

Contribution to the Measurement of Turbulent Structures



Creatis

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TI2006
Mai, 2006

Outline

- **Introduction**
- **Integral Length Scales**
- **Experimental set up**
- **Signal processing**
- **Result**
- **Conclusion**

Introduction

- Objective : Size estimation of turbulent structures.
- Classical way : Integral Length Scales (ILS) measurement with:
 - Hot Wire Anemometry method
 - Laser Doppler Velocimetry method.
- Measurement inside a transparent combustion engine:
 - Schlieren Optical Method & High Speed Film Camera
 - Signal processing: Time-Frequency distributions.

Integral Length Scales

Integral Length Scale represents a temporal average of all the length scales present in a flow.

$$T = \int_0^{\infty} R_E(0,0,0;\tau).d\tau$$

$$L_x = \int_0^{\infty} R_E(\Delta x,0,0;0).d(\Delta x)$$

$$L_y = \int_0^{\infty} R_E(0,\Delta y,0;0).d(\Delta y)$$

Eulerian space-time correlation coefficients $R_E(\Delta x, \Delta y, \Delta z ; t)$ of the velocity fluctuation $u(x, y, z ; t)$ considering a point $p(x, y, z)$ at time t .

ILS Measurement

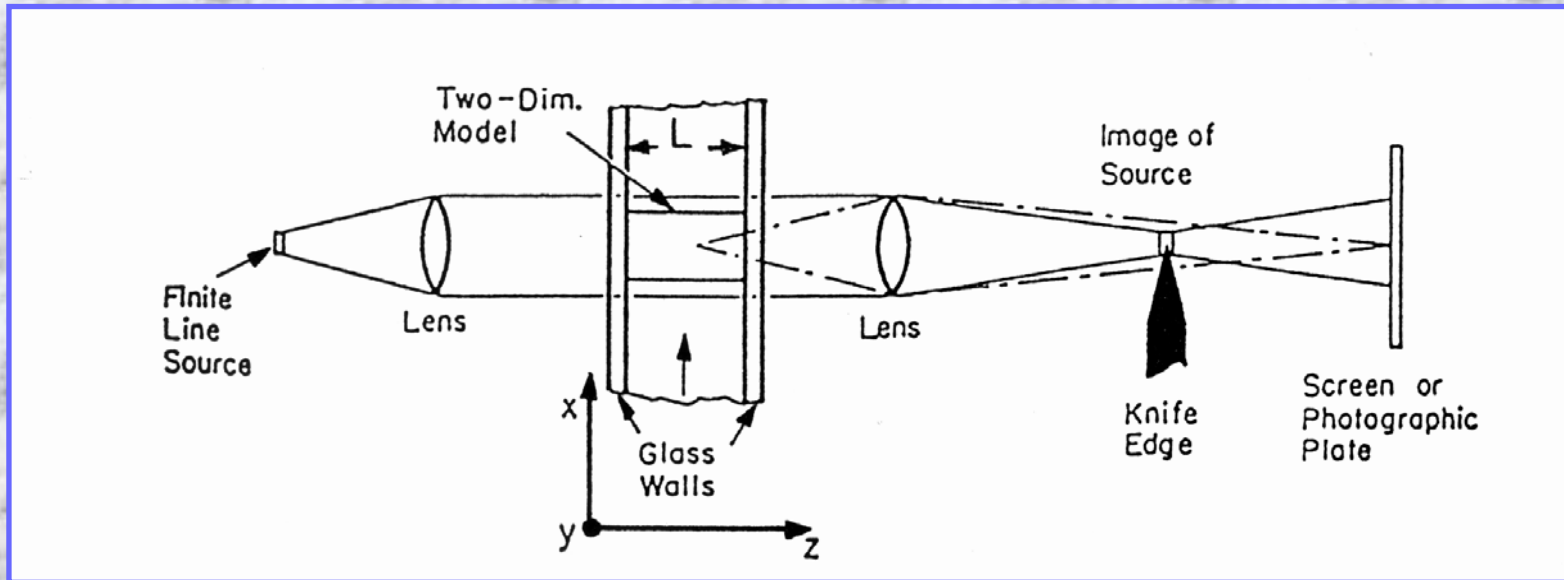
- From the velocity fluctuation (L.D.V.):
 - Covariance function.
 - Integral Length Scale (Empirical cut off frequency).
- From Schlieren optical method:
 - Schlieren images.
 - Time-Frequency distributions.

