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# Improving Accuracy of Timing Models: From CPA to CPA+

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# Motivation

## Verification of real-time systems and networks

ONERA, Toulouse

**Network  
Calculus (NC)**



TU Braunschweig

**Compositional  
performance  
analysis (CPA)**



- Formal timing analysis provides safe but pessimistic bounds on real-time properties for complex embedded computing systems.
  - In industrial practice, formal analysis is often replaced by simulation and test.
- ➔ **Unsatisfactory situation**

# Motivation

## Potential causes of pessimism?

### Comparison of NC and CPA

- **One interesting observation:**
  - NC is good at analyzing workload-dependent scheduling scenarios
  - CPA is good at analyzing event-dependent scheduling scenarios
- **Underlying reasons:**
  - Different system modeling

## Can we find a common input model of NC and CPA?

- Boyer et al. "Embedding network calculus and event stream theory in a common model." *ETFA* 2016.

## What does it mean to integrate this common input model in CPA?

- **This paper at *DATE* 2019, leading to CPA+.**

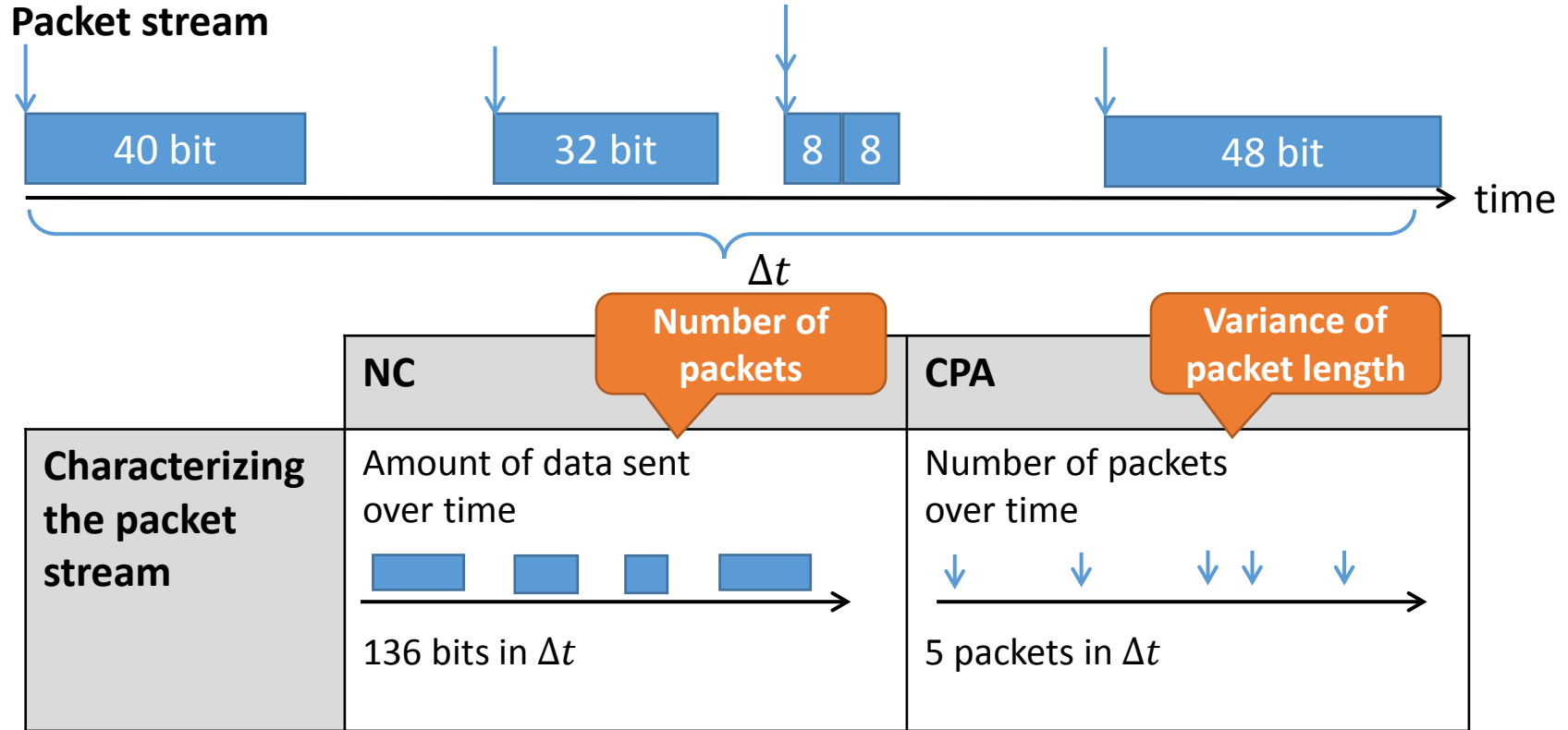
# Outline

- **Input models of CPA and NC**
  - Input model of CPA
  - Input model of NC
  - Common input model for CPA and NC [ETFA 2016]
  - Related work
- **Introducing CPA+**
  - CPA principle
  - Impact of new input model: interfaces, composition, analysis
  - Use cases
- **Conclusion**

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# Informal model of a packet stream in NC / CPA



# Formal model of a packet stream in NC / CPA

	NC (workload-based model)	CPA (event-based model)
Trace ( <i>also: flow</i> )	<p>Data flow <math>A(t)</math></p> <p><math>t</math></p>	<p>Event flow <math>E(t)</math></p> <p><math>t</math></p>
