \rightarrow w_2 & \frac{d}{dz} A_2 = -i\mathbf{k} A_3 A_1^* e^{-i\mathbf{Dk}z} \\ w_1 + w_2 \rightarrow w_3 & \frac{d}{dz} A_3 = -i\mathbf{k} A_1 A_2 e^{+i\mathbf{Dk}z} \end{array}$$

avec: $\mathbf{k} = \frac{1}{2} \frac{c^2}{c} \sqrt{\frac{w_1 w_2 w_3}{n_1 n_2 n_3}}$

Équations de Manley-Rowe: aspect corpusculaire

Si: $Dk=0$ 

$$\frac{d}{dz}(|A_1|^2) = \frac{d}{dz}(|A_2|^2) = -\frac{d}{dz}(|A_3|^2)$$

$$\frac{d}{dz}(F_1) = \frac{d}{dz}(F_2) = -\frac{d}{dz}(F_3)$$

Manley-Rowe: conservation du flux de particules

Interprétation corpusculaire

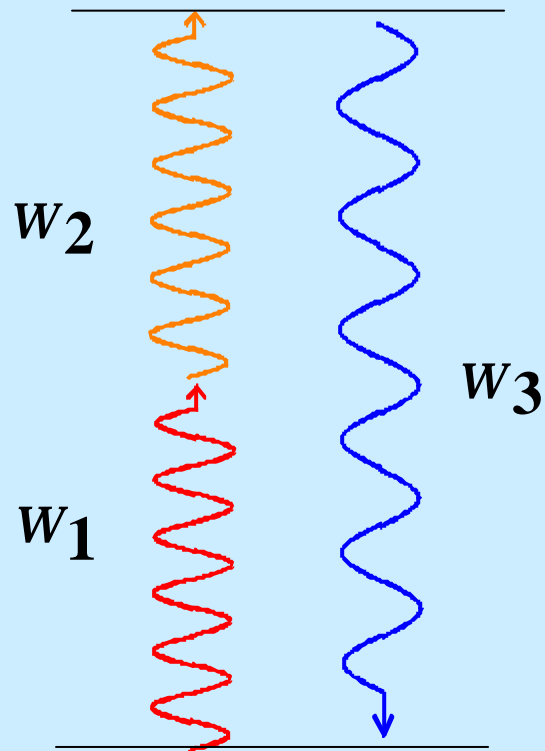
$$\hbar\omega_3 = \hbar\omega_1 + \hbar\omega_2$$

conservation de l'énergie

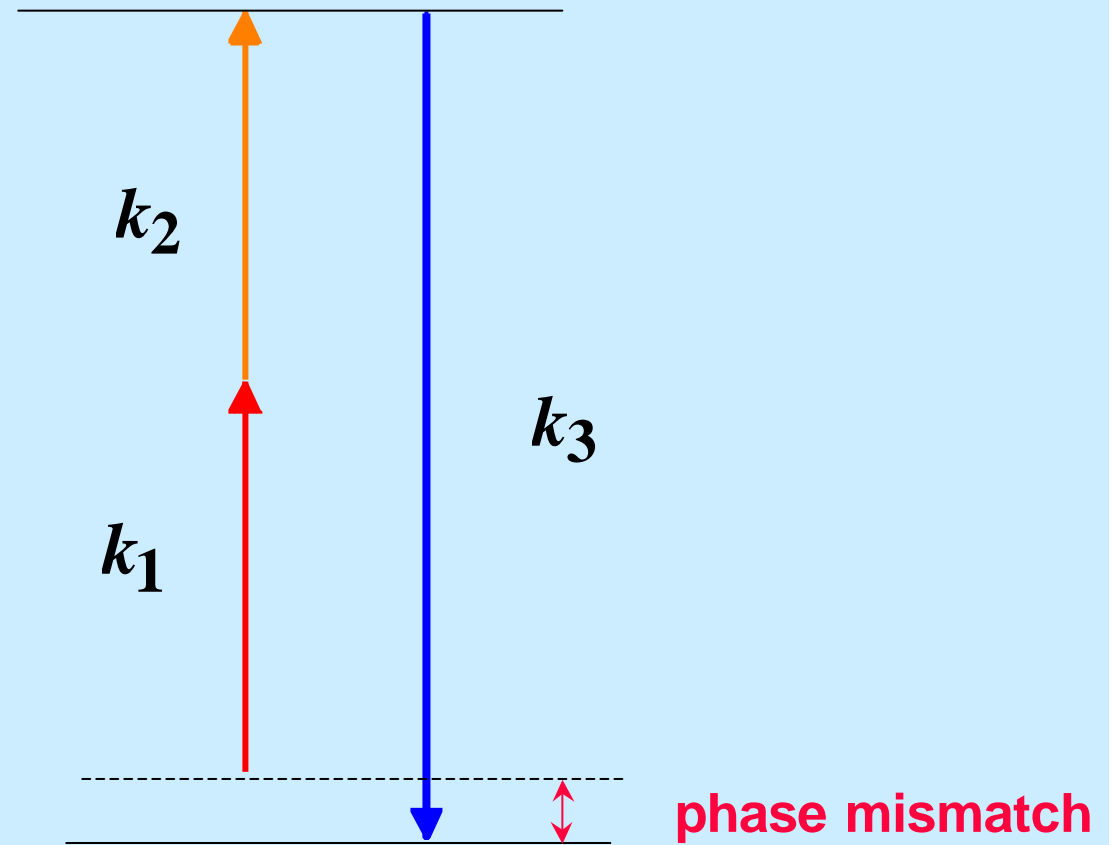
$$\hbar k_3 = \hbar k_1 + \hbar k_2$$

conservation de l'impulsion

THE PHASE MATCHING PROBLEM: THE PHOTON ASPECT



energy conservation



momentum conservation

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4. L'amplification paramétrique

Hypothèse de la pompe non appauvrie
avec accord de phase

$$\frac{d}{dz} A_1 = -i g A_2^*$$

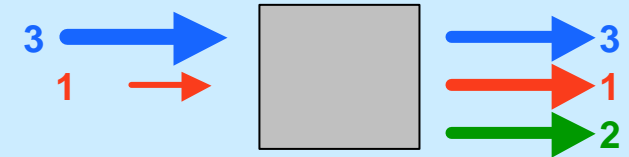
$$\frac{d}{dz} A_2 = -i g A_1^*$$

Avec le gain paramétrique

$$g = \frac{1}{2} \frac{c_2}{c} \sqrt{\frac{w_1 w_2}{n_1 n_2}} E_3(0)$$

$$A_1(z) = A_1(0) \cosh(gz) - i A_2(0)^* \sinh(gz)$$

$$A_2(z) = A_2(0) \cosh(gz) - i A_1(0)^* \sinh(gz)$$



Pour des gains paramétriques forts

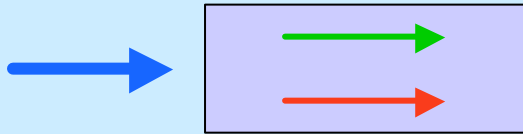
$$A_1(z) \approx A_2(z) \approx \frac{1}{2} A_1(0) e^{g z}$$

Exemple: dans GaAs pour 5 MW/cm²
Fondamental 5,3 μm ® 10,6 μm
c = 100 pm/V
G = 0,35 cm⁻¹

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4. L'amplification paramétrique

Génération et fluorescence paramétrique optique



$$|n_1, n_2, n_3\rangle \Rightarrow |n_1 + 1, n_2 + 1, n_3 - 1\rangle$$

Hypothèse de la pompe non appauvrie
sans accord de phase

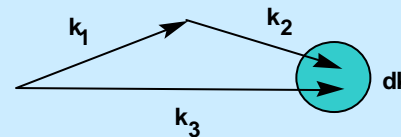
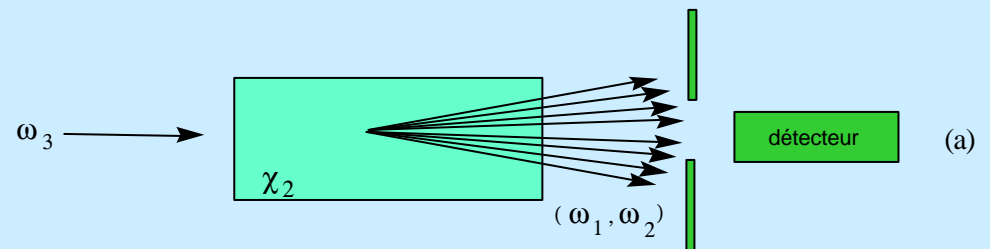
$$\frac{d}{dz} A_1 = -i g A_2^* e^{-i Dk z}$$

$$\frac{d}{dz} A_2 = -i g A_1^* e^{-i Dk z}$$

Avec le gain paramétrique

$$g = \sqrt{g^2 - (Dk)^2}$$

$$A_2(z)^* = i \frac{g}{g} A_1(0) \text{Sinh}(g z) e^{i Dk z}$$



$A_1(0)$ correspond à un seul photon par mode

Génération et fluorescence paramétrique optique

Calcul effroyable:

Nombre de modes w_1 entrant acceptable pour w_3

on met un photon w_1 par mode et on utilise le résultat de la planche précédente

On somme sur toutes les paires acceptables tombant dans l'angle de vue q du détecteur

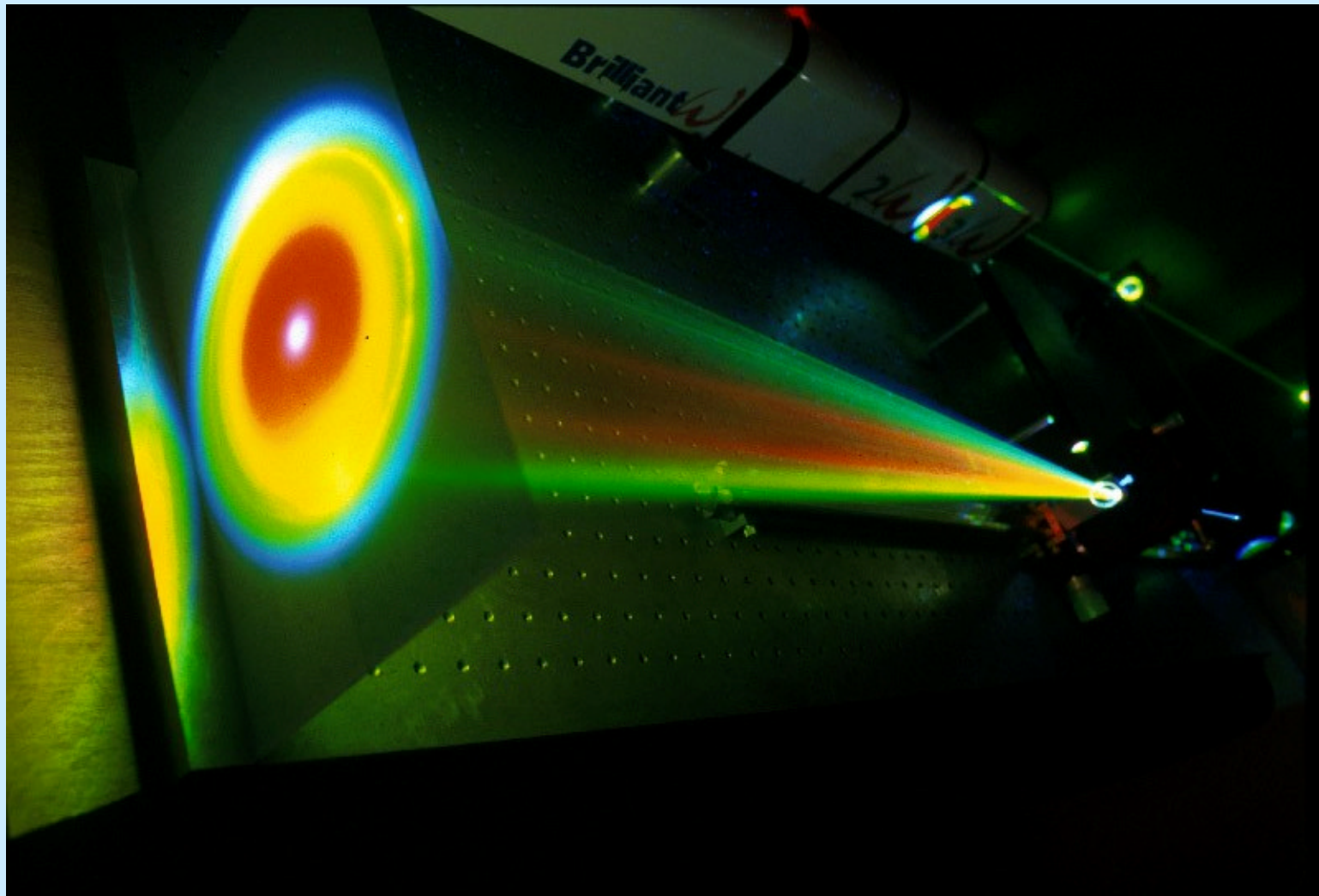
$$P_2 = p \frac{b L P_3}{|b|} q^2$$

$$b = \frac{\hbar w_1 w_2^4 n_2 c_2^2}{p^2 c^5 n_1 n_3 \epsilon_0^3}$$

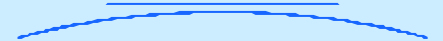
$$b = \frac{\partial k_2}{\partial w_2} \Big|_{w_{20}} - \frac{\partial k_1}{\partial w_1} \Big|_{w_{10}}$$

Utilisation:

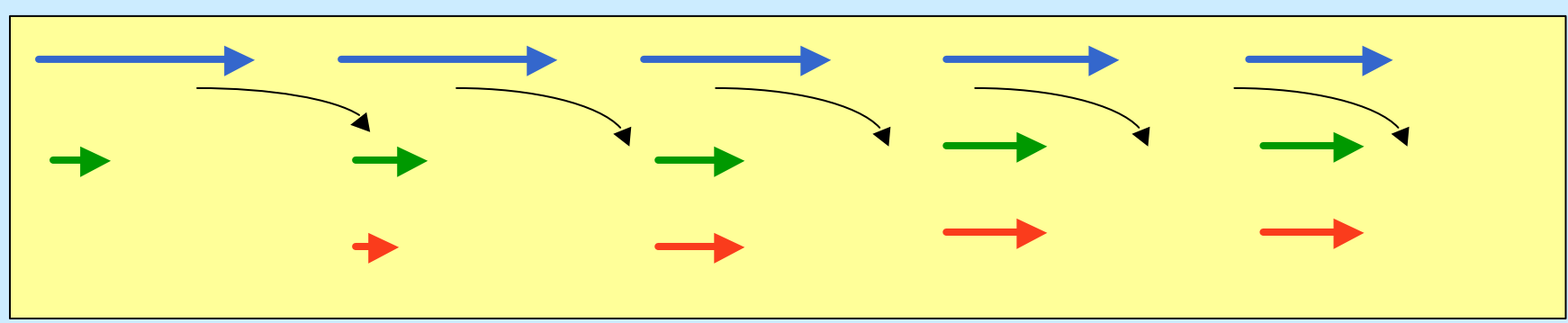
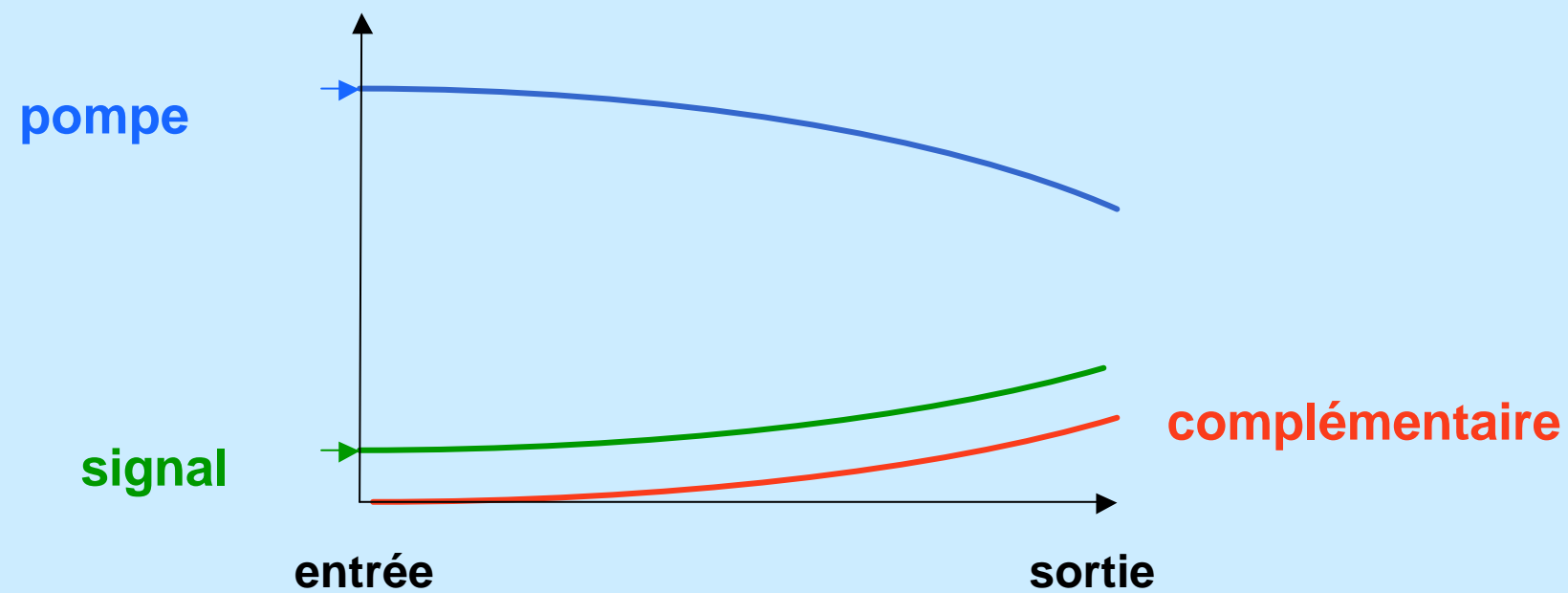
- précurseur de l'oscillation paramétrique
- courbe d'accord de phase expérimentaux



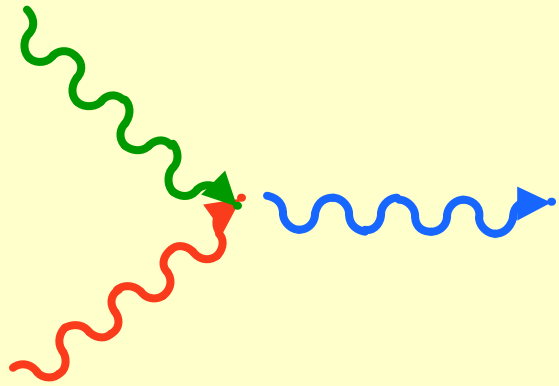
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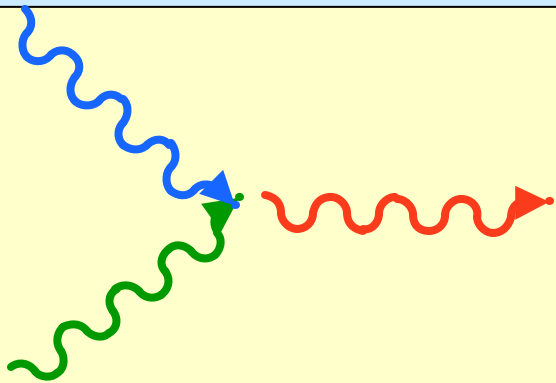
AMPLIFICATION ET FLUORESCENCE PARAMETRIQUE