Experimental Set-up

- Air – propane IC Engine.
- Optical access in combustion chamber : Quartz windows.
- RPM = 1000
- CR=7.5
- $Re_T = 100$
- Crankangle: -40° before TDC to $+20^\circ$ after TDC.

Experimental Set-up

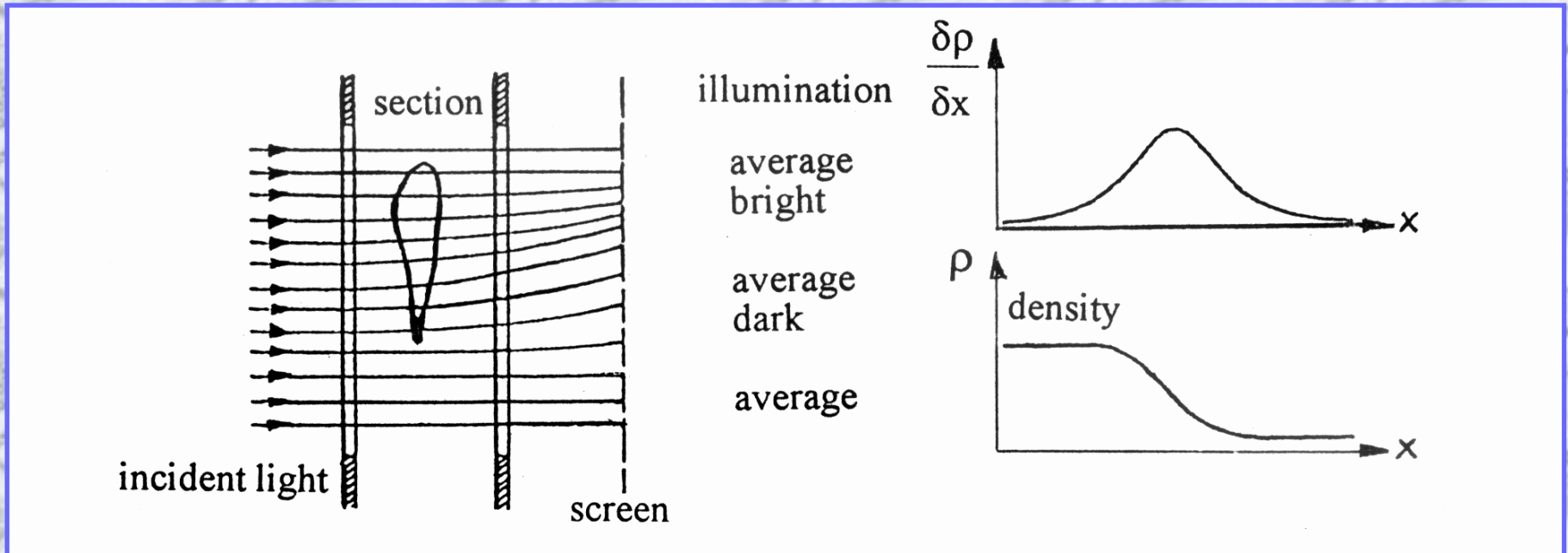
Schlieren system



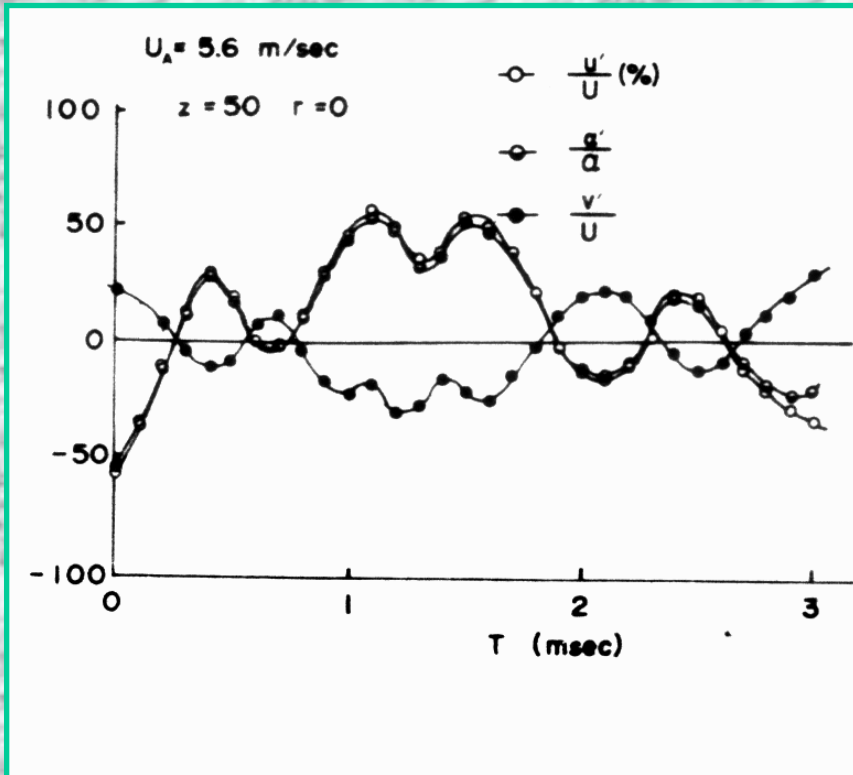
Deflection along x axis:

$$\vec{\varepsilon} = \frac{\vec{L}}{R} = L \cdot \overrightarrow{\text{grad}} n = L \cdot K_{G-D} \frac{\overrightarrow{\partial \rho}}{\partial x}$$

Experimental Set-up



Velocity & Density



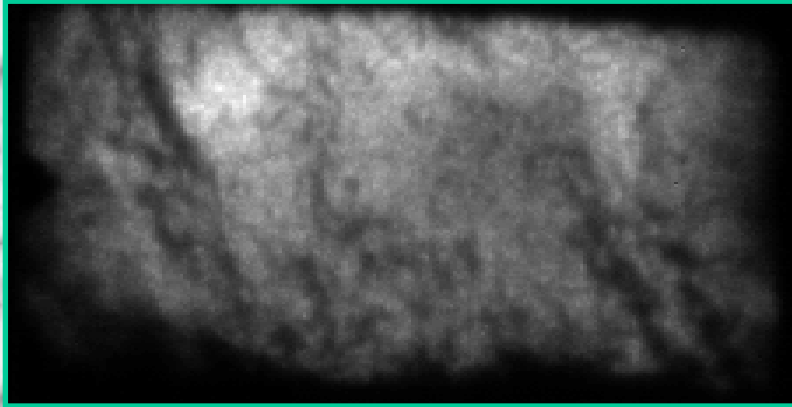
*High correlation between:

- Density Fluctuations
 - Velocity Fluctuations
- (Y. Aihara et al 1974).

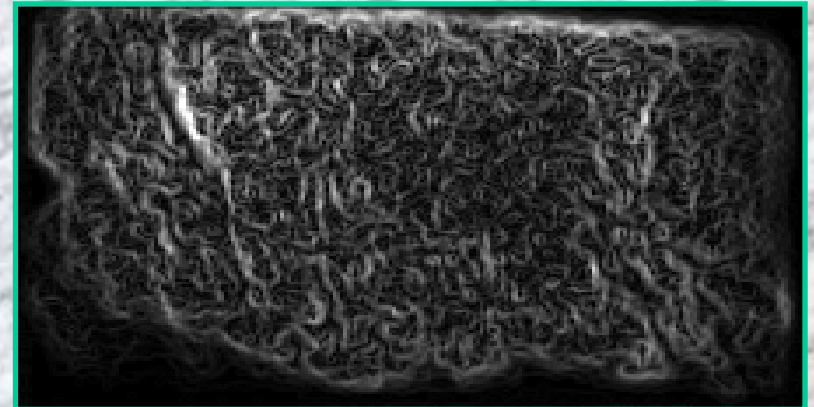
*From Schlieren Images:

- Density fluctuations
- Covariance function
- Integral Scales.