Interval Bounding Pair (IBP)	<p>Workload curves</p> <p><math>\bar{\alpha}(\Delta t)</math></p> <p><math>\underline{\alpha}(\Delta t)</math></p> <p><math>\Delta t</math></p>	<p>Event curves</p> <p><math>\bar{\eta}(\Delta t)</math></p> <p><math>\underline{\eta}(\Delta t)</math></p> <p><math>\Delta t</math></p>

# Common input model for NC/CPA

- Addition of a **packet function**  $P$ : number of packets in the first  $x$  bits of the data flow
- Interval bounding pair for  $P$ : **packet curves**  $(\underline{\pi}, \overline{\pi})$

## NC [ETFA 2016]

Workload curves  $(\underline{\alpha}, \overline{\alpha})$   
bounding data flow  $A(t)$

Packet curves  $(\underline{\pi}, \overline{\pi})$   
bounding packet function  $P$

Event curves  $(\underline{\eta}, \overline{\eta})$   
bounding event flow  $E(t)$  are **implicit**.

## CPA [ETFA 2016]

Workload curves  $(\underline{\alpha}, \overline{\alpha})$   
bounding data flow  $A(t)$  are **implicit**.

Packet curves  $(\underline{\pi}, \overline{\pi})$   
bounding packet function  $P$

Event curves  $(\underline{\eta}, \overline{\eta})$   
bounding event flow  $E(t)$

compatibility



# Common input model for NC/CPA

## What is the benefit of the common input model?

- **NC** needs to **infer information on events** during analysis.
- **CPA** needs to **infer information on workload** during analysis.

### NC: From workload to events

#### Simple transformation

$$\underline{\eta}(\Delta t) = \frac{\underline{\alpha}(\Delta t)}{p^+}$$
$$\underline{\bar{\eta}}(\Delta t) = \frac{\underline{\bar{\alpha}}(\Delta t)}{p^-}$$

#### Transformation [ETFA 2016]

$$\underline{\eta}(\Delta t) = (\underline{\pi} \circ \underline{\alpha})(\Delta t)$$
$$\underline{\bar{\eta}}(\Delta t) = (\underline{\pi} \circ \underline{\bar{\alpha}})(\Delta t)$$

lossless

### CPA: From events to workload

#### Simple transformation

$$\underline{\alpha}(\Delta t) = p^- \cdot \underline{\eta}(\Delta t)$$
$$\underline{\bar{\alpha}}(\Delta t) = p^+ \cdot \underline{\bar{\eta}}(\Delta t)$$