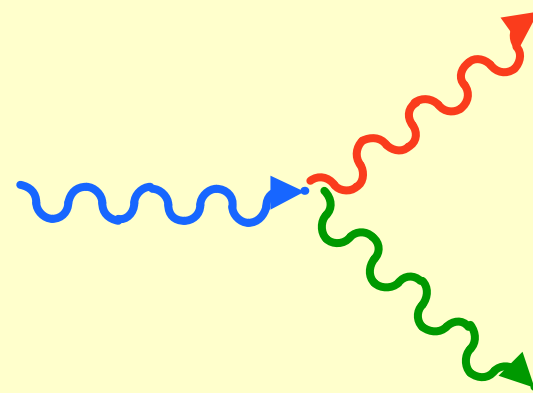
Sum and Difference Frequency Generation vs parametric interaction



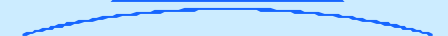
Sum Frequency Generation



Difference Frequency Generation



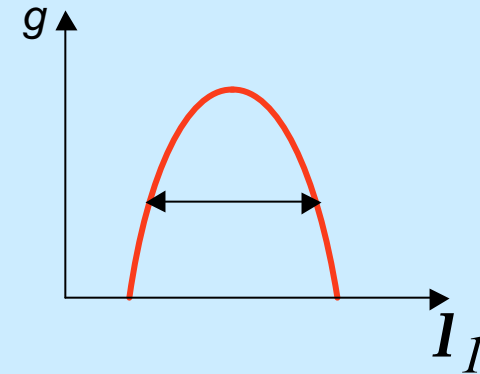
Optical Parametric Generation



L'amplification paramétrique

Largeur de gain paramétrique

$$Dk L = \pm p$$

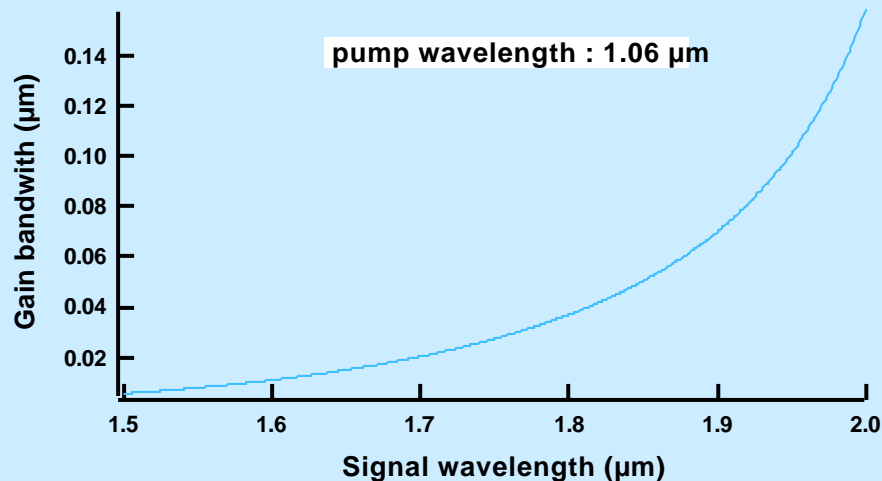


accord de phase $\frac{Dk}{2p} = \frac{n(I_3)}{I_3} - \frac{n(I_1)}{I_1} - \frac{n(I_2)}{I_2} = 0$

Conservation de l'énergie $\frac{1}{I_3} = \frac{1}{I_1} + \frac{1}{I_2}$

La pompe I_3 est fixée

$$DI_1 = \frac{I_1^2 / L}{\left(n_1 - n_2 + \frac{dn(I_2)}{dI_2} I_2 - \frac{dn(I_1)}{dI_1} I_1 \right)}$$

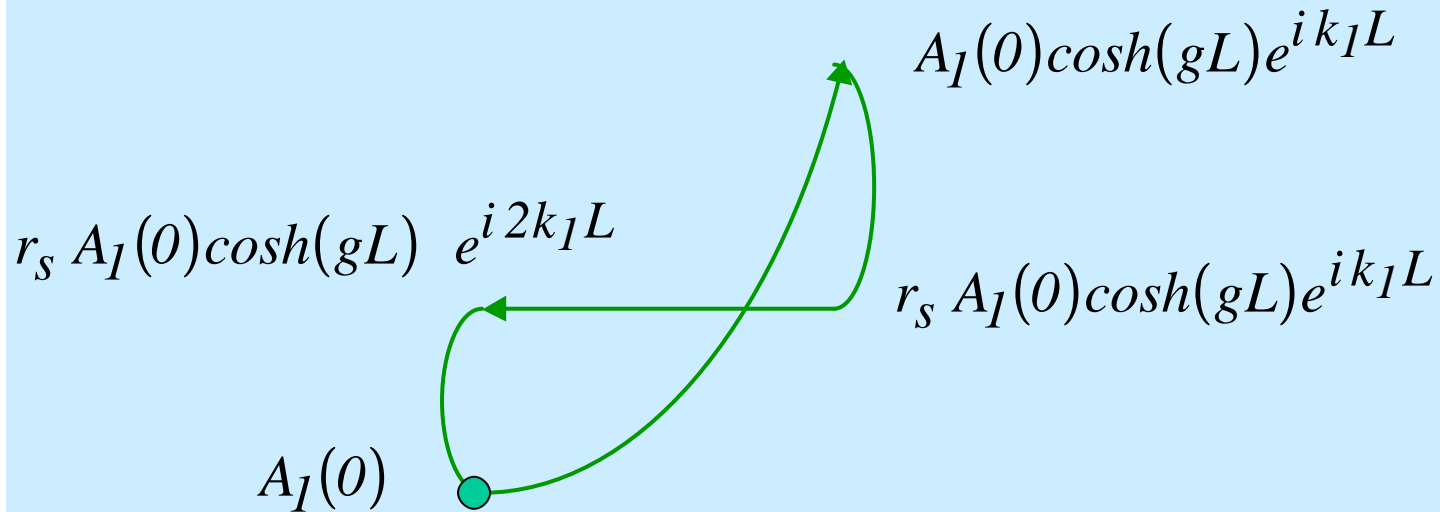


Accord de type I: polar. identique pour 1 et 2
 Accord de type II: polar. différente pour 1 et 2

Niobate de lithium
 Accord de type I



5. l'oscillateur paramétrique simplement résonant



$$A_I(0) = r_e r_s \cosh(gL) e^{i 2 k_1 L} A_I(0)$$

$$\cosh(g_{seuil} L) = \frac{1}{\sqrt{R_e R_s}}$$

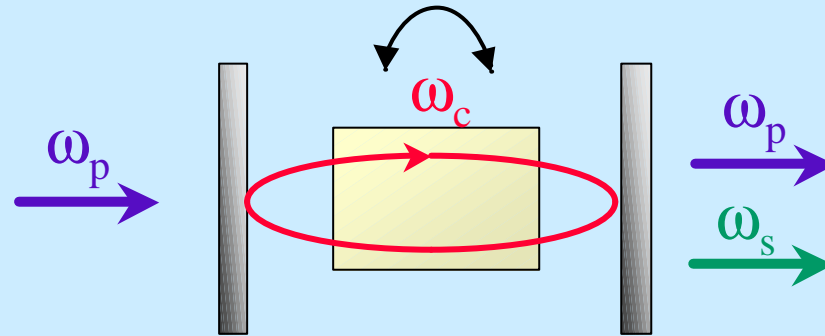
Condition sur l'amplitude de pompe

$$k_1 L = m \mathbf{p}$$

Condition de résonance

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Optical Parametric Oscillator: basic principles

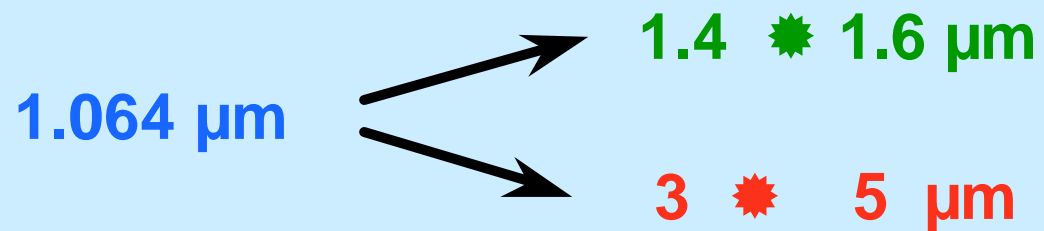


$$\omega_s + \omega_c = \omega_p$$

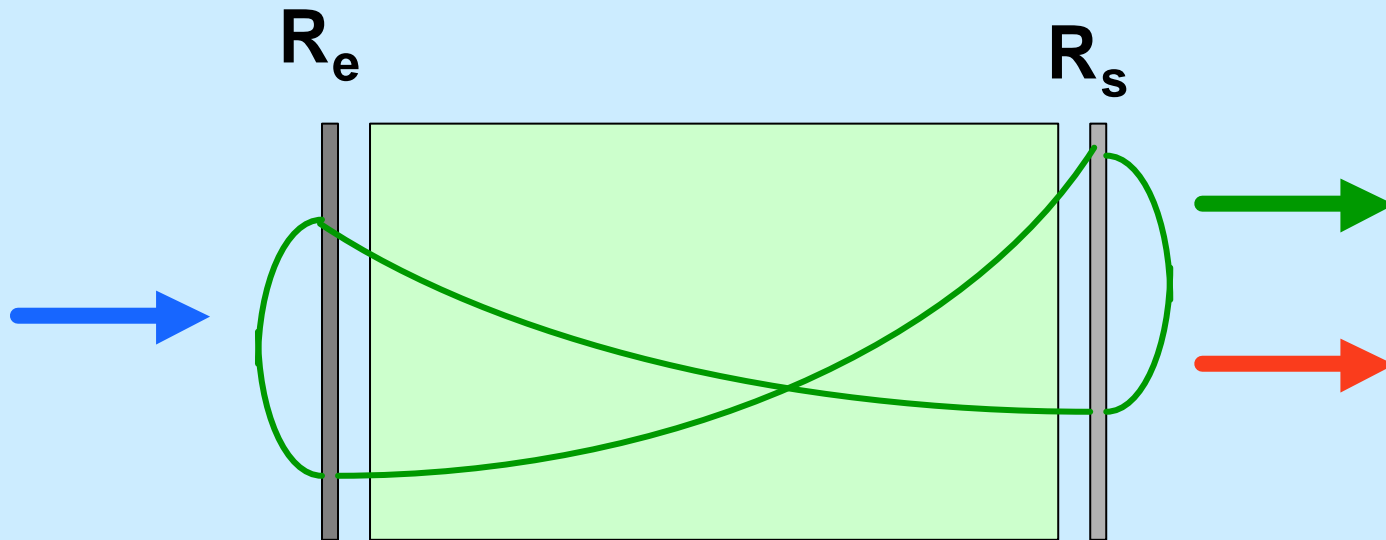
(energy conservation)

$$\mathbf{k}_s + \mathbf{k}_c = \mathbf{k}_p$$

(phase matching condition)



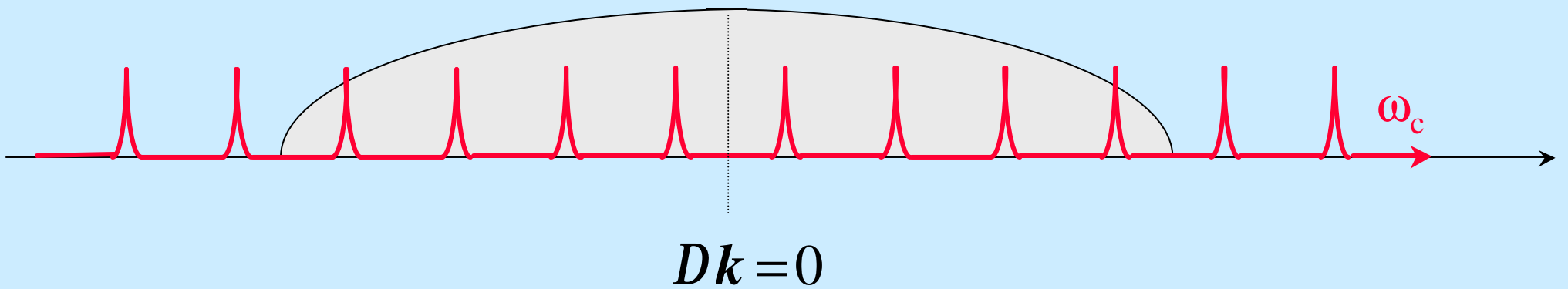
SINGLY RESONANT OPO (SROPO)



SEUIL:
gain = perte

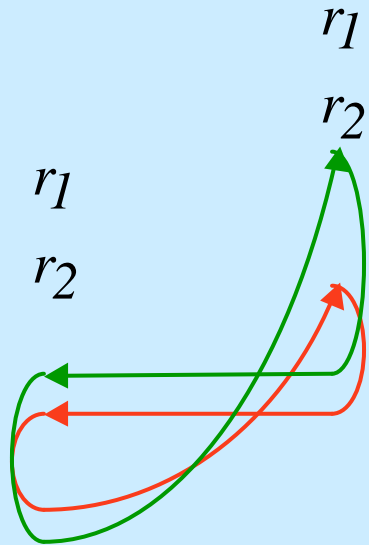
$$g(I_{pompe})L \gg \sqrt{T}$$

gain paramétrique



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5. l'oscillateur paramétrique doublement résonant



$$A_1(0) = \left[A_1(0) \text{Cosh}(g L) - i A_2(0)^* \text{Sinh}(g L) \right] r_1^2 e^{i 2 k_1 L}$$

$$A_2(0) = \left[A_2(0) \text{Cosh}(g L) - i A_1(0)^* \text{Sinh}(g L) \right] r_2^2 e^{i 2 k_2 L}$$



$$\det \begin{bmatrix} r_1^2 \cosh(gL) e^{i 2 k_1 L} - 1 & -i r_1^2 \text{sh}(gL) e^{i 2 k_1 L} \\ i r_2^2 \text{sh}(gL) e^{i 2 k_2 L} & r_2^2 \cosh(gL) e^{i 2 k_2 L} - 1 \end{bmatrix} = 0$$



$$\text{Cosh}(g_{\text{seuil}} L) = \frac{1 + R_1 R_2}{R_1 + R_2}$$

Condition sur l'amplitude de pompe

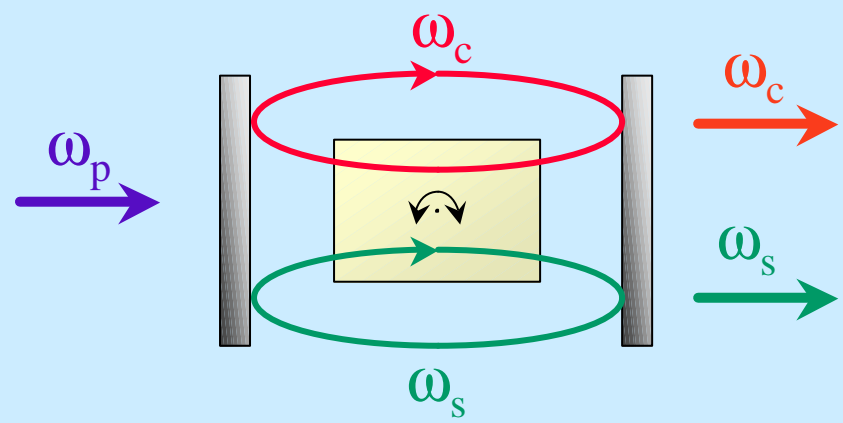
$$k_1 L = m \mathbf{p}$$

Conditions de résonance

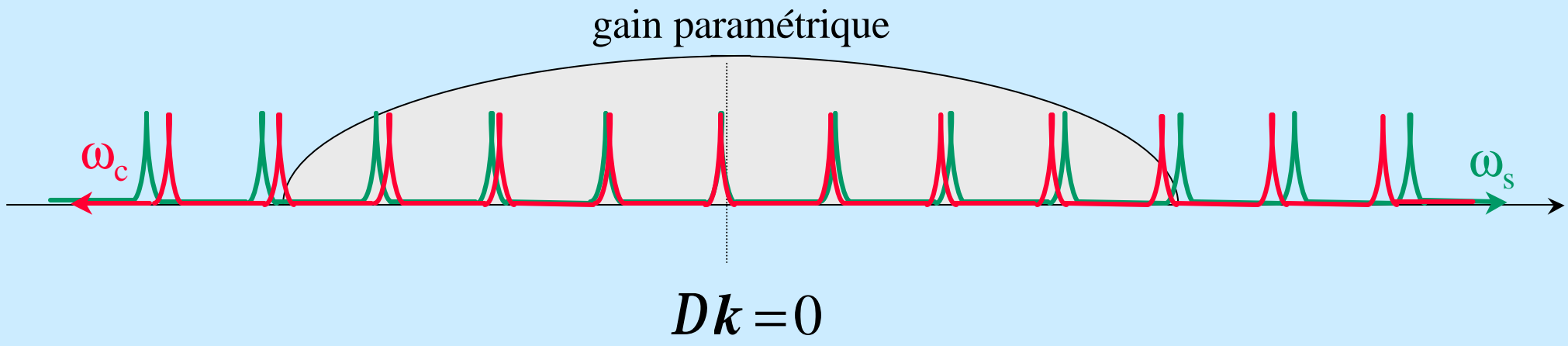
$$k_2 L = n \mathbf{p}$$

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DOUBLY RESONANT OPO (DROPO)



SEUIL:
gain = perte

$$g(I_{pompe})L \gg \sqrt{T_s T_c}$$


5. l'oscillateurs paramétriques optiques: 2 exemples

GaAs : $c = 100 \text{ pm/V}$
 $n = 3.2$
 $l = 5 \text{ }\mu\text{m}$
 $L = 5 \text{ mm}$ accordé en phase

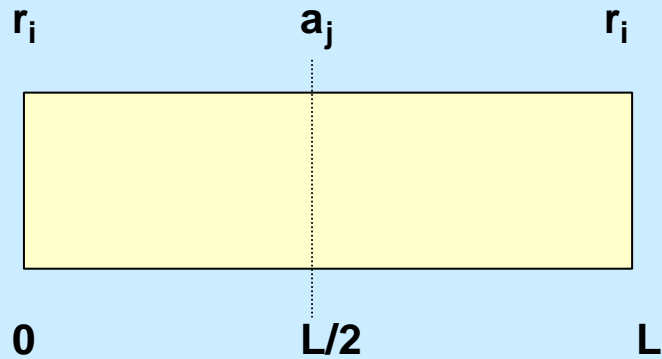
SROPO: $R_e = R_s = 99\%$

$$\text{Cosh}(g_{\text{seuil}} L) \approx \sqrt{1 - R_1} \quad \longrightarrow \quad P_{\text{seuil}} = 6 \text{ MW/cm}^2$$

DROPO: $R_e = R_s = 99\%$

$$\text{Cosh}(g_{\text{seuil}} L) \approx \sqrt{(1 - R_1)(1 - R_2)} \quad \longrightarrow \quad P_{\text{seuil}} = 0,2 \text{ MW/cm}^2$$