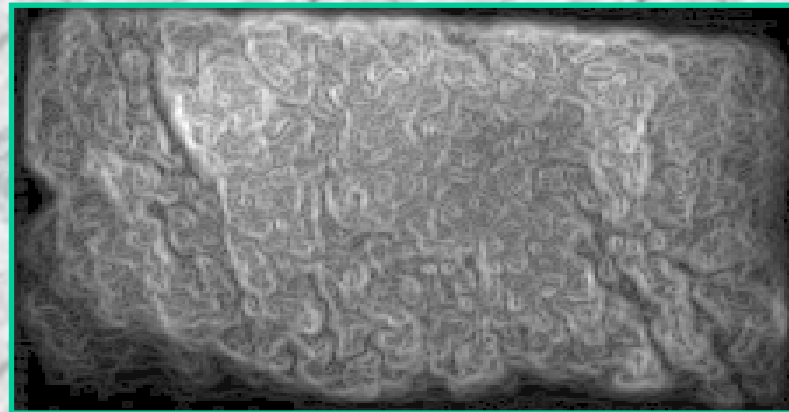
Turbulence image



Schlieren view



Sobel gradient image



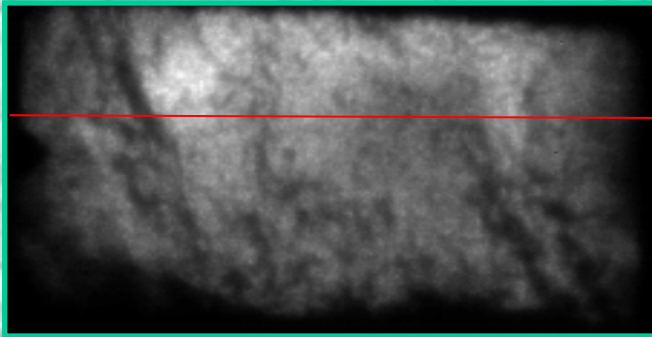
“Turbulence” view

Signal processing

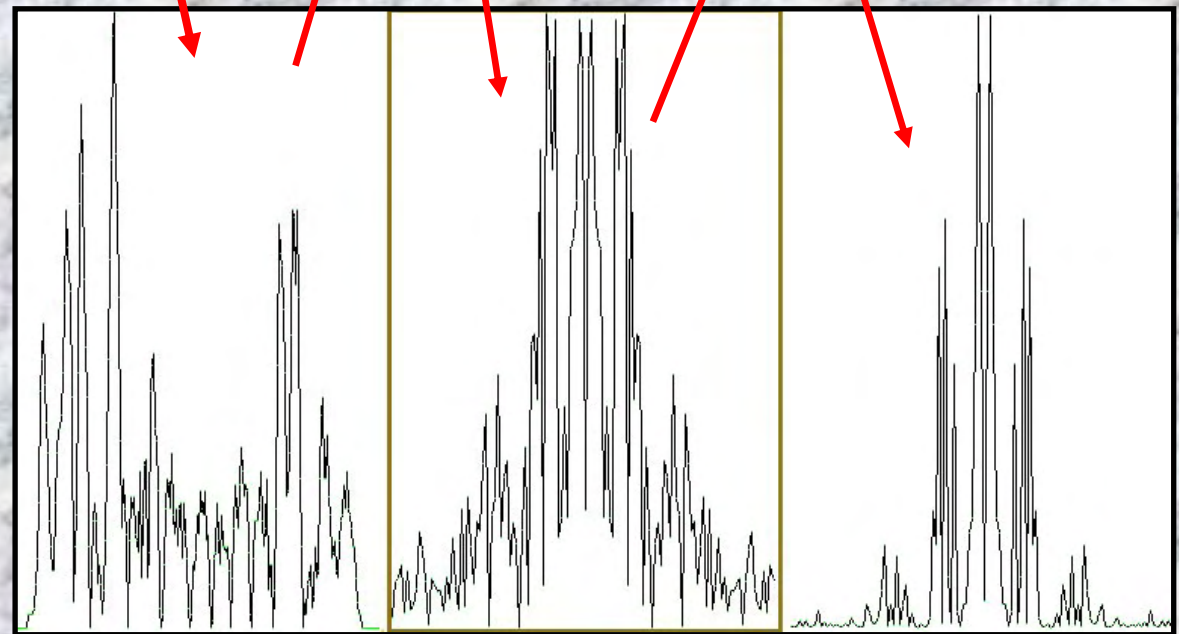
Measurement with Time-Frequency distributions of non stationary density fluctuations.

- Spectrogram : squared short time Fourier transform
- Wigner-Ville distribution.