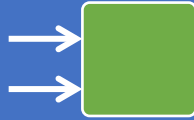
#### Transformation [ETFA 2016]

$$\underline{\alpha}(\Delta t) = (\underline{\pi}^{-1} \circ \underline{\eta})(\Delta t)$$
$$\underline{\bar{\alpha}}(\Delta t) = (\underline{\pi}^{-1} \circ \underline{\bar{\eta}})(\Delta t)$$

bit arrival rates are lost

# Related work

component  
with workload-event  
input model



Add variation in  
packet sizes

*Mok et al. 1997*

*Quinton et al.  
2012*

Add information on  
events

*Wandeler et al.  
2005*

*Bouillard et al.  
2011 + 2012*

Compatible input model for NC/CPA

*Boyer et al. 2016*

Composition  
of components



NC

*Wandeler et al.  
2005*

*Bouillard et al.  
2011 + 2012*

*Boyer et al. 2016*

CPA

Contribution  
DATE 2019

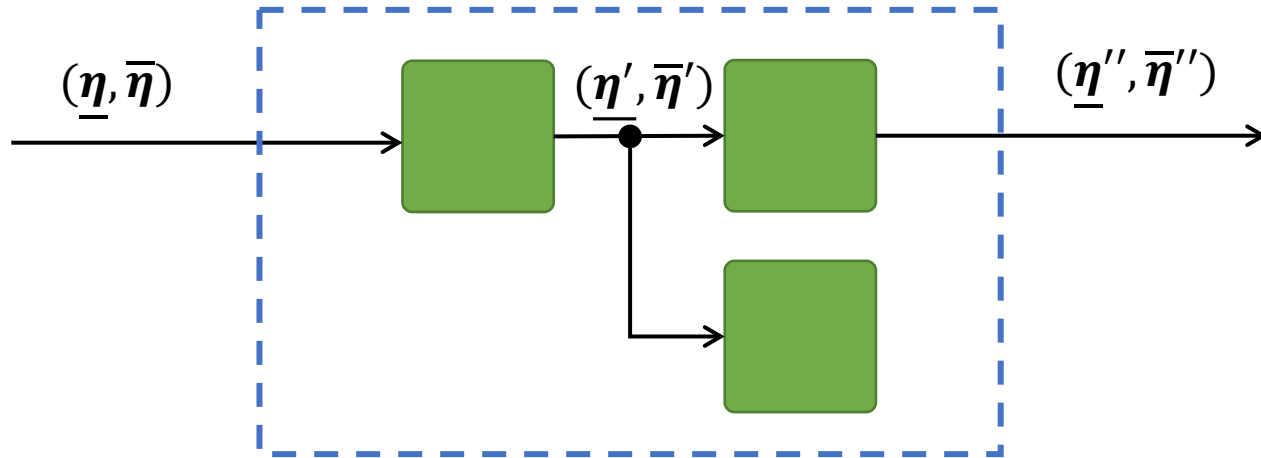
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# CPA principle

Compositional approach:

- **Global analysis problem** is decomposed into dependent **local analysis problems**
- Dependencies are represented by **event streams**