6. Comportement dynamique des OPO



Linéarisation des équations

$$u_i^n(L) = u_i^n(L/2) \pm \frac{\mathbf{k}L}{2} u_j^n(L/2) u_k^n(L/2)$$

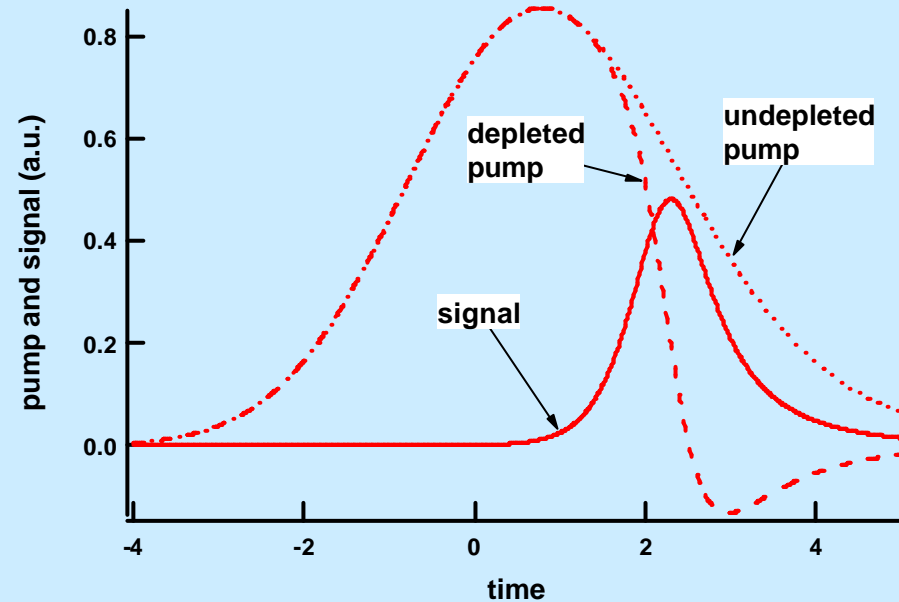
$$\frac{d}{dt} a_1(t) = -\frac{a_1}{t_1} + \mathbf{g}_1 a_2 a_3$$

$$\frac{d}{dt} a_2(t) = -\frac{a_2}{t_2} + \mathbf{g}_2 a_1 a_3$$

$$\frac{d}{dt} a_3(t) = f(t) - \frac{a_3}{t_3} - \mathbf{g}_3 a_1 a_2$$

avec

$$t_j = \frac{T_{AR}}{1-r_j} \quad \text{et} \quad \mathbf{g}_j = (1+r_j) \frac{\mathbf{k}c'}{4}$$



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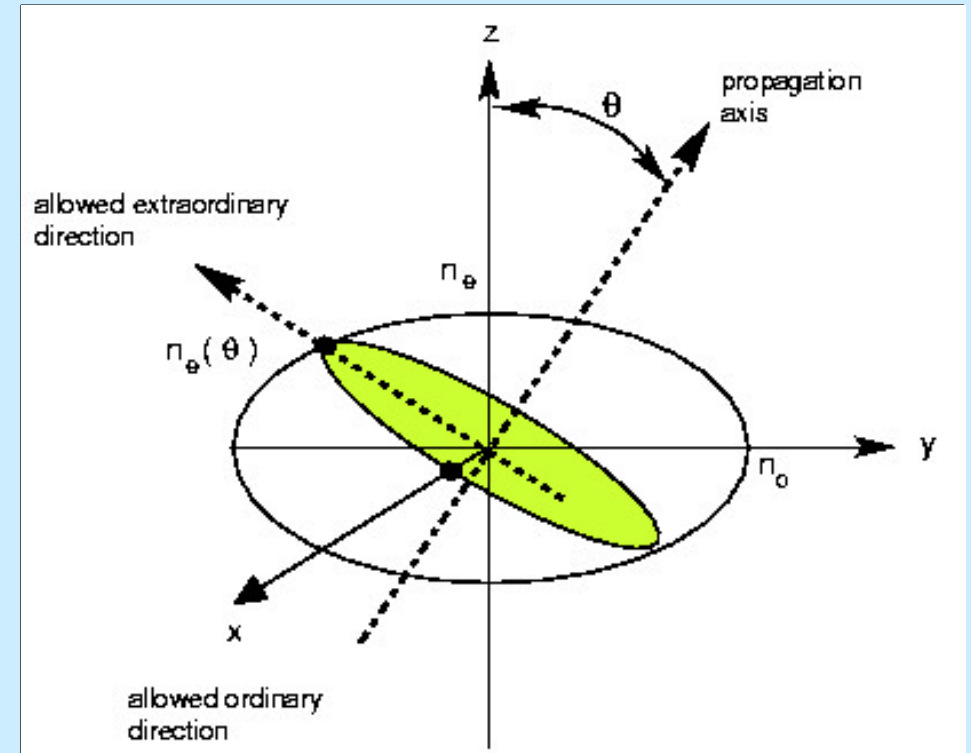
7.a Accord de phase par biréfringence

Cristal biréfringent d'axe optique Oz

n_o **Indice ordinaire (Ox, Oy)**

n_e **Indice extraordinaire (Oz)**

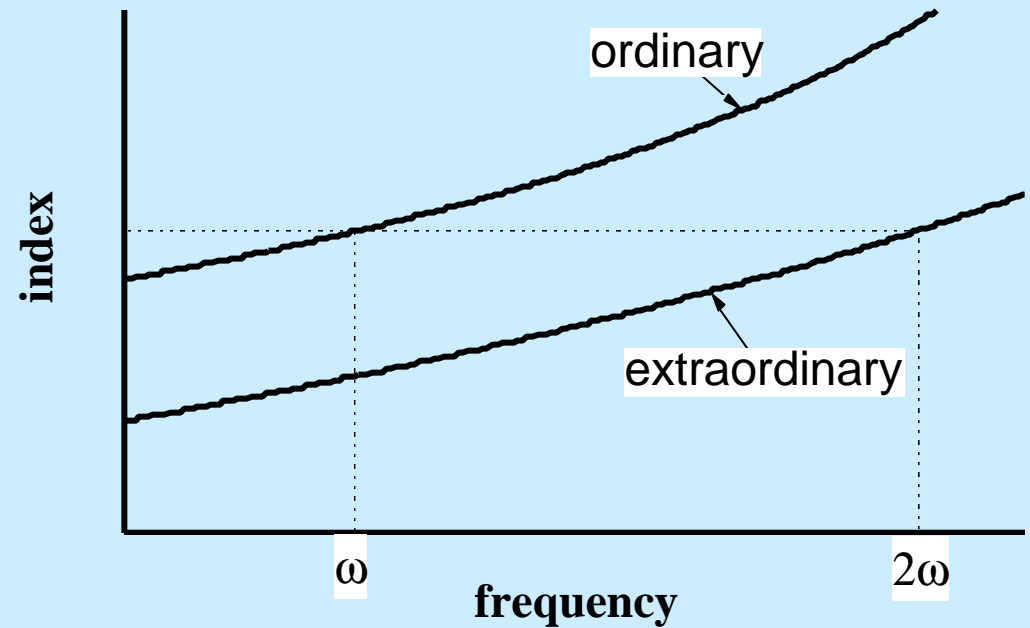
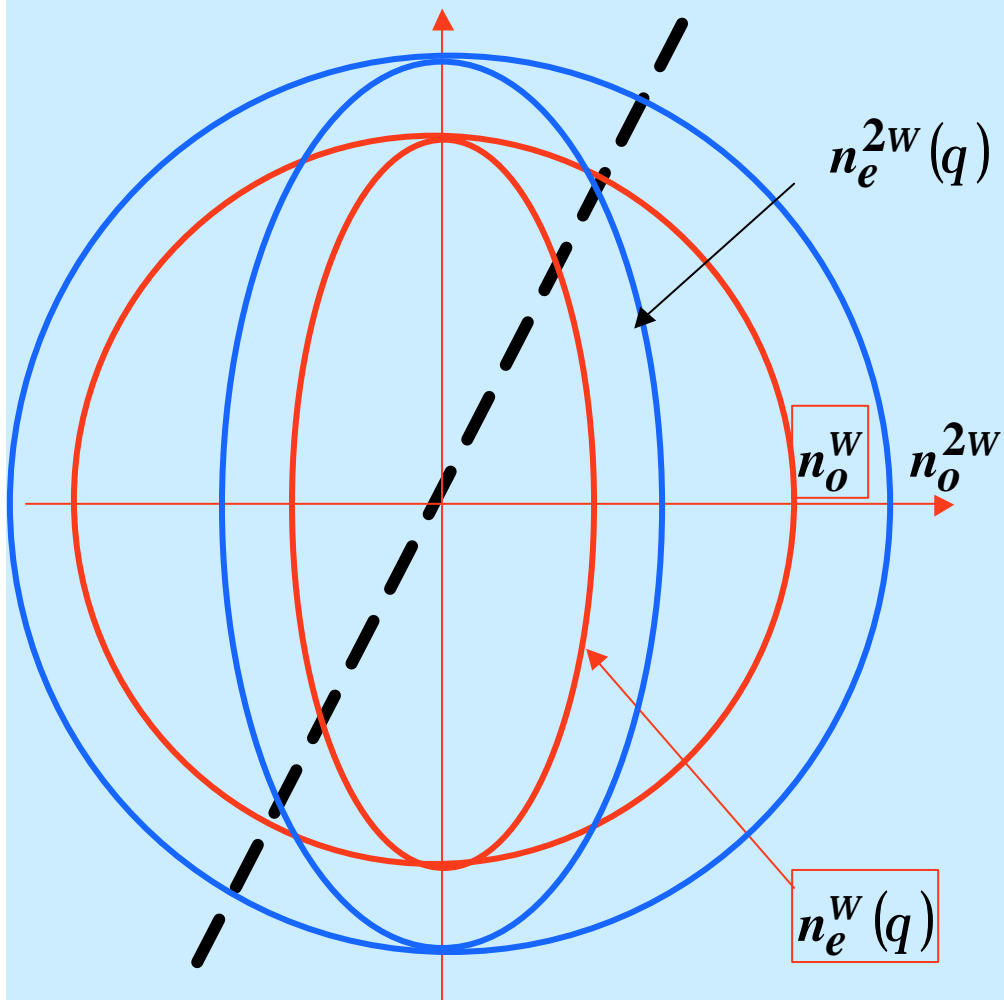
$$\frac{1}{n_e^2(\mathbf{q})} = \frac{\cos^2 \mathbf{q}}{n_o^2} + \frac{\sin^2 \mathbf{q}}{n_e^2}$$



Une onde se propage dans zOy avec un angle avec l'axe optique: deux directions de propagation de polarisation linéaire

- L'indice ordinaire (le long de Ox) est indépendant de l'angle q_s
- L'indice extraordinaire dépend de l'angle q_s

Accord de phase par biréfringence



Milieu uniaxe négatif

$$n_e^{2W}(q) = n_o^W(q) \text{ P accord de phase}$$

7.a Exemple : doublage dans le niobate de lithium

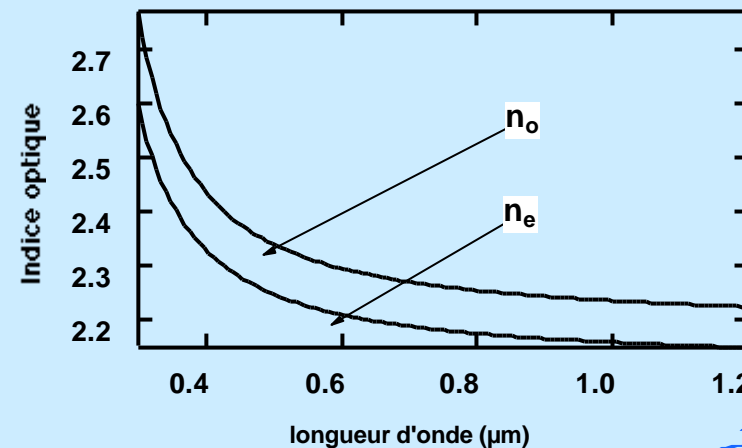
$$n_e(2\mathbf{w}, \mathbf{q}_s) = n_o(\mathbf{w}) \quad \longrightarrow \quad \frac{1}{n_o(\mathbf{w})^2} = \frac{\cos^2 \mathbf{q}_s}{n_o(2\mathbf{w})^2} + \frac{\sin^2 \mathbf{q}_s}{n_e(2\mathbf{w})^2}$$

Relation de Sellmeier

$$n^2 = A - \frac{B}{C - \lambda^2} - D\lambda^2$$

	A	B	C	D
n_e	4.5820	0.099169	0.044432	0.021950
n_o	4.9048	0.11768	0.04750	0.027169

Exemple : 1,3 μm \otimes 0,65 μm
 $q_s = 45^\circ$

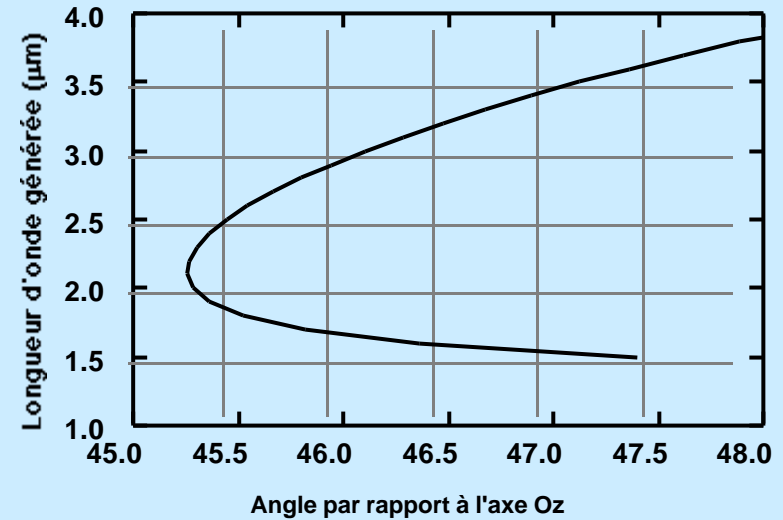


7.a Exemple : oscillation paramétrique dans le niobate de lithium

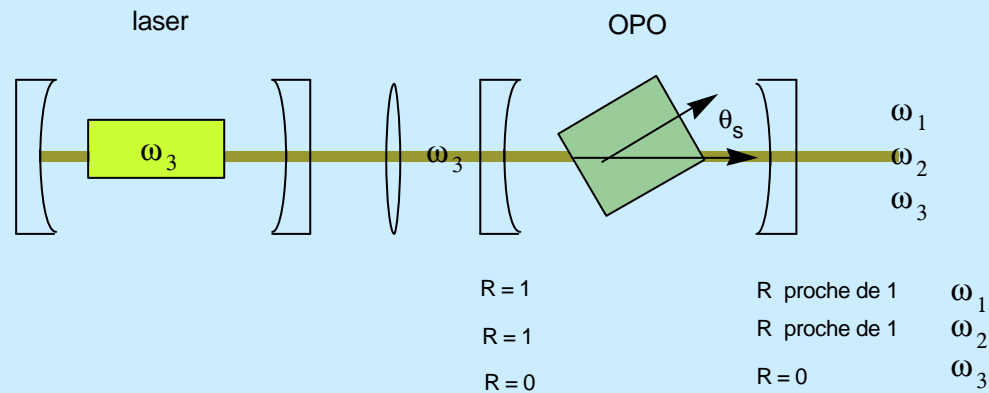
Accord de phase \otimes eeo

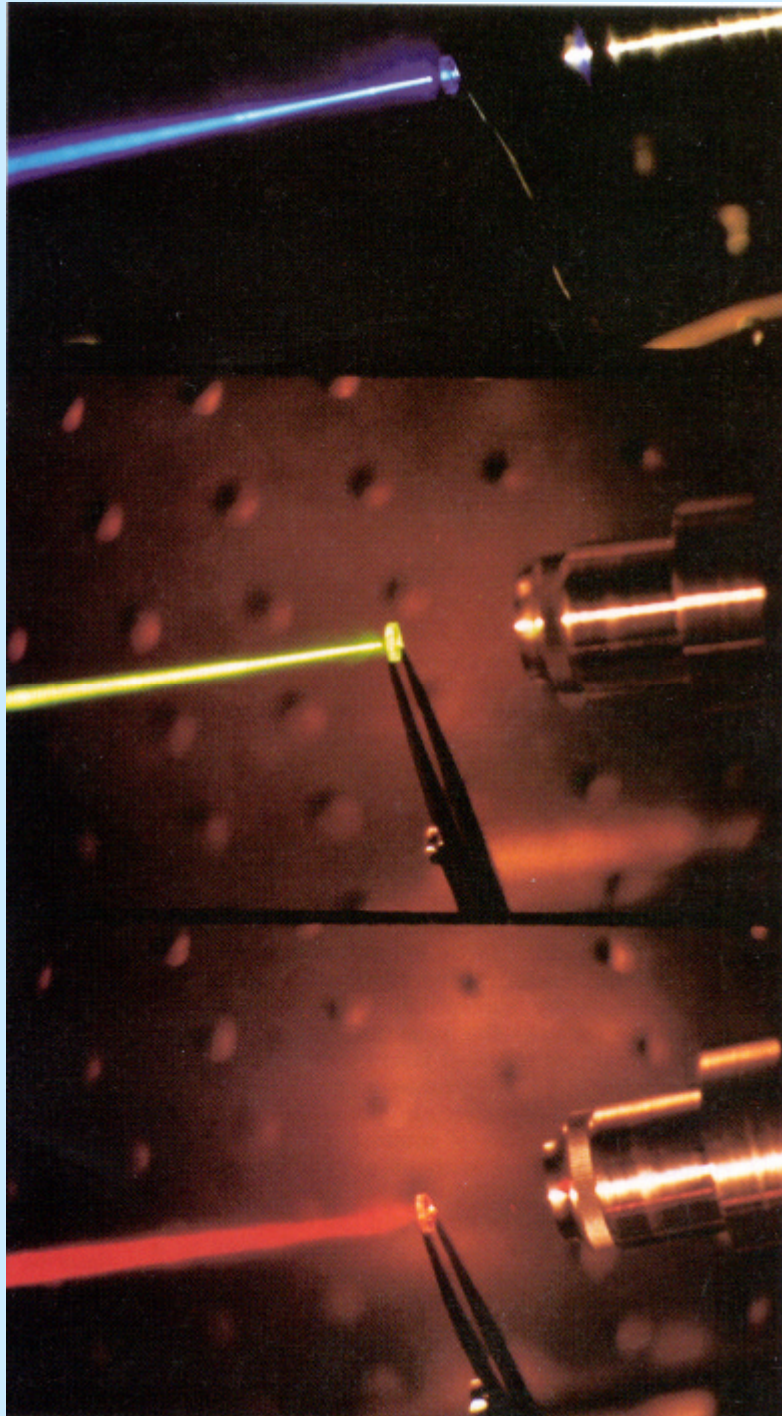
$$\omega_1 + \omega_2 = \omega_3$$

$$n_o(\omega_1)\omega_1 + n_o(\omega_2)\omega_2 = n_e(\omega_3, \mathbf{q}_s)\omega_3$$