Signal processing – Fourier Transform



Schlieren view



Spectrogram

$$S_Z(t, \nu) = \left| \int_{\mathbf{R}} Z(\tau) \cdot H^*(\tau - t) e^{-i2\pi\nu\tau} d\tau \right|^2$$

$$S_{\Gamma_Z}(\xi, \nu) = \left| \int_{\square} \Gamma_Z(\tau) \cdot \Gamma_H^*(\xi, \tau) \cdot e^{-i2\pi\nu\tau} d\tau \right|^2$$

Z consists in a row of a considered “Turbulence” image

Γ is the covariance of the non-stationary signal Z

Wigner-Ville distribution

$$W_z(t, \nu) = \int_{\mathbf{R}} z\left(t + \frac{\tau}{2}\right) \cdot z^*\left(t - \frac{\tau}{2}\right) \cdot e^{-2i\pi\nu\tau} d\tau$$

$$W(\xi, \nu) = \int_{\mathbf{R}} \Gamma_z(\tau, \xi) \cdot \Gamma_z^*(\tau, \xi) \cdot e^{-2i\pi\nu\tau} d\tau$$

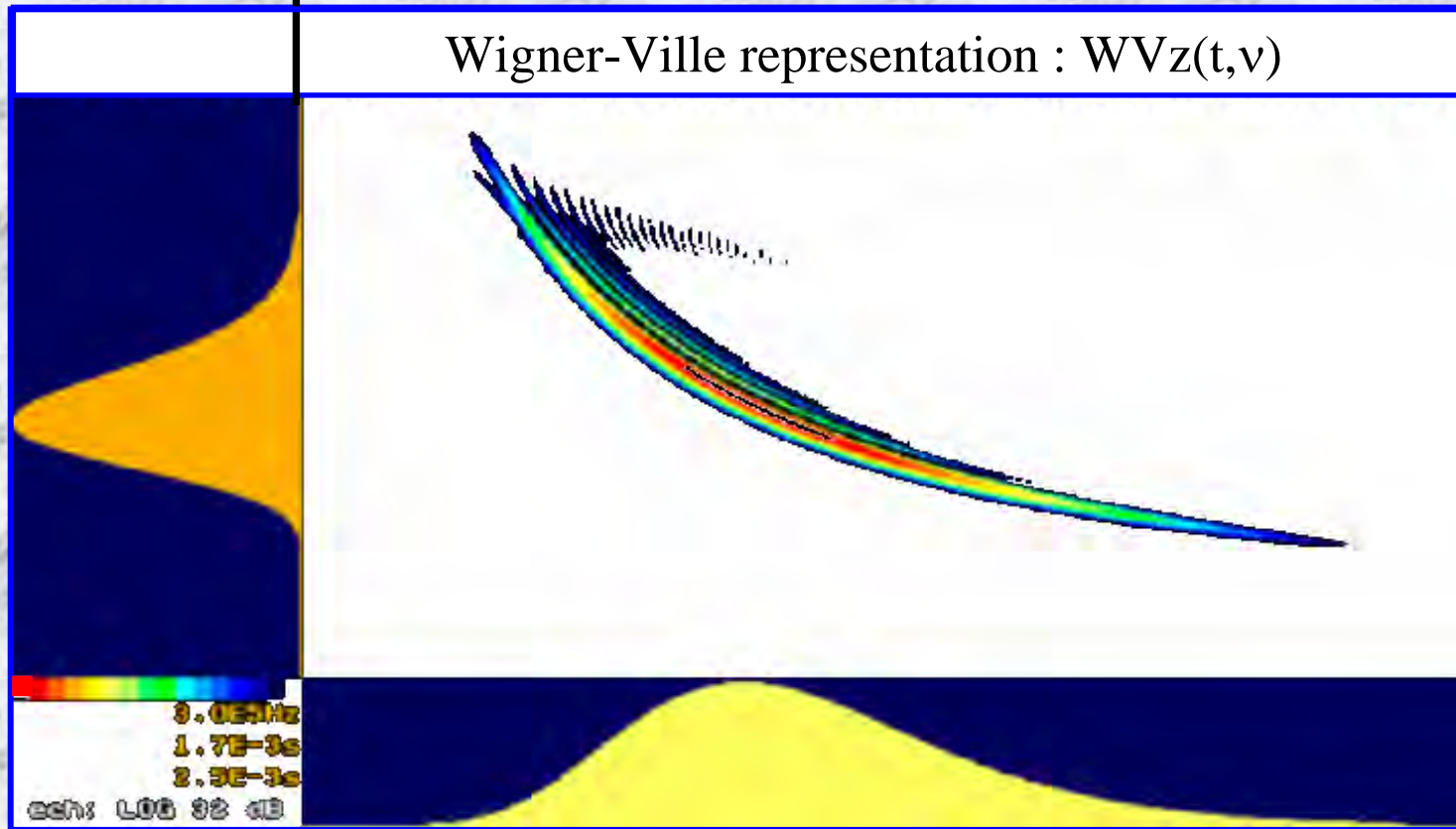
Z consists in a row of a considered “Turbulence” image