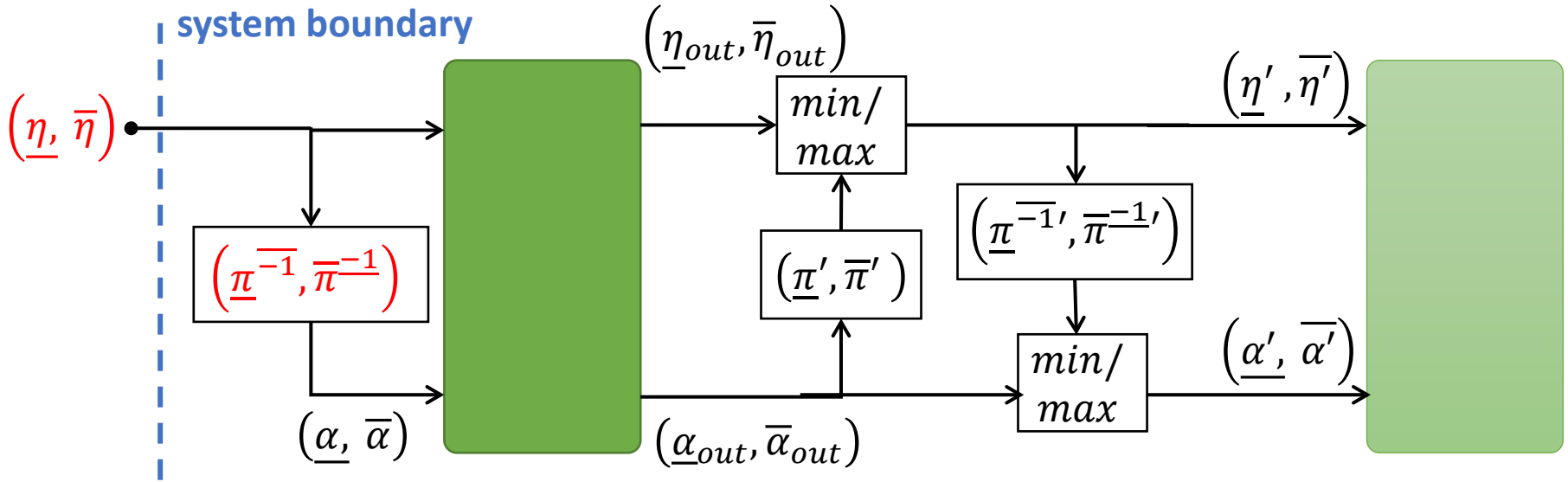


New input model  
will change  
interfaces of local  
analysis problems.

Composition of local  
analysis problems?

Internals of local  
analysis problems?

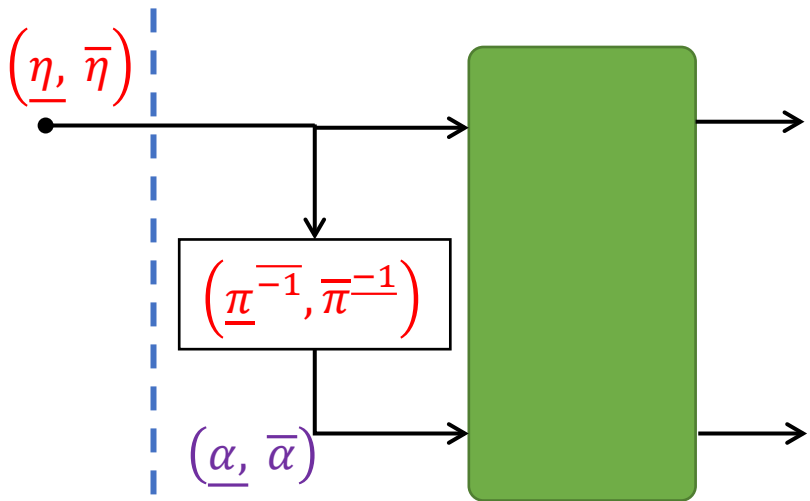
# Naïve interface and composition



- **Lossy event-to-workload transformation at the input**
- **Composition allows lossy chained transformations**