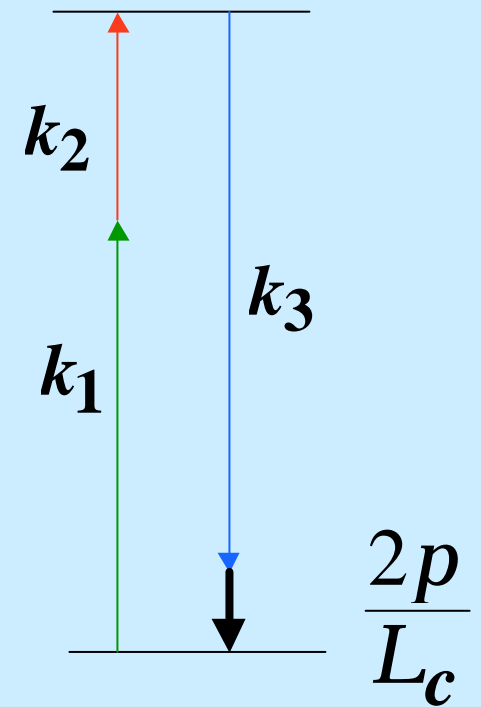
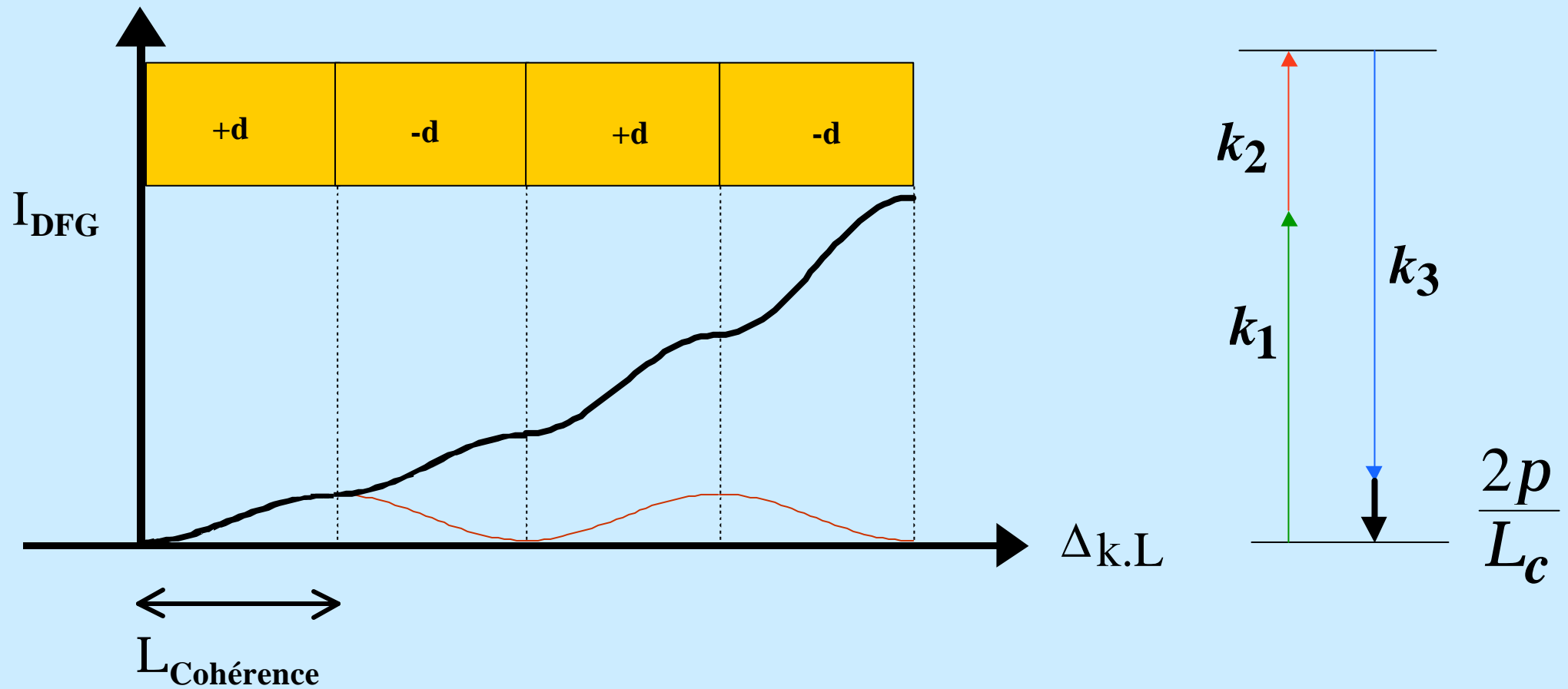
Accord de longueur d'onde par rotation





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7.b First order quasi-phase matching



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7.b le quasi accord de phase

Indice non linéaire modulé $c_2(z) = c_2 f(z)$ avec $f(z) = \sum_n f_n e^{i n (2p/L) z}$

Pompe non appauvrie $\frac{d}{dz} E_{2W} = -i \frac{W}{n_{2W} c} c_2 E_W^2 f(z) e^{+i Dk z}$

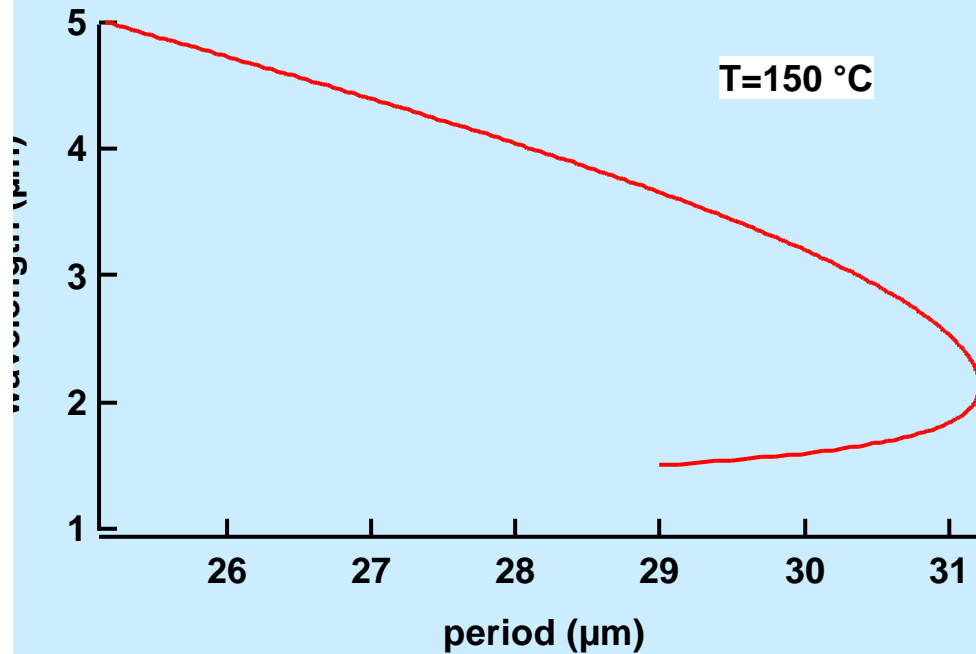
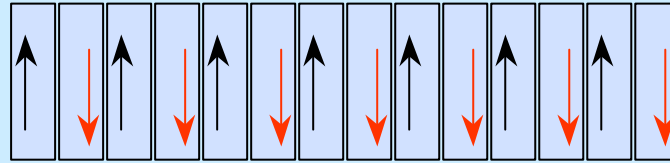
→ $E_{2W}(z) = -i \frac{W}{n_{2W} c} c_2 E_W^2 \int_0^L f(z) e^{+i Dk z} dz$

Seul terme non nul $k_{2W} - 2k_W = n \frac{2p}{L}$ soit $L = (2n+1)L_c$

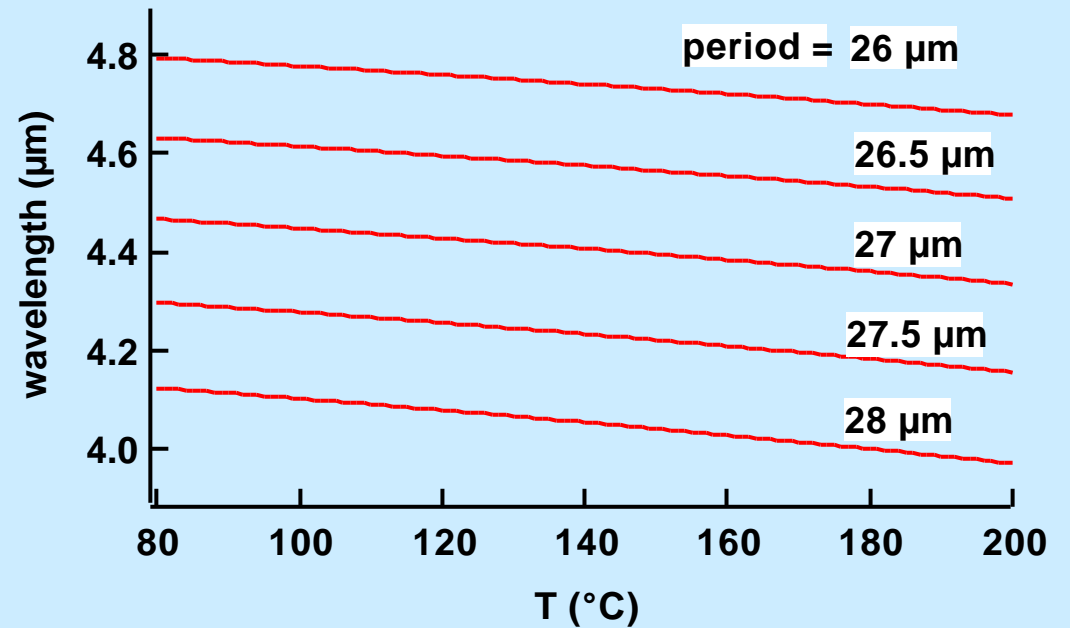
Susceptibilité effective $c_2^{eff} = c_2 |f_n| = \frac{2}{p} c_2$



Periodically Poled Lithium Niobate



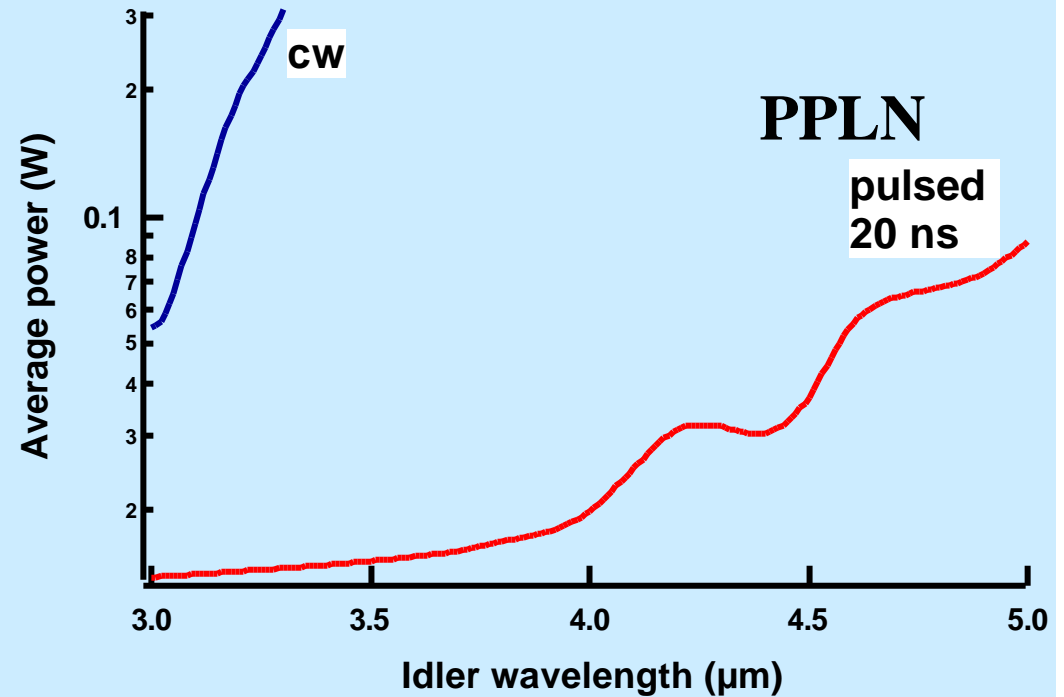
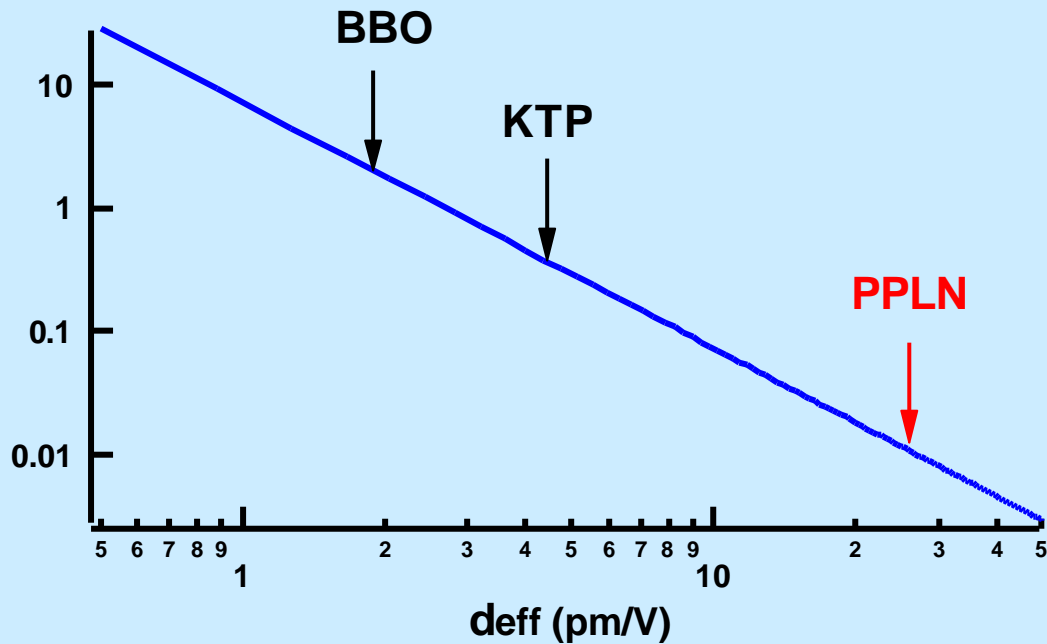
wavelength vs period



wavelength vs T

$d_{\text{eff}} = 27\text{ pm/V} \text{ !!!!!}$

Optical Parametric Oscillator Threshold: PPLN breakthrough

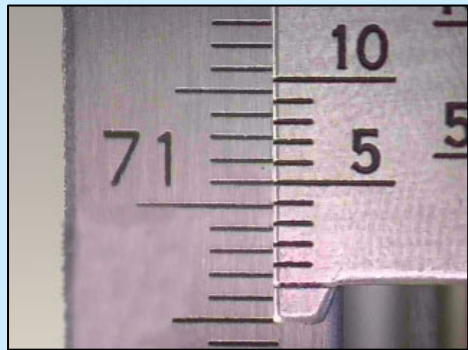
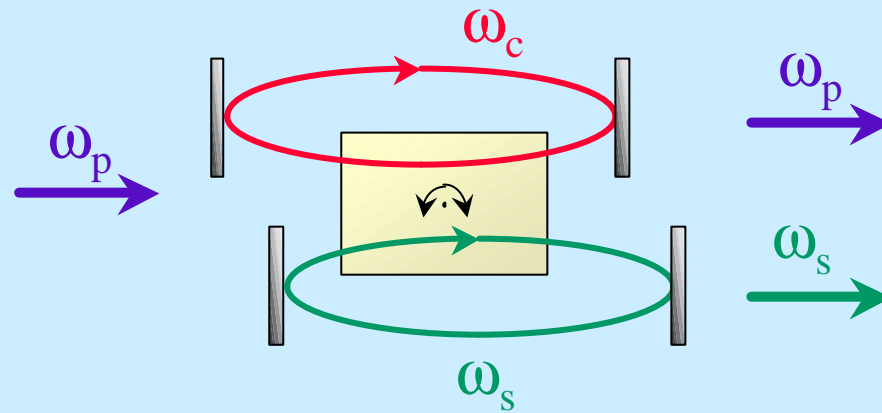


Gaussian pulse ;DROPO, $\Phi = 40 \mu\text{m}$;
 $f = 10 \text{ kHz}$; $L_{cav} = 2 \text{ cm}$

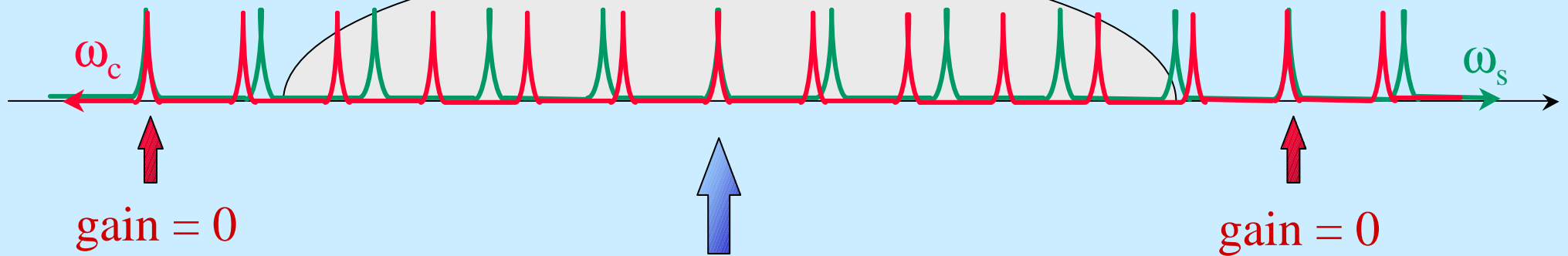
8. Quelques développements récents

- 8.a Etat de l'art des OPO impulsions
- 8.b Etat de l'art des OPO continus
- 8.b Accord de phase dans les guides d'ondes
- 8.c Biréfringence de Fresnel
- 8.d Amplification paramétrique géante d'impulsions chirpées
- 8.e Matériaux non linéaire quantique

Entangled Cavity Doubly resonant OPO

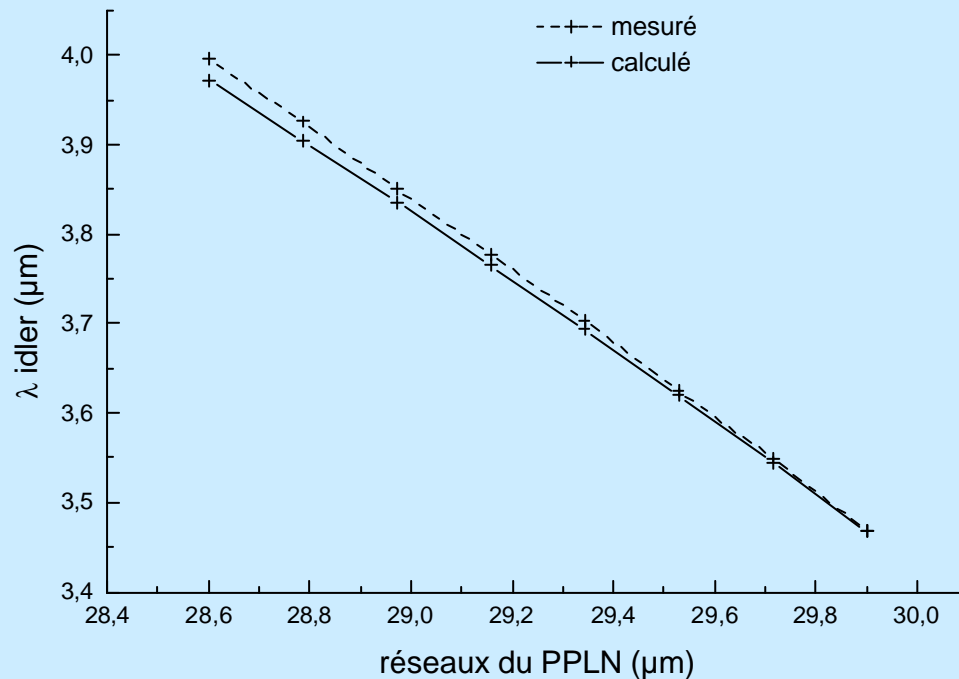
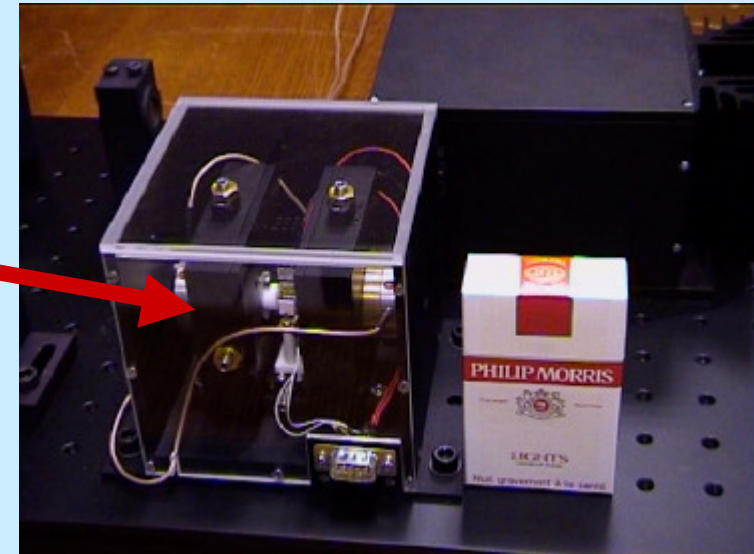
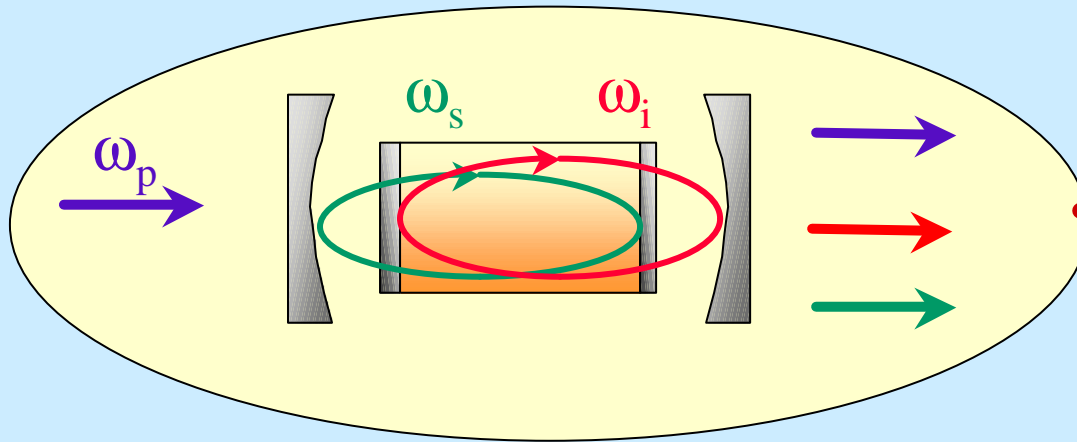