Γ is the covariance of the non-stationary signal Z

Hyperbolic frequency modulation

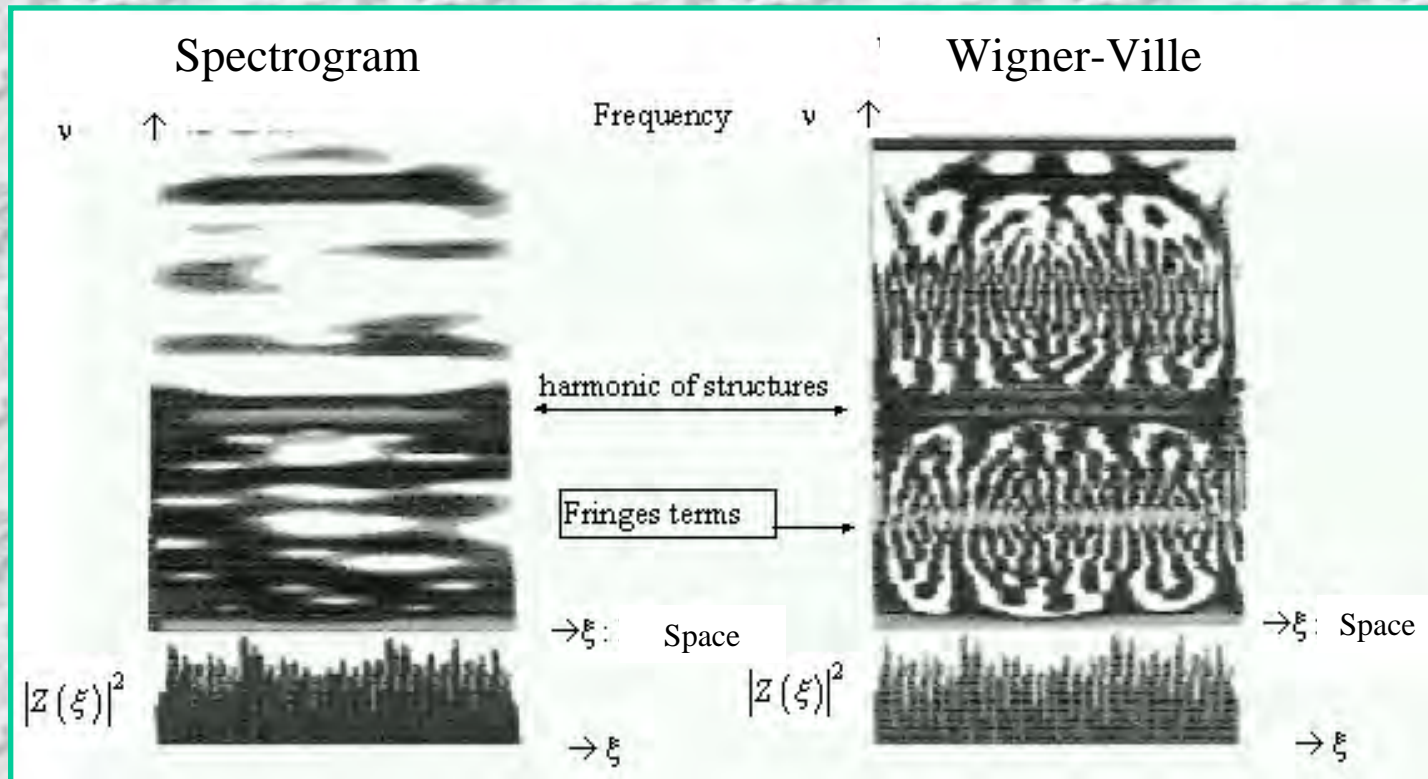
Frequency ν