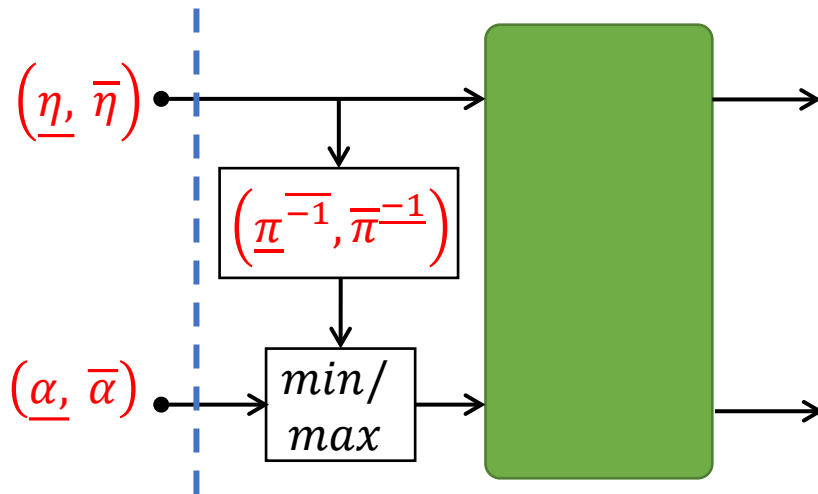
# Interface issues

## Lossy event-to-workload transformation at the input



**2 primary inputs:** events + packet sizes  
**1 implicit input:** workload

## Better:

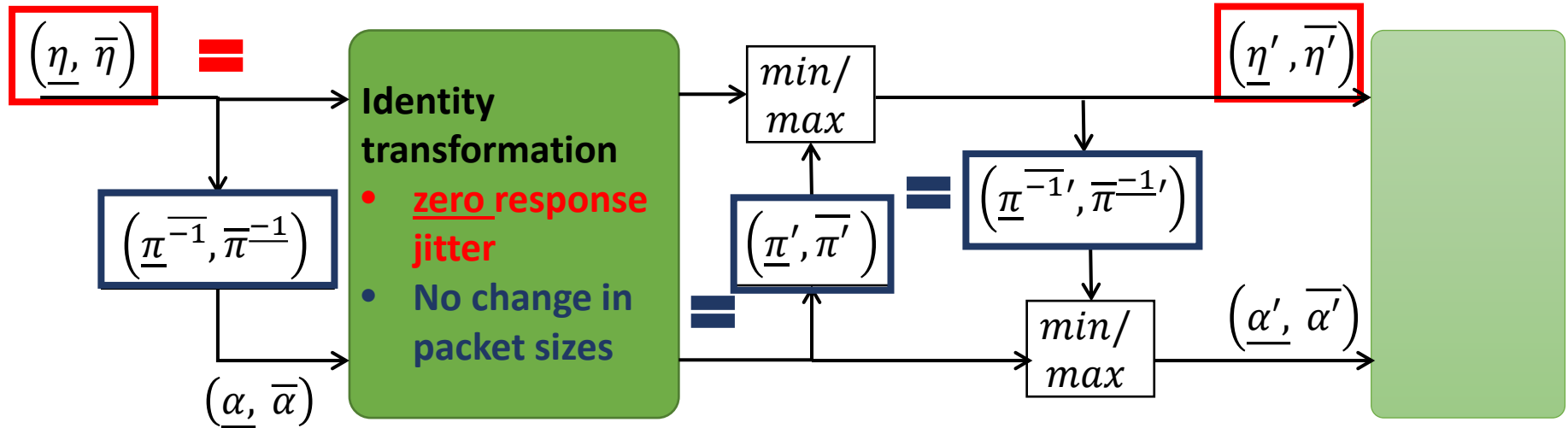


**3 primary inputs:**  
Events, workload and packets

# Composition issues

## Chained transformations in the naïve composition

Example:



es

1<sup>st</sup> transf.: event-to-workload

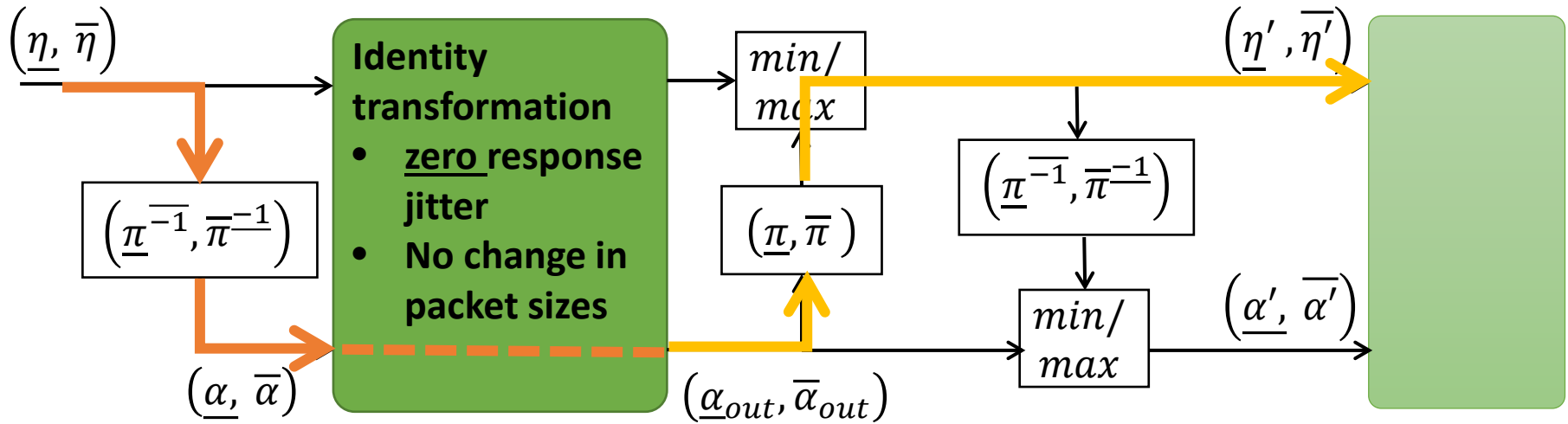
$$\bar{\alpha}_{out}(\Delta t) = (\bar{\pi}^{-1} \circ \bar{\eta})(\Delta t)$$