Parametric gain



Single frequency emission

Semi-monolithic dual cavity mid-IR DROPO



Performances :

$f \sim 15$ kHz

$E = 1$ $\mu\text{J}/\text{pulse}$

λ_i tunable 3 to 4,5 μm

Threshold ~ 4 $\mu\text{J}/\text{pulse}$

single frequency (~ 200 MHz)

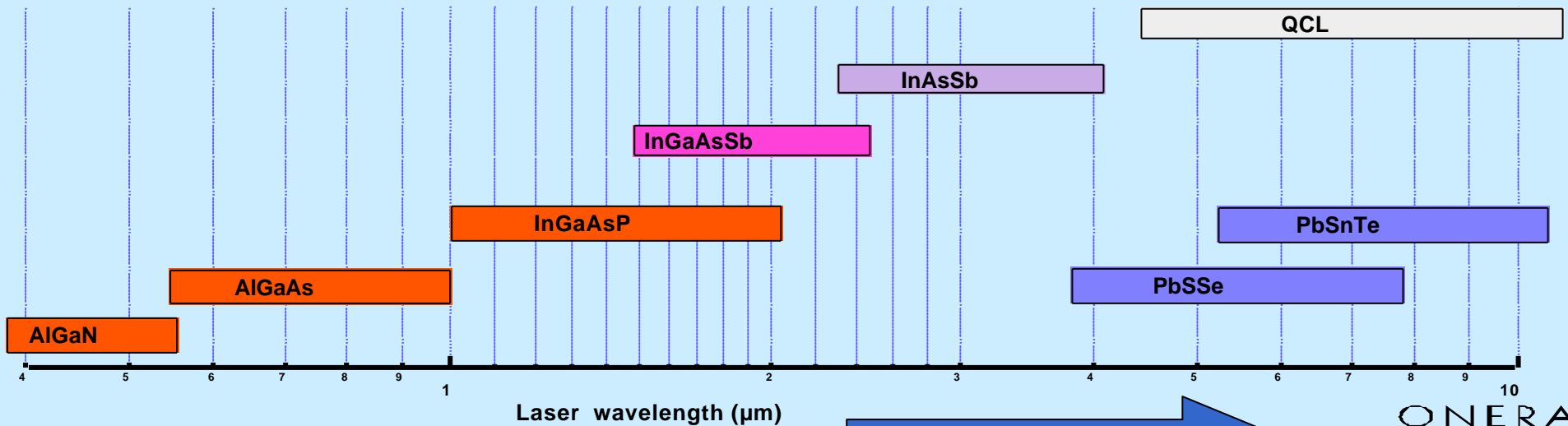
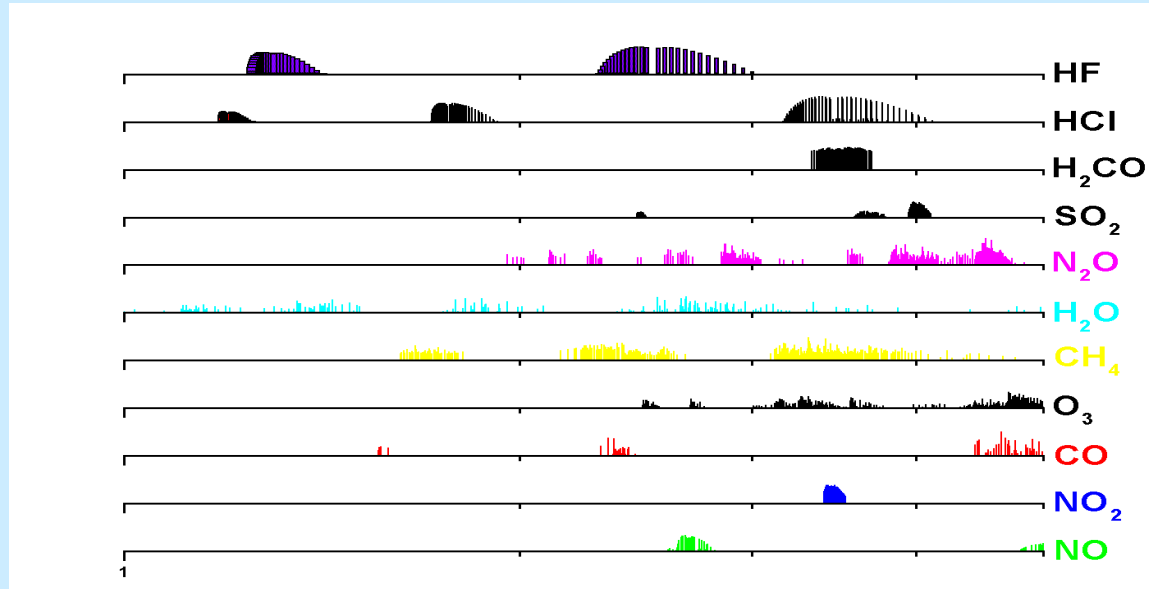
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Lefebvre, Rosencher, Ribet, Drag JOSA 2000, OL 2002

Diodes laser

VS

OPO



CRYOGENY →

ONERA

SEMICONDUCTORS

- $0.45 \mu\text{m} < l_{\text{cutoff}} < 20 \mu\text{m}$ ($0.05 \text{ eV} < E_{\text{gap}} < 3 \text{ eV}$)

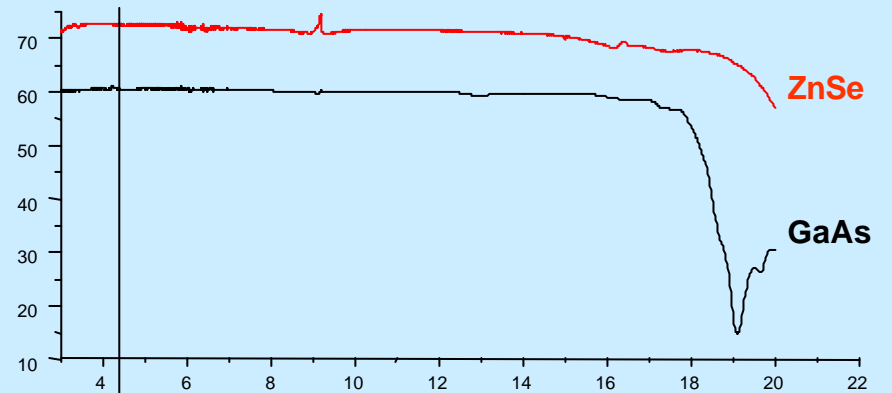


- High nonlinear performance (band theory) :

$$P_{NLO} \propto \frac{d^2}{n^3} \propto \frac{E_{\text{gap}}^{-4}}{E_{\text{gap}}^{-3}} \propto I_{\text{cutoff}}$$

Second Fermi Golden Rule

Transmission including Fresnel losses (%)



- Large transparency region



- Low cost



- Mature technology III-V



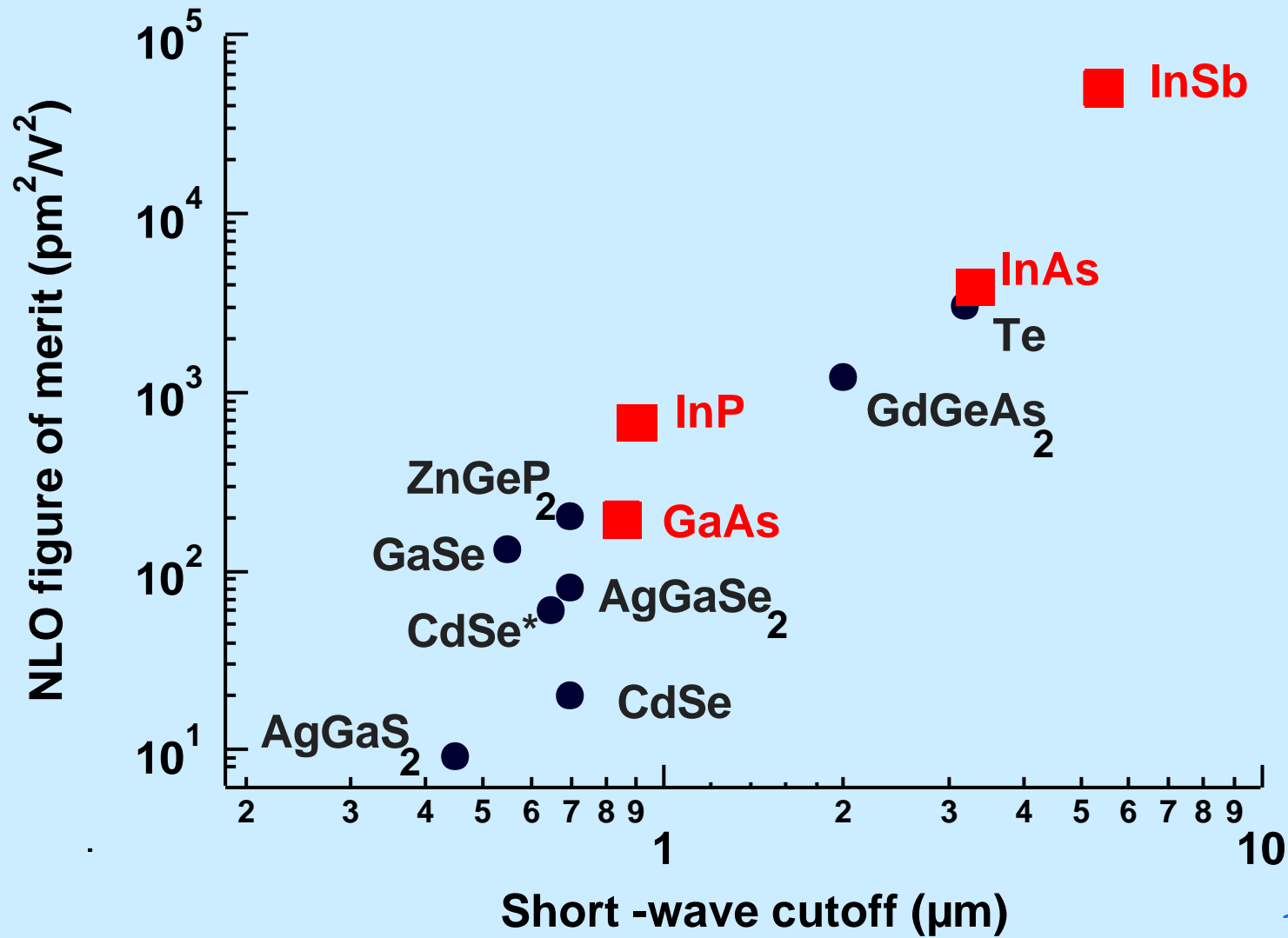
- Isotropic materials ↻ NO possible phase matching scenario

LiNbO₃



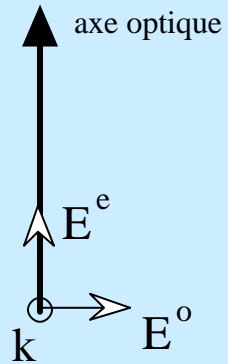
Figure de mérite des semiconducteurs

$$\frac{d^2}{n^3}$$

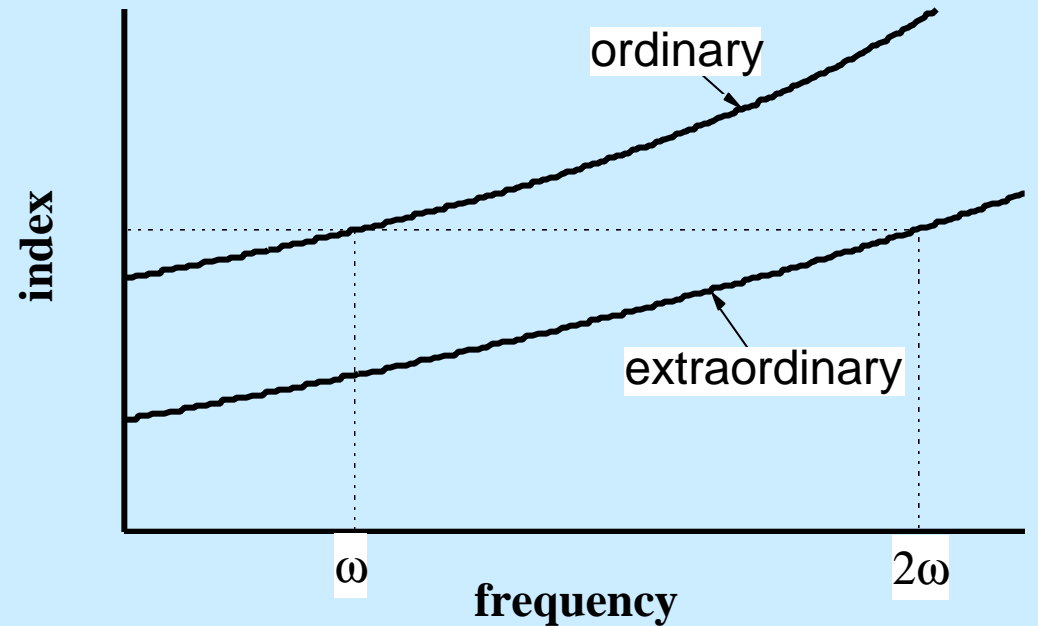
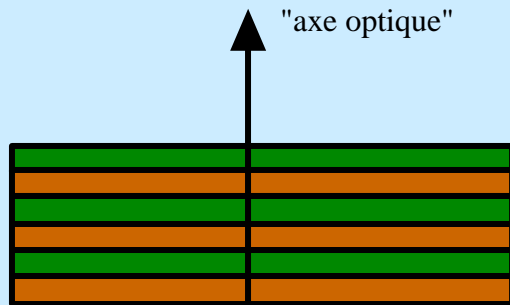


PHASE MATCHING BY ARTIFICIAL BIREFRINGENCE

cristaux biréfringents: (ex. KTP)

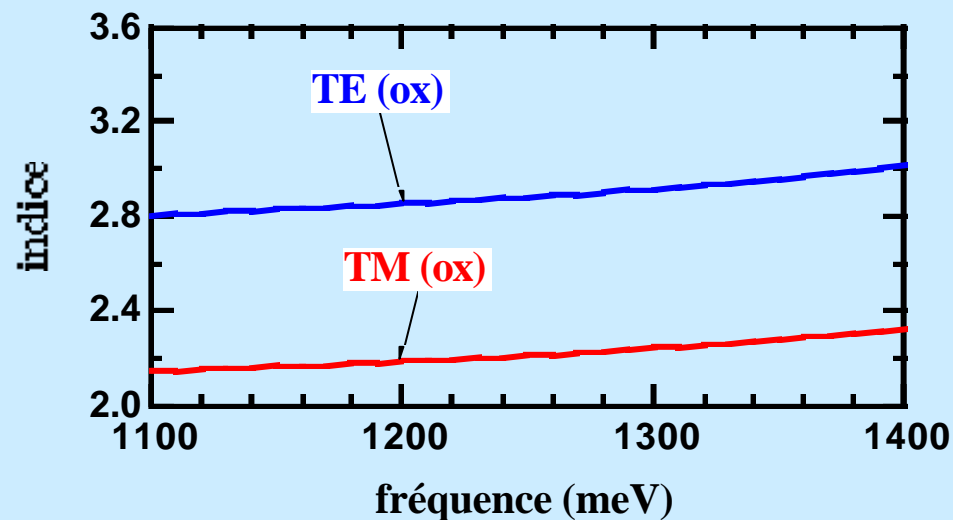
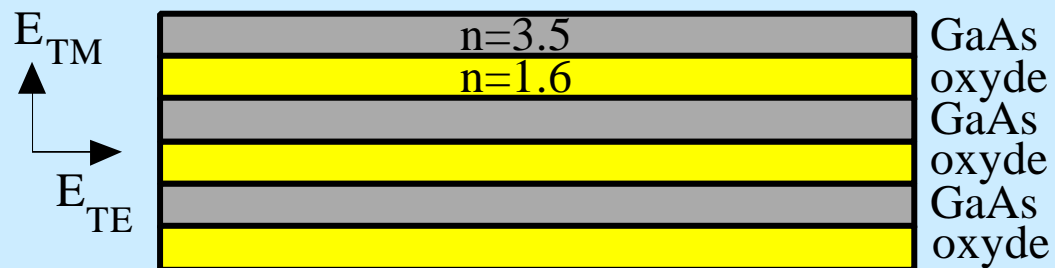
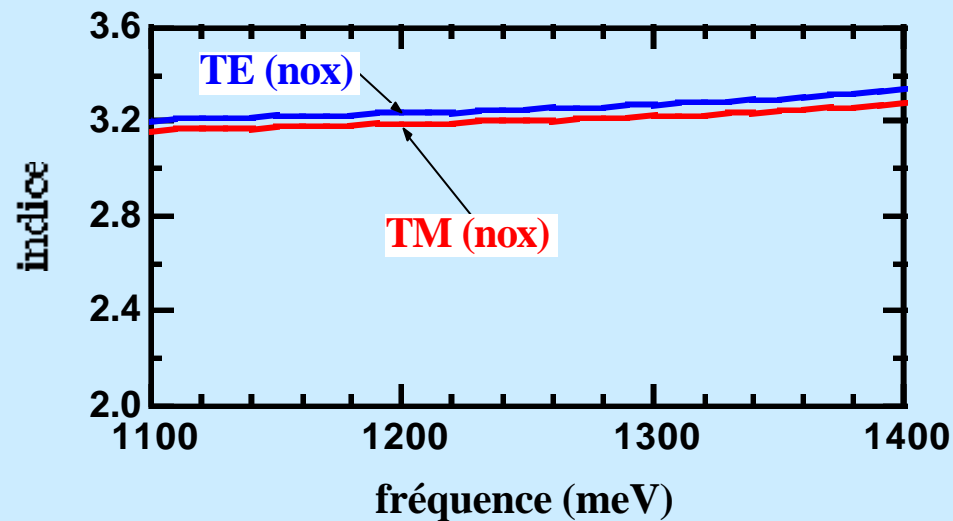
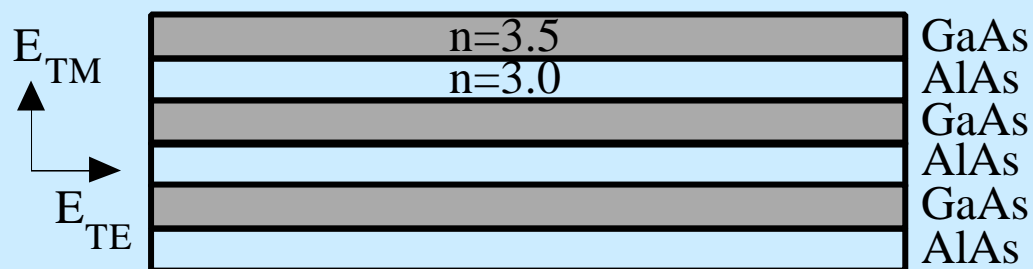


biréfringence de forme: (ex. GaAs/AlAs)