Wigner-Ville representation : $WVz(t, \nu)$



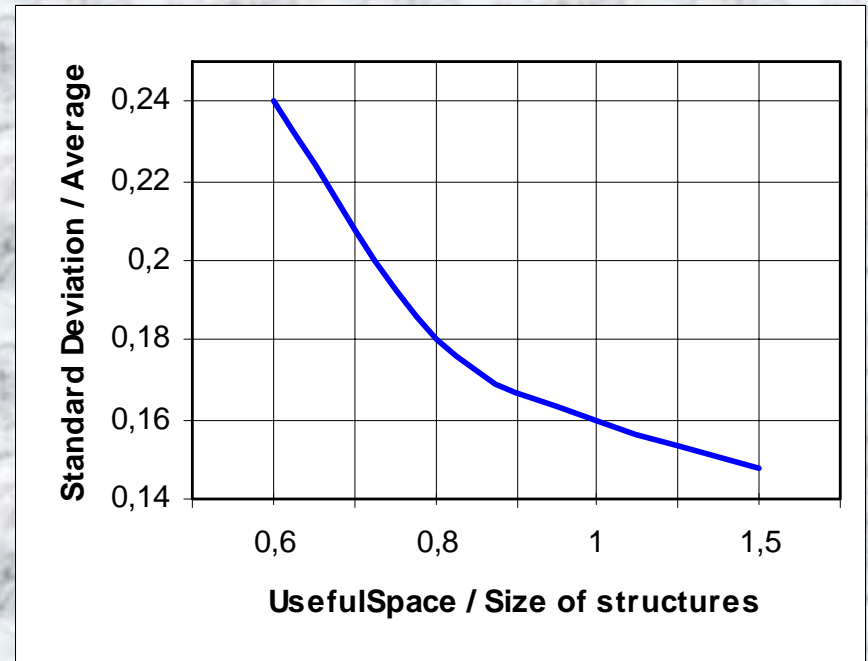
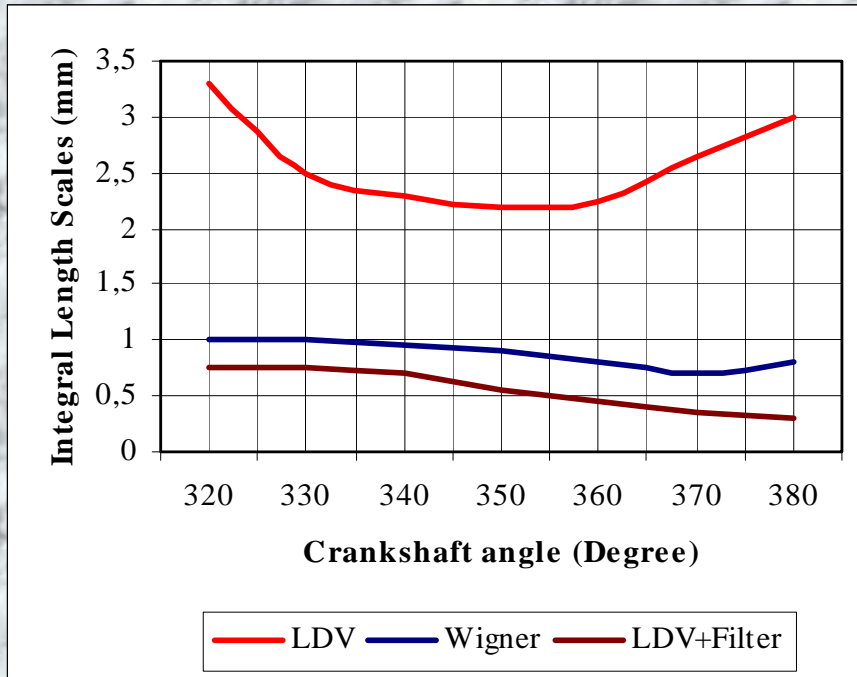
Time