Maximum workload = largest packets combined with maximum event number

2nd transf.: workload-to-event

$$\bar{\eta}'(\Delta t) = (\underline{\pi} \circ \bar{\alpha}_{out})(\Delta t)$$

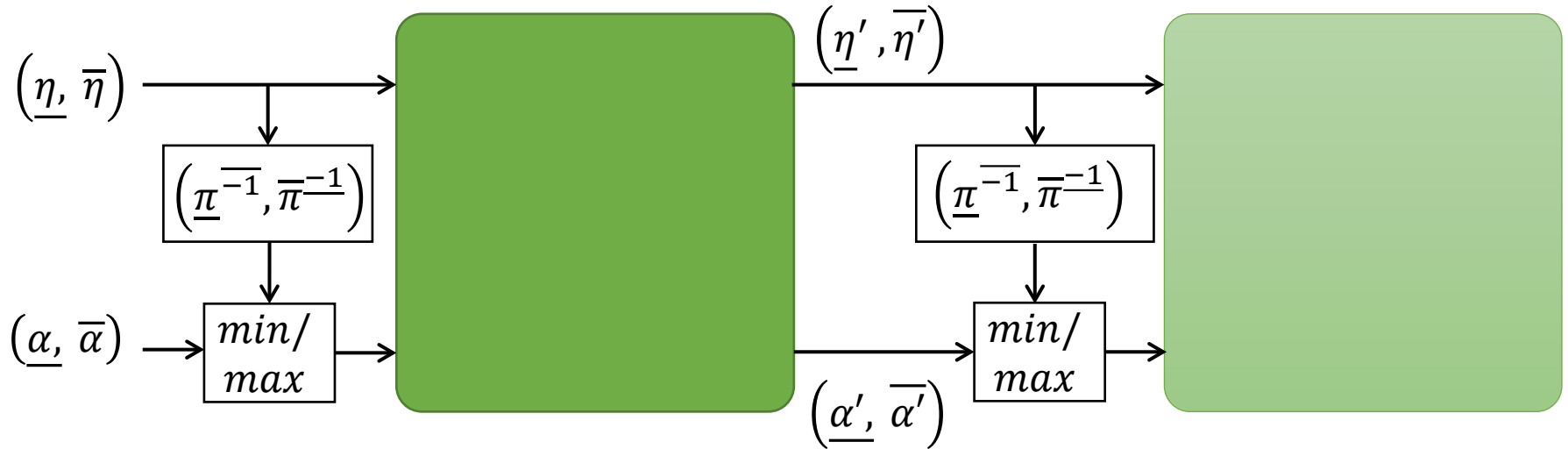
Maximum number of events = smallest packets combined with maximum workload



$$\bar{\eta}'(\Delta t) = (\underline{\pi} \circ \bar{\pi}^{-1} \circ \bar{\eta})(\Delta t) \Rightarrow \bar{\eta}'(\Delta t) > \bar{\eta}(\Delta t)$$