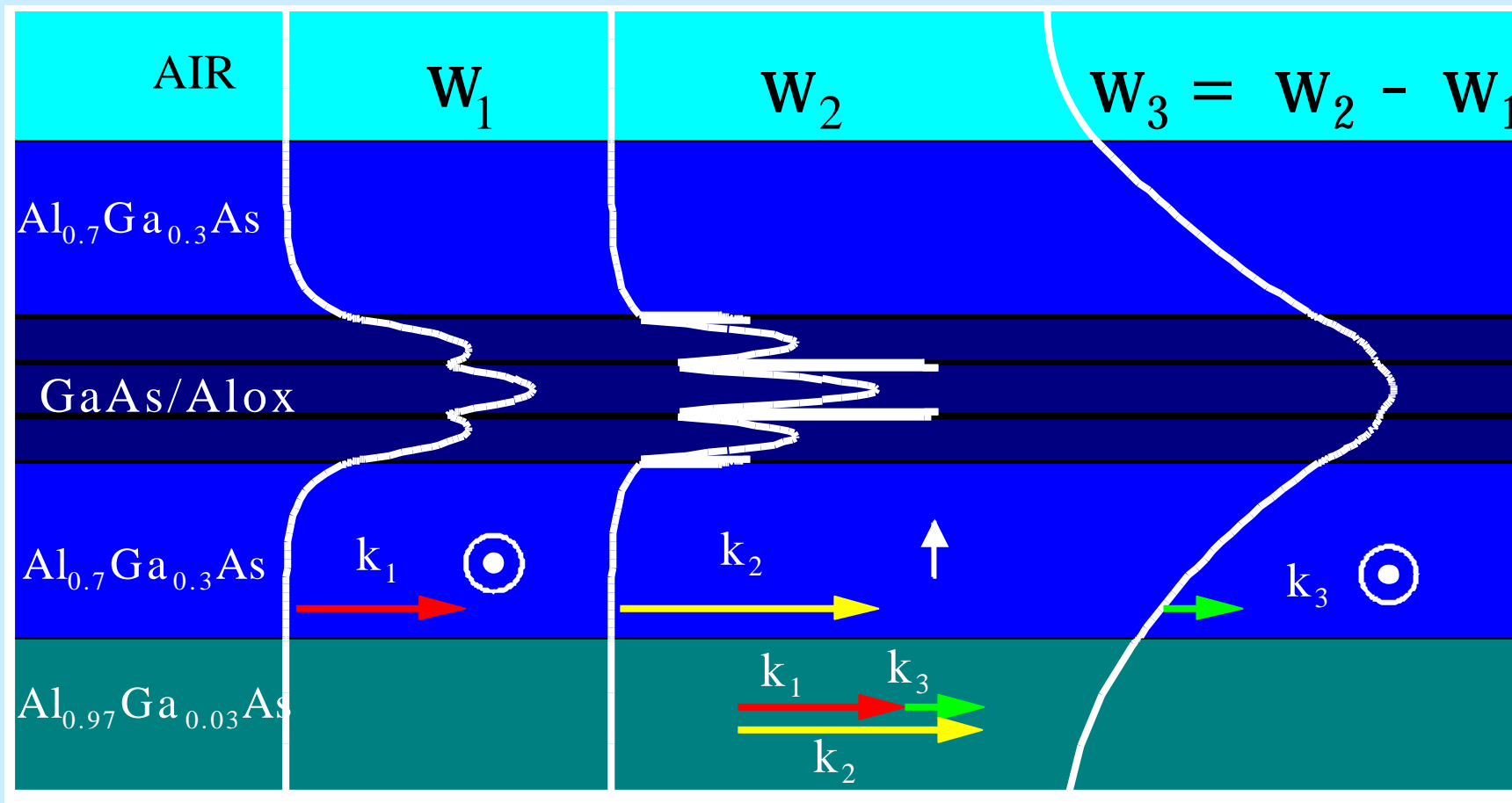
$$n_o(\omega) = n_e(2\omega) \quad \text{P accord de phase}$$

GIANT BIREFRINGENCE IN GaAs/AlOx heterostructures

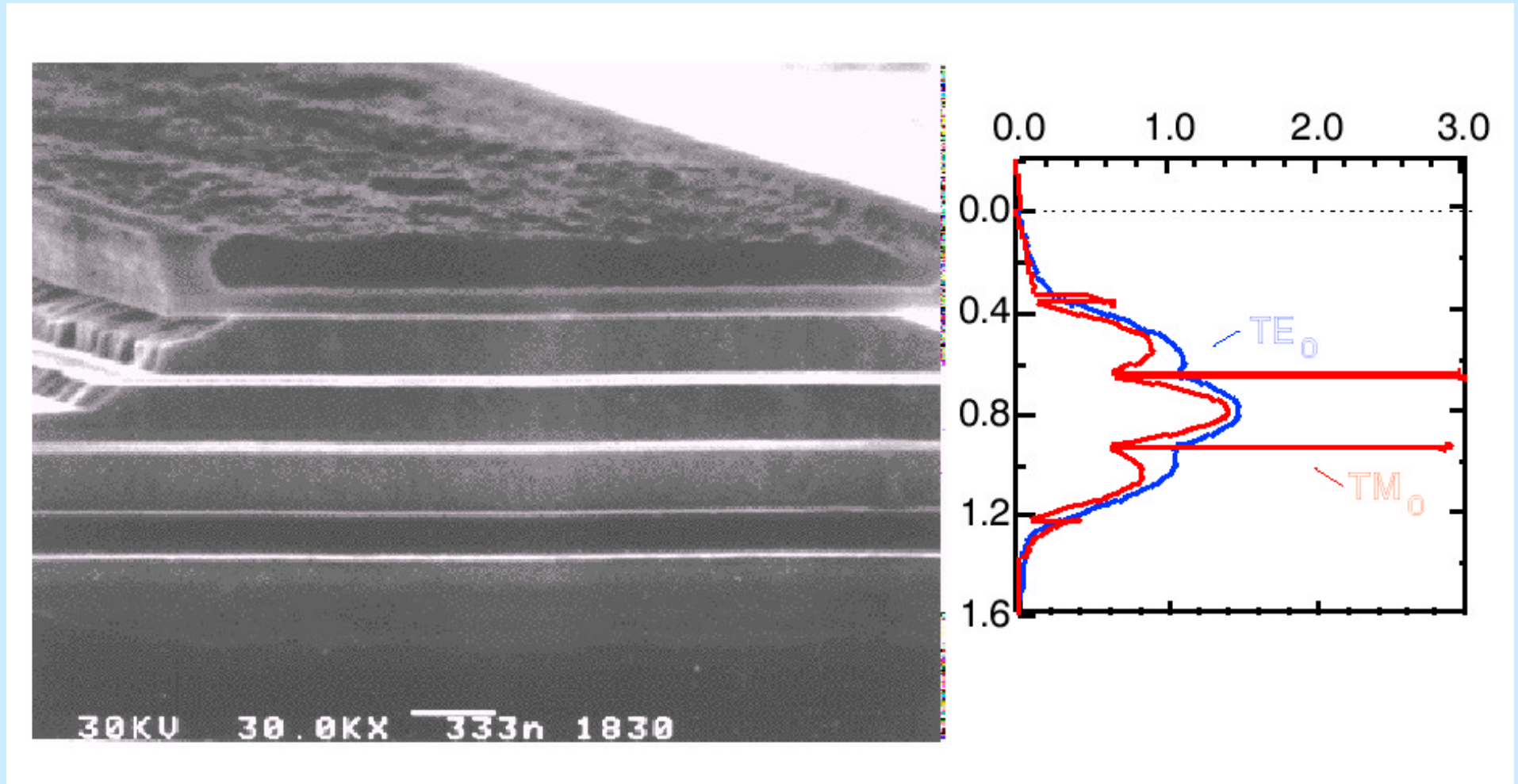


$$E_{TE} (1) = E_{TE} (2)$$

$$n_1^2 E_{TM} (1) = n_2^2 E_{TM} (2)$$



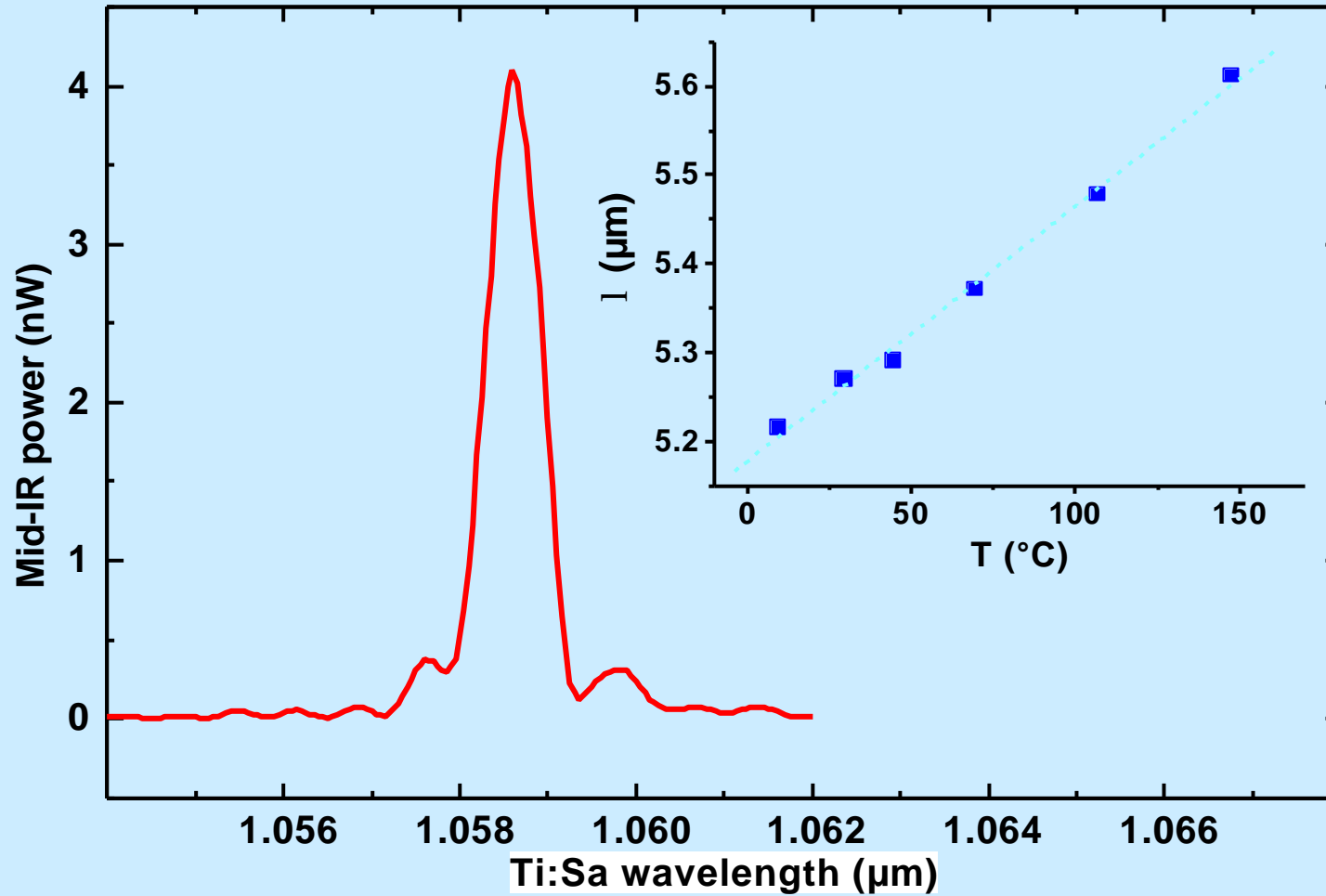
SAMPLE AND ELECTRIC FIELD DISTRIBUTION



OPTIMISATION DE $\int_0^L E_1(z) E_2(z) E_3(z) dz$

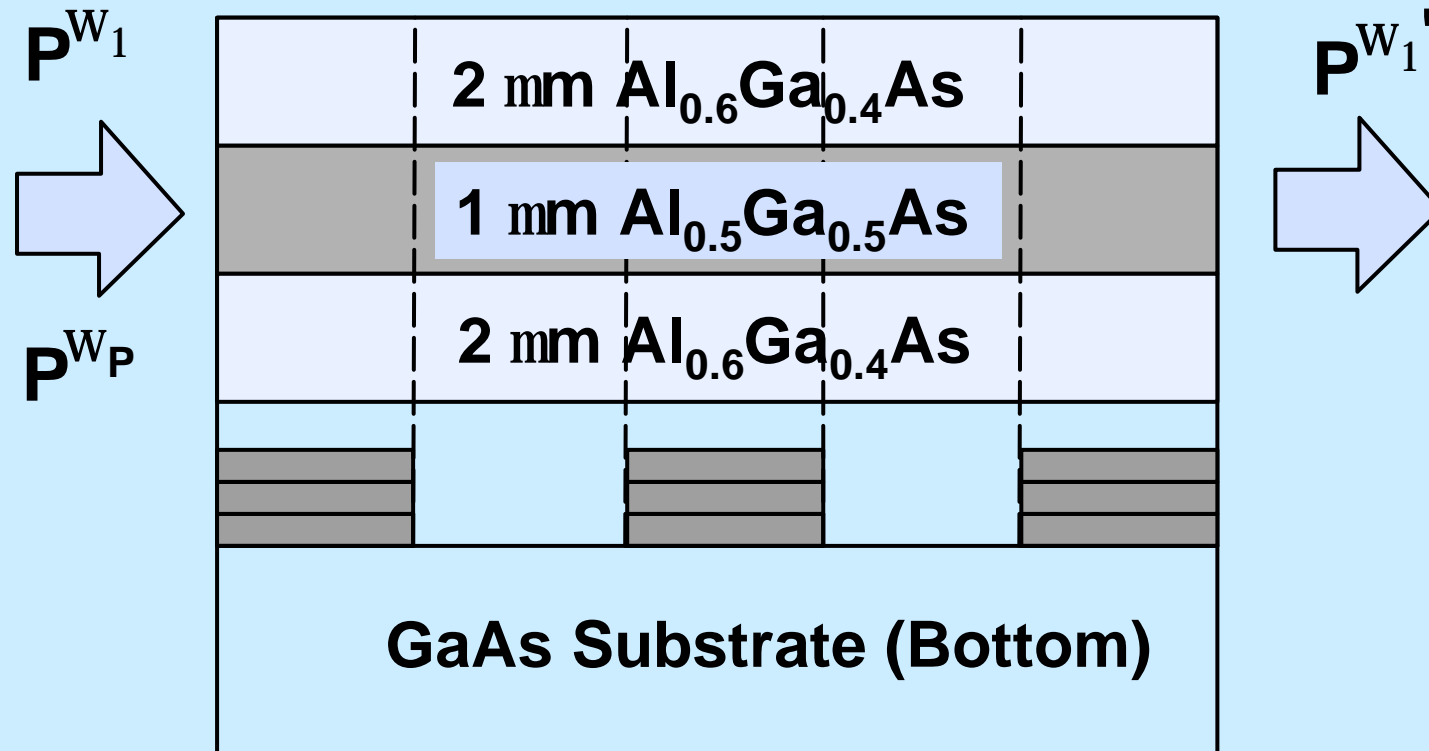
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IR OUTPUT AND TUNABILITY

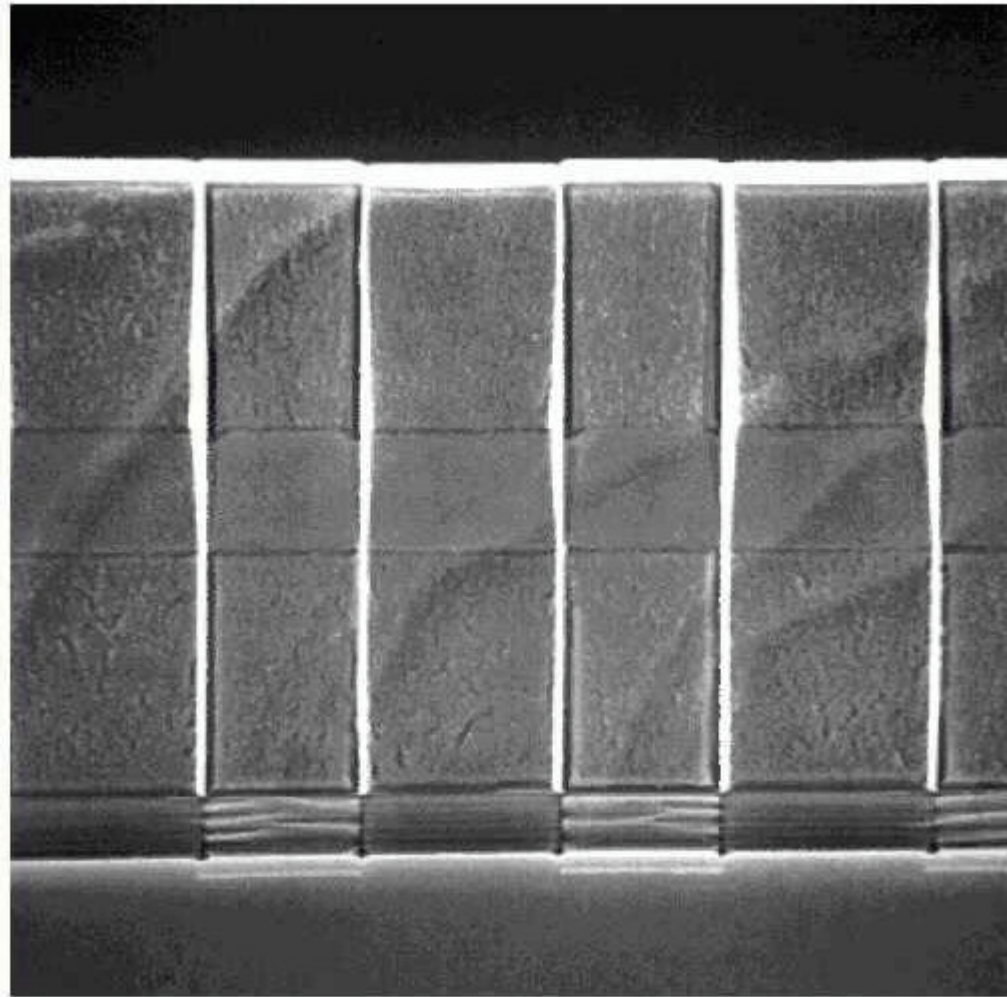


Fiore, Berger, Rosencher, Nagle Nature 1998

QUASI PHASE MATCHING IN GaAs/AlGaAs waveguide: the patterned growth method



MBE: Ben Yoo, APL (1997)
MOCVD: M. Fejer and B. Gérard, APL (2000)