Time-Frequency analysis of the density fluctuation



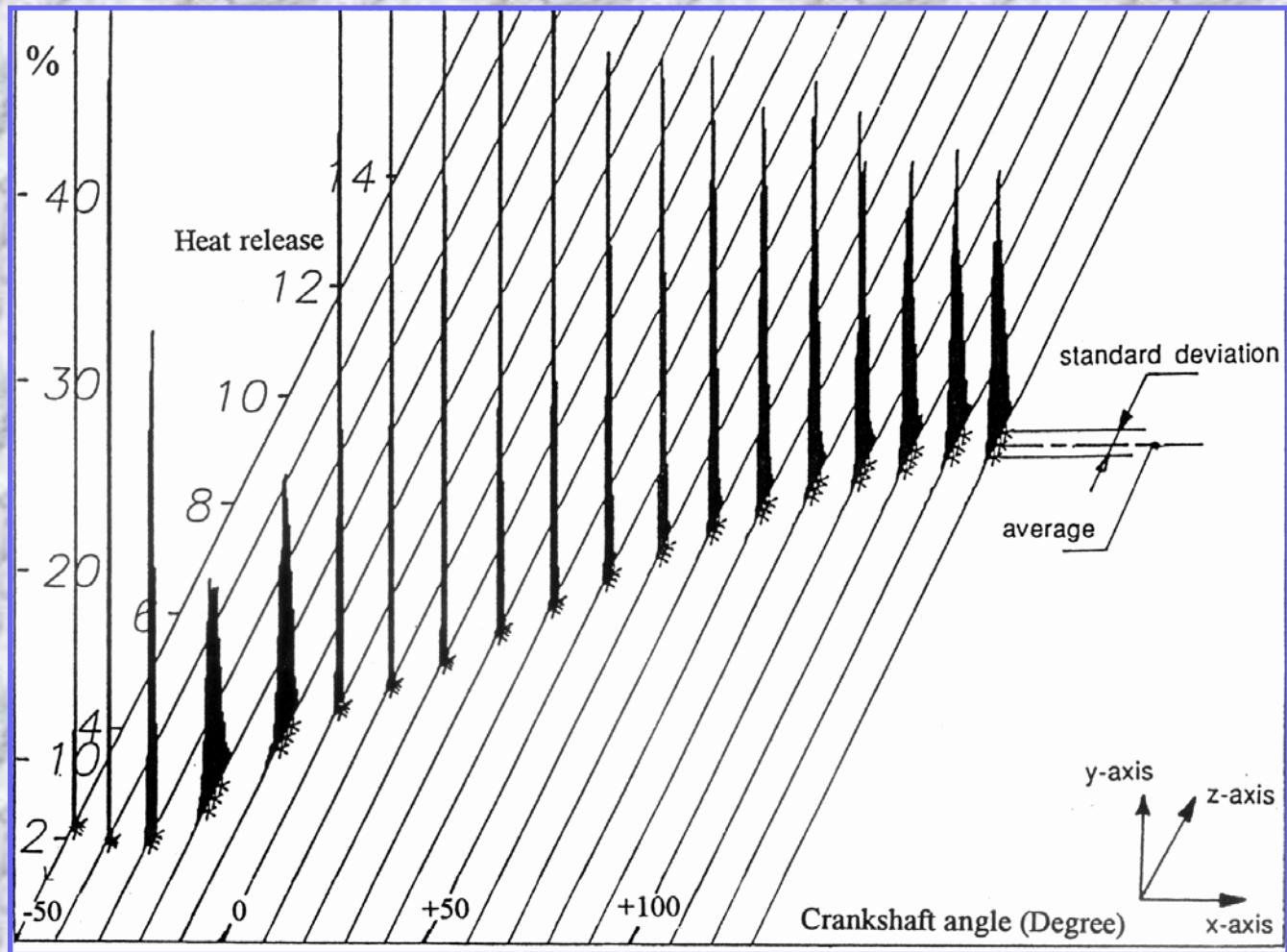
Results

I.L.S. sizes compared with LDV sizes



Dispersion of heat release

Heat release over 800 cycles



Results

- Resulting Turbulent structure sizes have been compared with L.D.V. sizes.
- Correlation between dispersion of heat release and sizes of structures is established.

Conclusions

- Non classical method to measure turbulent structures.
- Direct comparison with L.D.V.
- An other way : 2D wavelet transform to estimate Lipchitz exponent in order to measure turbulent structures in term of singularities.
- Over crossing of domains.