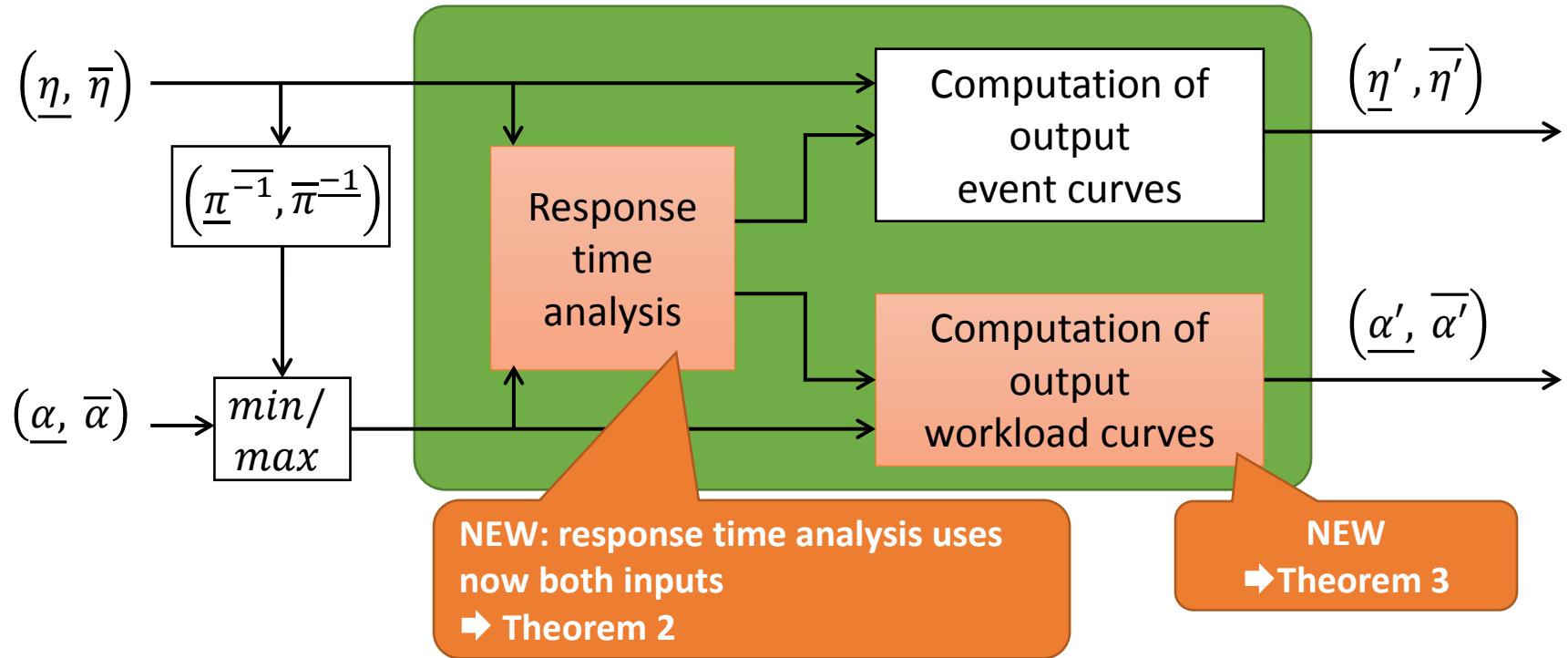


# Improved interface and composition



- ✓ Three primary inputs
- ✓ Elimination of chained transformations:  
only event-to-workload transformations are allowed.

# Impact on the local analysis problem



# Use Cases for Event-Workload-Dualism in NC and CPA

## Multi-component system with complex schedulers

- event-centered scheduler, e.g., round robin
  - Distinction of individual packets (events) is important!
- workload-centered scheduler, e.g., budget-based scheduling
  - Sent data over time is important (workload), not number of packets!
- scheduler depending on events and workload, e.g., packetizer
  - Packet dispatch on time-out, buffer-full, high-priority event, ...
- **Multi-component system with different service specifications**
  - per-event service specification, e.g., decoder
  - per-workload service specification, e.g., processor

# Use Cases for Event-Workload-Dualism in NC and CPA

- **Computation of buffer filling**

- **per-packet (event-based)**



- **per-byte (workload-based)**



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# Conclusion

## Problem:

- Apply a **dual (event-workload) input model** to CPA

## Solution: CPA+

- Define and compute a **dual (event-workload) output model** for CPA components
- Define **new composition rules** for CPA components
- Update **response-time analysis** within CPA components.

## Benefits:

- Accurate system model and analysis for complex systems
- Compatability of NC and CPA+

## Future work:

- joint tool of NC and CPA+