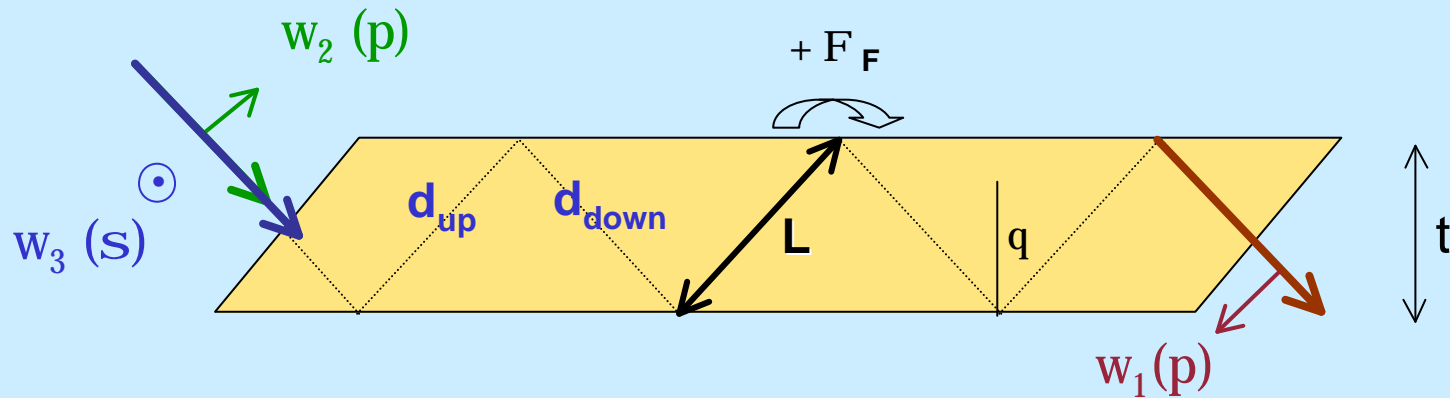


3 mm

MBE: Ben Yoo ,APL (1997)

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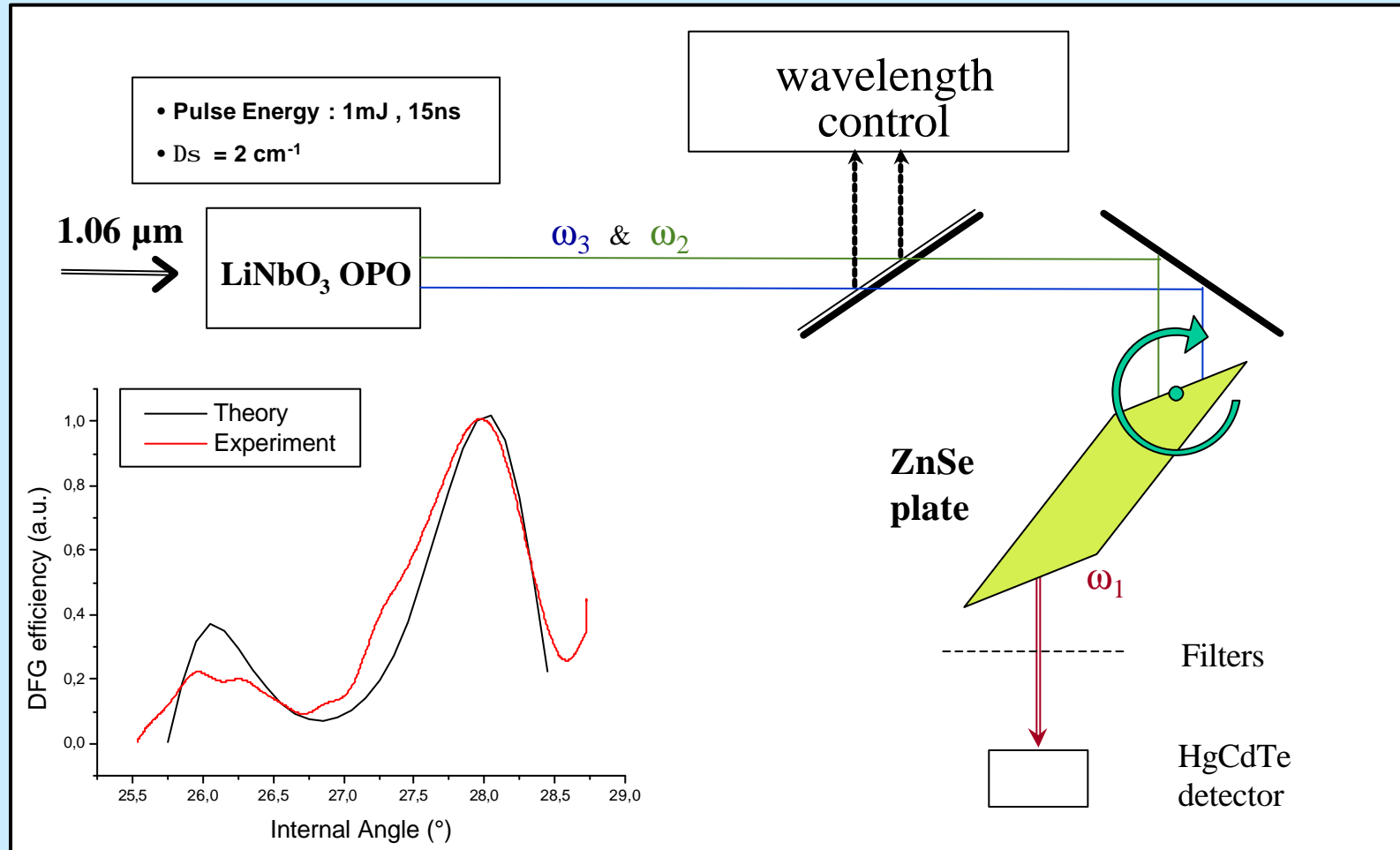
Quasi Phase Matching by Total Internal Reflexion * taking into account Fresnel Birefringence



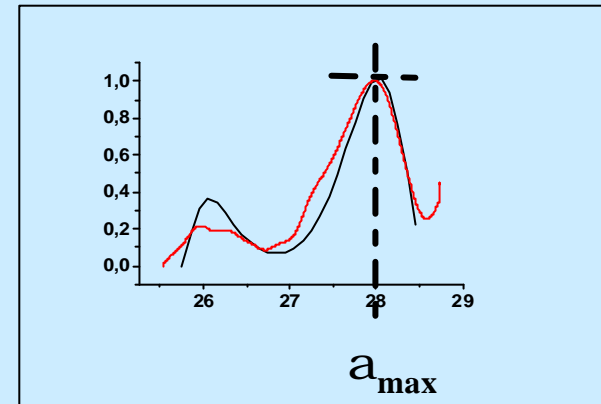
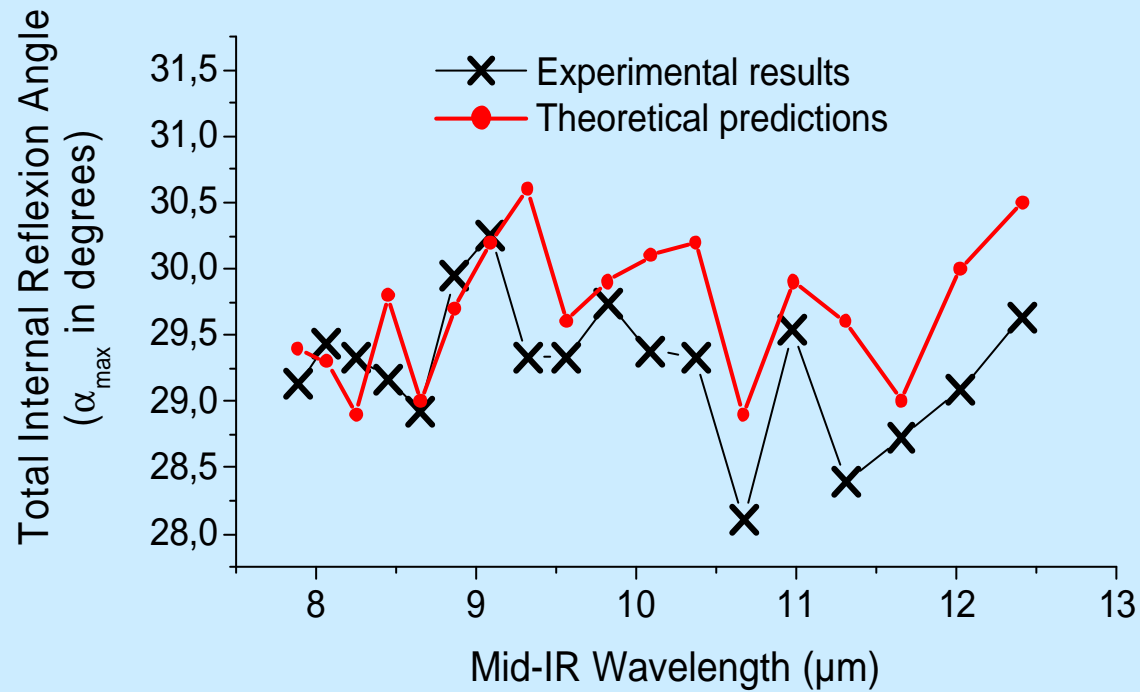
$$df_{\text{tot}} = Dk \cdot L + F_F + \begin{cases} 0 & \text{if } d_{\text{up}} \cdot d_{\text{down}} > 0 \\ p & \text{if } d_{\text{up}} \cdot d_{\text{down}} < 0 \end{cases}$$

* Armstrong et al., Phys. Rev. **127**, 1918-1939 (1962)

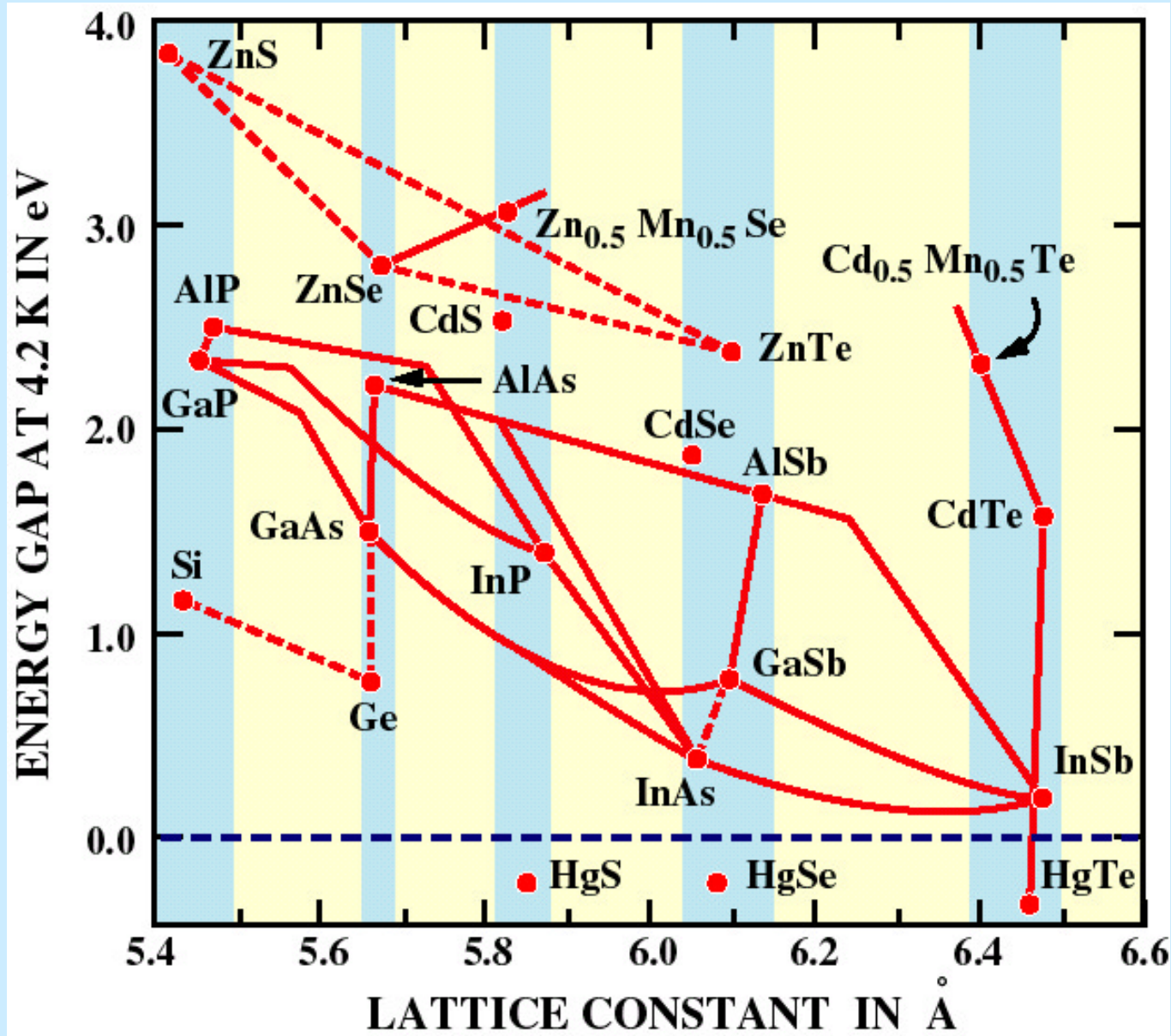
Fresnel phase matching Configuration : experimental set-up



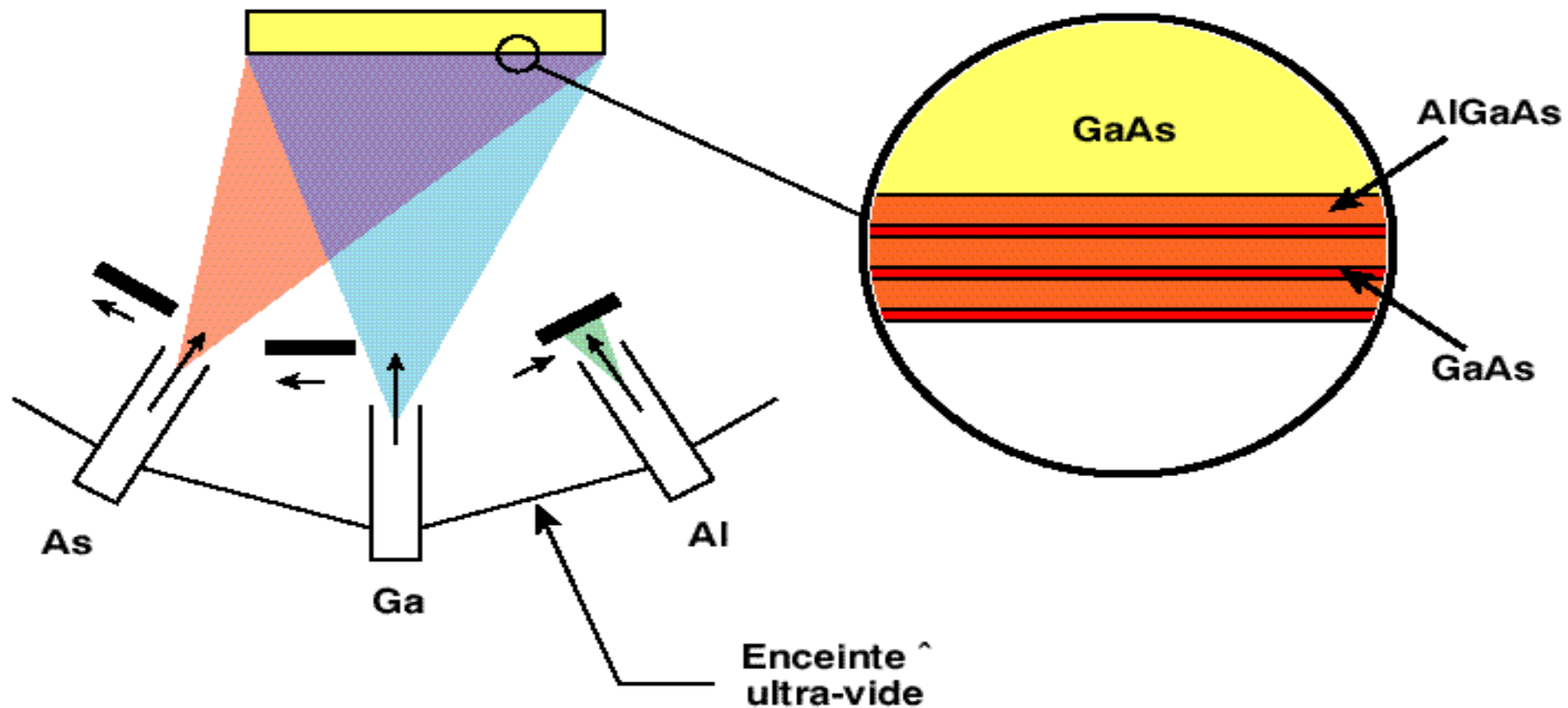
Tuning behaviour of Fresnel phase matching

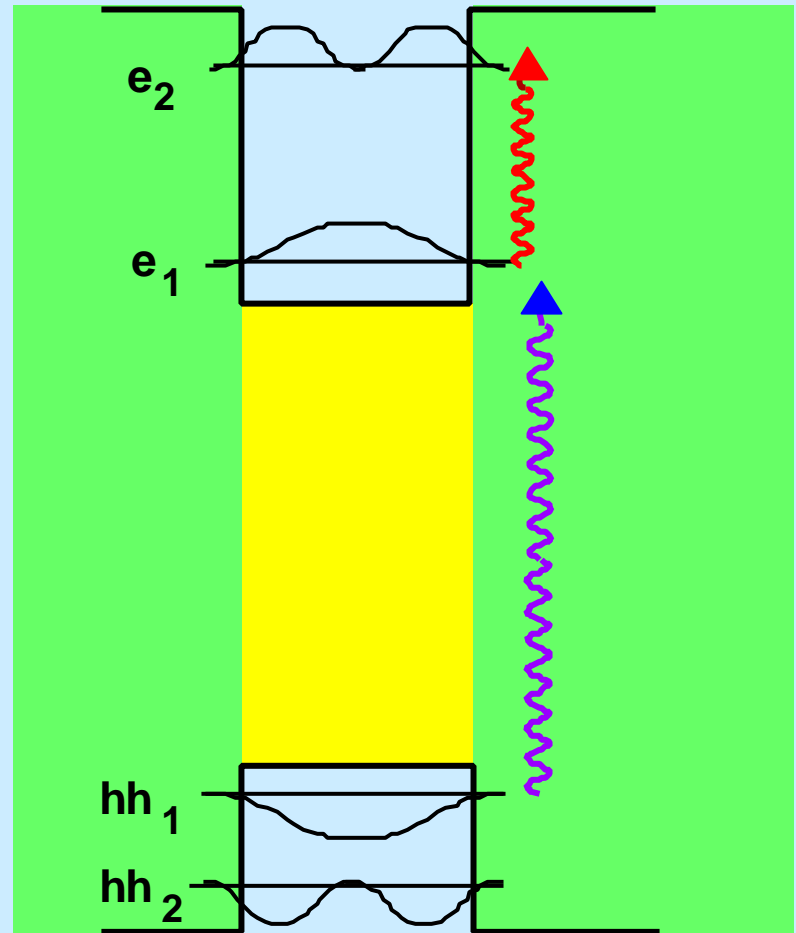
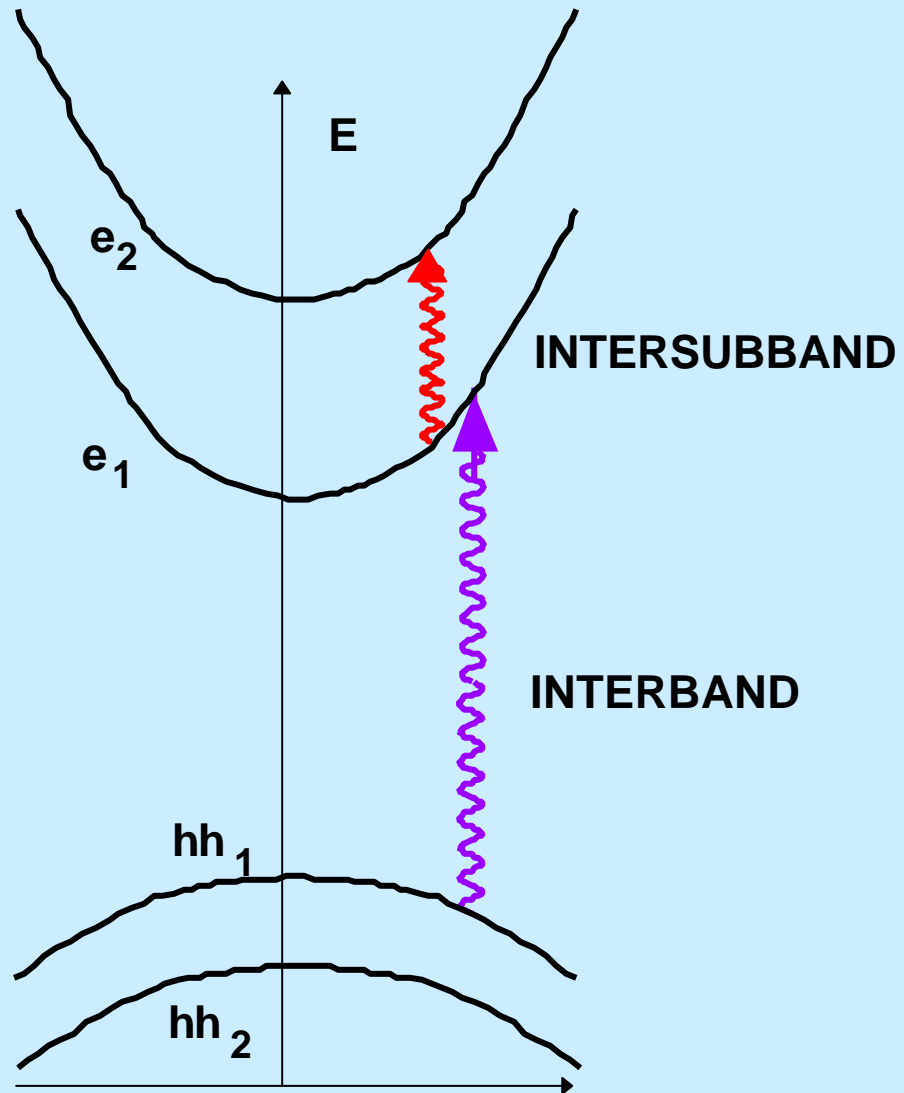


Familles de semiconducteurs



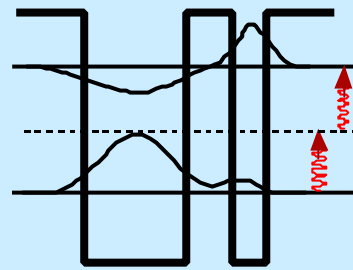
EPITAXIE PAR JETS MOLECULAIRES



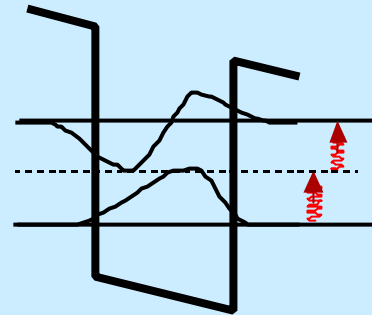


ONERA

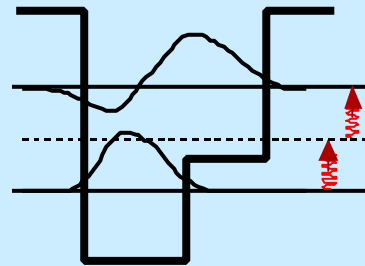
Différentes structures asymétriques



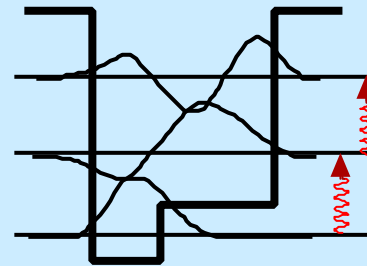
(A)



(B)



(C)



(D)

ORIGIN OF GIANT OPTICAL SUSCEPTIBILITY

Second Fermi golden rule :

$$C^{(2)} = \frac{q^3 n_s}{e_0 \hbar^2} m_{31} \frac{m_{12}}{\text{total energy mismatch 1} \otimes 2} \frac{m_{23}}{\text{total energy mismatch 2} \otimes 3}$$

Two effects in QWs :

$$C^{(2)} \gg \frac{q^3 n_s}{e_0 \hbar^2} \frac{m_{12} m_{23} m_{31}}{(w - w_{12} - ig)(2w - 2w_{12} - ig)}$$

$\frac{1}{m_c^{3/2}}$	effective mass
$\frac{1}{dw^2}$	double resonance

Approche quantique de l'Optique Non Linéaire:1

\mathbf{r} matrice densité du système quantique $\mathbf{r} \equiv \sum_i p_i |\mathbf{j}_i\rangle\langle\mathbf{j}_i|$

p_i probabilité statistique que le système soit dans un état \mathbf{j}_i

$$\langle \bar{A} \rangle = \text{Tr}(\mathbf{r} A)$$

r_{ii} population moyenne de l'état i

r_{ij} cohérence entre les états i et j

$$\frac{\partial r_{ij}}{\partial t} = \frac{1}{i\hbar} [H_0 - qz E(t), \mathbf{r}]_{i,j} - \mathbf{G}_{i,j} \left(\mathbf{r} - \mathbf{r}^{(0)} \right)_{i,j}$$

Exemple: valeur moyenne de la polarisation

$$P(t) = \text{Tr}(\mathbf{r} q \hat{z})$$

Approche quantique de l'Optique Non Linéaire:2

Approche perturbative $\mathbf{r}(t) = \sum_n \mathbf{r}^n(t)$ avec

$$\frac{\partial \mathbf{r}_{i,j}^{n+1}}{\partial t} = \frac{1}{i\hbar} \left\{ H_0, \mathbf{r}^{n+1} \right\}_{i,j} - i\hbar \mathbf{G}_{i,j} \mathbf{r}_{i,j}^{n+1} \left\} - \frac{1}{i\hbar} \left[q \hat{z} E(t), \mathbf{r}^n \right]_{i,j}$$

La polarisation est maintenant la somme de contribution d'ordres croissants

$$P^n(t) = Tr \left(\mathbf{r}^n q \hat{z} \right) \quad \text{avec} \quad \mathbf{r}^n(t) = \mathbf{r}^n(\omega) e^{in\omega t} + cc$$

aux deux premiers ordres

$$P(t) = \underbrace{\mathbf{e}_0 \mathbf{c}^{(1)} E e^{i\omega t}}_{\text{Optique linéaire}} + \underbrace{\mathbf{e}_0 \mathbf{c}^{(2)} E^2 e^{i2\omega t}}_{\text{GSH}} + \underbrace{\mathbf{e}_0 \mathbf{c}_r |E|^2}_{\text{Rectification optique}}$$

Optique linéaire

GSH

Rectification optique

ONERA

Approche quantique de l'Optique Non Linéaire:3

Relation de récurrence

$$\mathbf{r}_{i,j}^{n+1}(\mathbf{w}) = \frac{q \left[\hat{z}, \mathbf{r}^n \right]_{i,j}}{\hbar \left[(n+1)\mathbf{w} + \mathbf{w}_{i,j} - i\mathbf{G}_{i,j} \right]} E$$

Aux deux premiers ordres

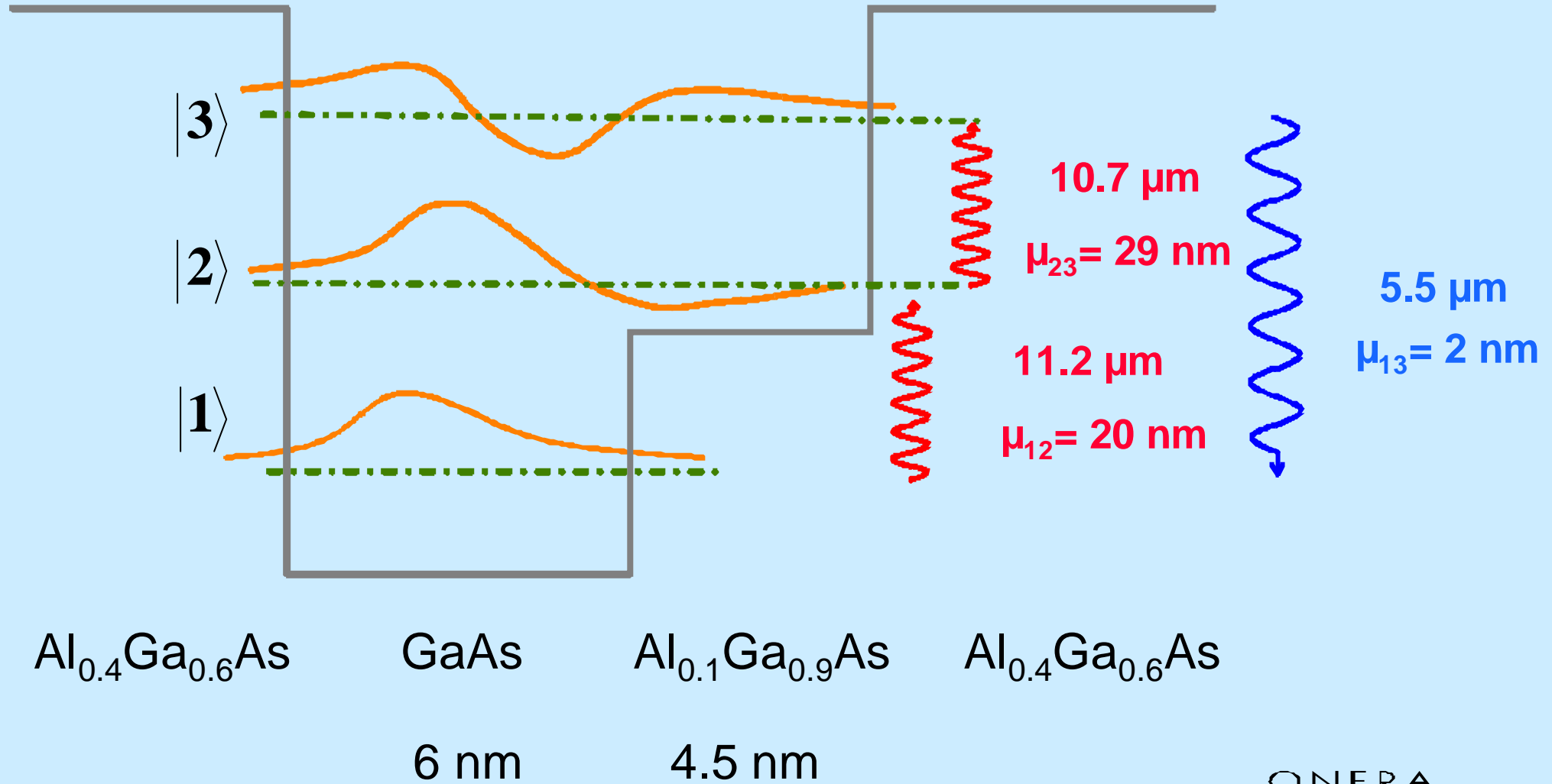
$$\left\{ \begin{array}{l} \mathbf{r}_{i,j}^1(\mathbf{w}) = \frac{q z_{i,j} (n_j - n_i)}{\hbar \left[\mathbf{w} + \mathbf{w}_{i,j} - i\mathbf{G}_{i,j} \right]} E \\ \mathbf{r}_{i,j}^2(\mathbf{w}) = \frac{1}{\hbar \left[2\mathbf{w} + \mathbf{w}_{i,j} - i\mathbf{G}_{i,j} \right]} \left[q \hat{z}, \mathbf{r}^1 \right]_{i,j} E \end{array} \right.$$

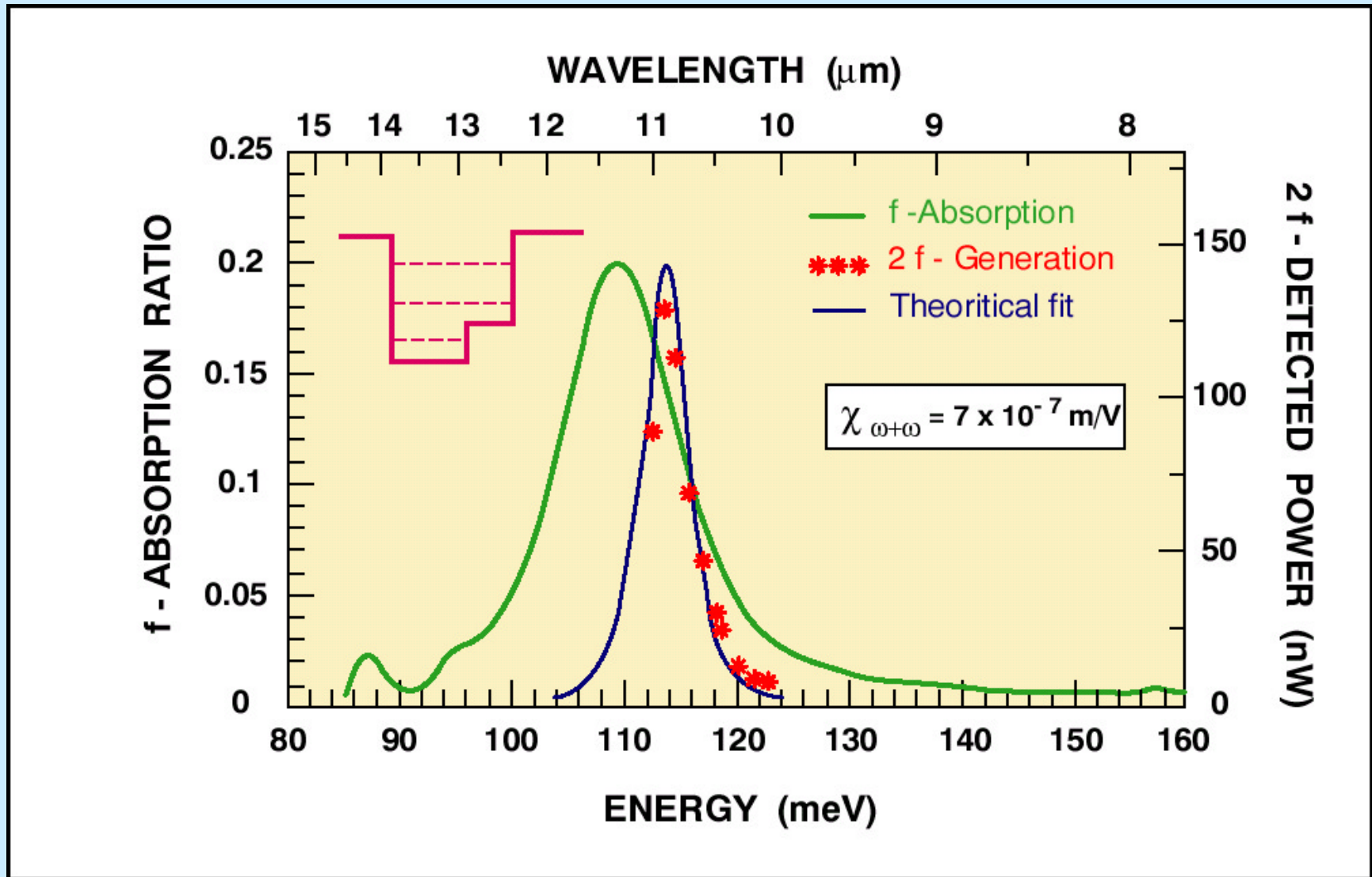
$$\mathbf{c}^{(2)} = \frac{q^3}{\epsilon_0 \hbar^2} \sum_i \sum_i \frac{1}{(2\mathbf{w} + \mathbf{w}_{ki}) - i\mathbf{G}_{ki}}$$

Purement quantique

$$\sum_l \mathbf{m}_{ik} \mathbf{m}_{kl} \mathbf{m}_{li} \left[\frac{n_i - n_l}{(\mathbf{w} + \mathbf{w}_{li}) - i\mathbf{G}_{li}} - \frac{n_l - n_k}{(\mathbf{w} + \mathbf{w}_{kl}) - i\mathbf{G}_{kl}} \right]$$


STRUCTURE QUANTIQUE ASYMETRIQUE: «LA» FORME OPTIMALE





CONCLUSIONS

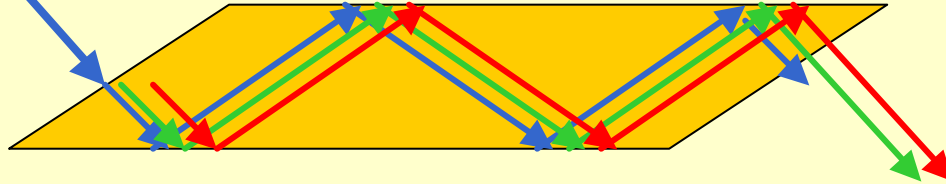
- **Semiconductors:** already very useful parametric sources in the 6 – 13 μm range
soon parametric oscillations

	pros	cons
QPM by molecular bonding	<ul style="list-style-type: none"> • No growth • possibility of complex structures 	<ul style="list-style-type: none"> • Large tunability only from the MIR • Time consuming, manual
QPM by patterned growth	<ul style="list-style-type: none"> • Large tunability • mass production 	<ul style="list-style-type: none"> • Extreme technological difficulties
Fresnel phase matching	<ul style="list-style-type: none"> • no technology • parametric florescence • NR-QPM: high tunability, tolerance 	<ul style="list-style-type: none"> • complex optical system • highly demanding in roughness control
Microcavity OPO	<ul style="list-style-type: none"> • integration potential • simple micro-device 	<ul style="list-style-type: none"> • low tunability
Artificial birefringence in waveguide	<ul style="list-style-type: none"> • mass production • integration potential 	<ul style="list-style-type: none"> • Extreme technological difficulties <p style="text-align: right;">ONERA</p> 

Future work

Sol 1: auto-OPO accordé en biréfringence de Fresnel


1.9 μm



Pompe: 1.9 μm

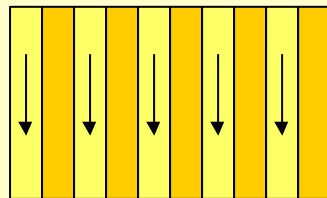
Laser: 2.3 μm


DFG-OPO: 10 μm

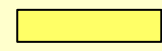
 ZnSe:Cr X

Sol 2: auto-OPO quasi-accordé en phase

1,9 μm



 ZnSe:Cr poly

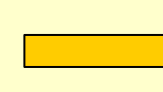
 ZnSe X

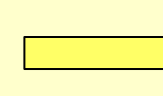
Sol 3: passer de la DFG à l'OPO

1,9 μm



10 μm

 ZnSe
GaAs

 Ge, Si
GaAs